



Multi-Parton Interactions in Experiments

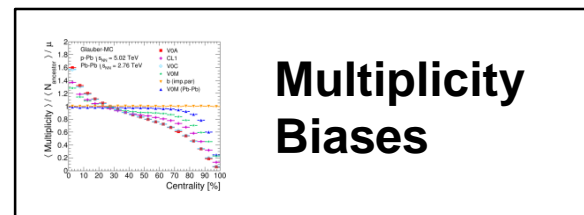
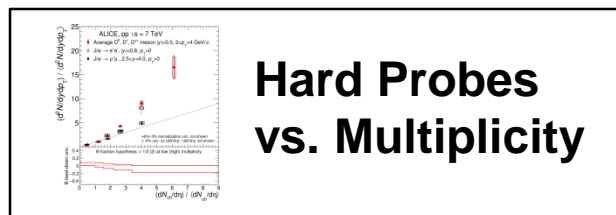
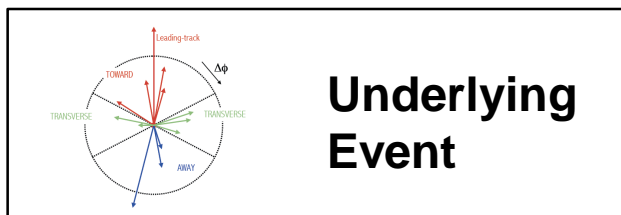
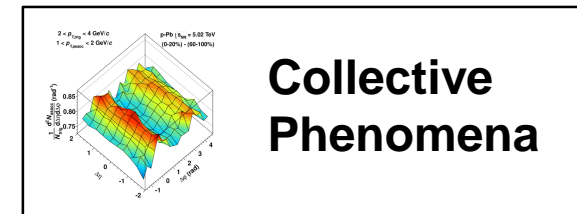
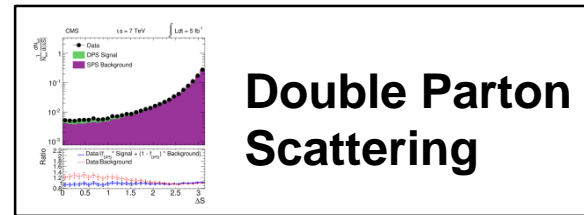
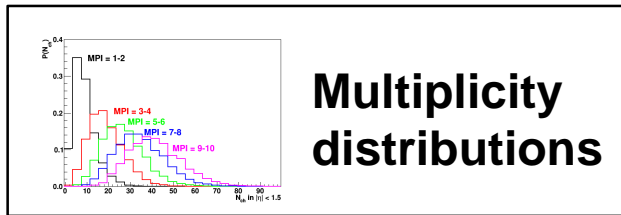
Jan Fiete Grosse-Oetringhaus, CERN

37th Joliot-Curie International School, La Grande Motte

October 2018

This Lecture

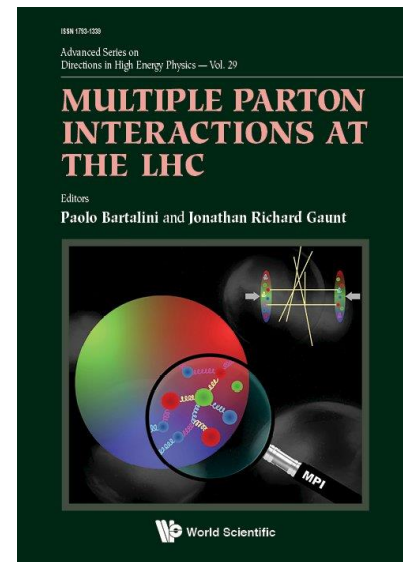
- Discuss measurements sensitive to or related to multi-parton interactions
 - Available observables (soft and hard)
 - Definition and measurement procedure (including selected details how to reproduce them)
 - Results and interpretation
 - Influence of MPI





Further Reading

- Multiplicity
 - JFGO, PhD thesis, [link](#)
- Underlying Event
 - Sara Vallero, PhD thesis, [link](#)
- Uncorrelated seeds / minijets
 - In pp: Eva Sicking, PhD thesis, [link](#),
 - In p-Pb: Emilia Leogrande, PhD thesis, [link](#)
- Hard Probes vs. Multiplicity
 - Javier Blanco, PhD thesis, [link](#)
- Concepts of multiplicity biases
 - Phys. Rev. C 91 (2015) 064905, [arXiv link](#)
- Multiple Parton Interactions at the LHC, [ISBN: 978-981-3227-75-0](#)





Multiplicity Distributions



Multiplicity Distributions

cities. The present availability of bubble-chamber facilities at Serpukhov, U. S. S. R., and at Batavia, U. S. A., has consequently made available for the first time accurate measurements of topological cross sections for very high-energy proton-proton collisions (50–300 GeV/c). In this

- Multiplicity distribution $P(N_{ch}) =$ probability that event has certain (charged) multiplicity
 - Within p_T and η phase space (due to detectors)

Fixed target collisions
→ cms: 10-24 GeV
Find the math [here](#)

- Very sensitive to MPI

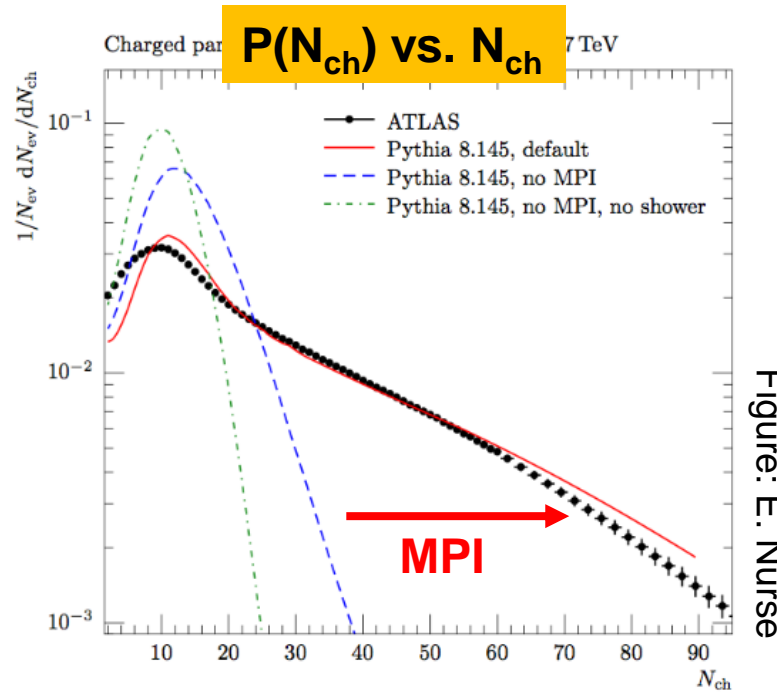
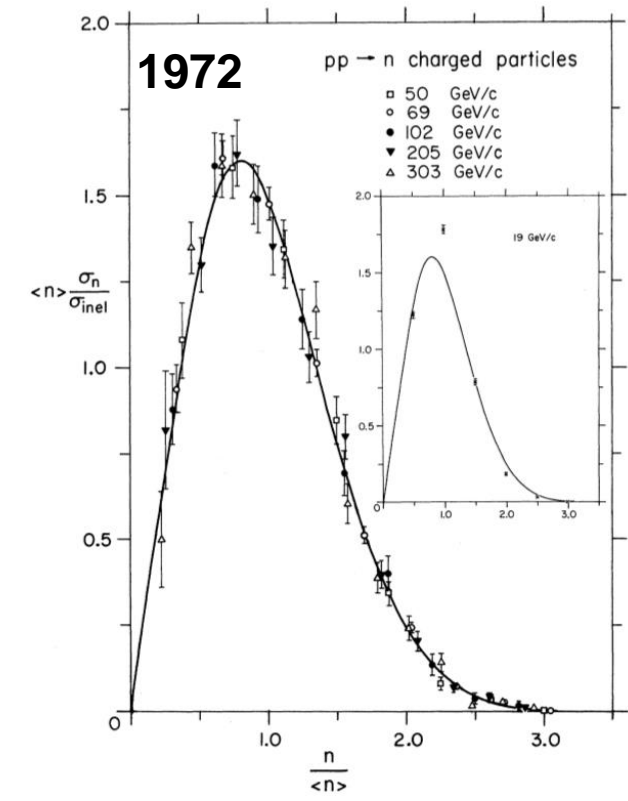


Figure: E. Nurse

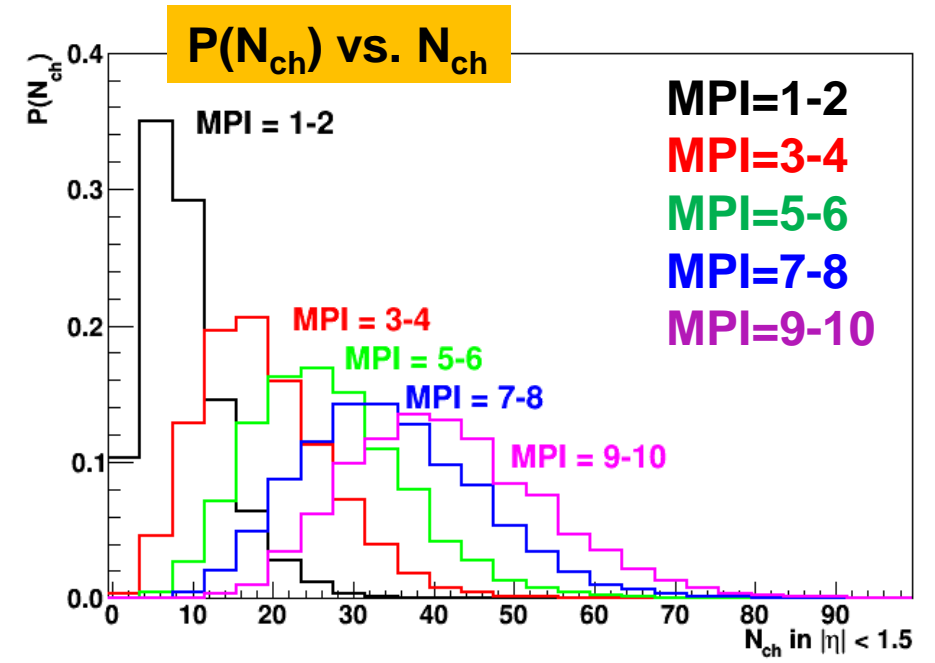
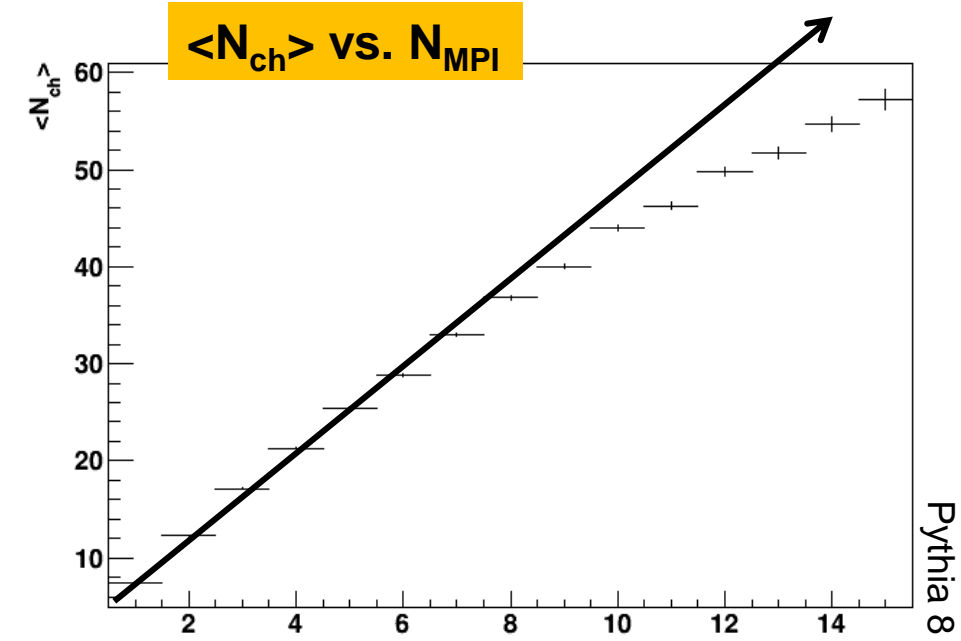


PRL29(1972)24



Multiplicity vs. MPI

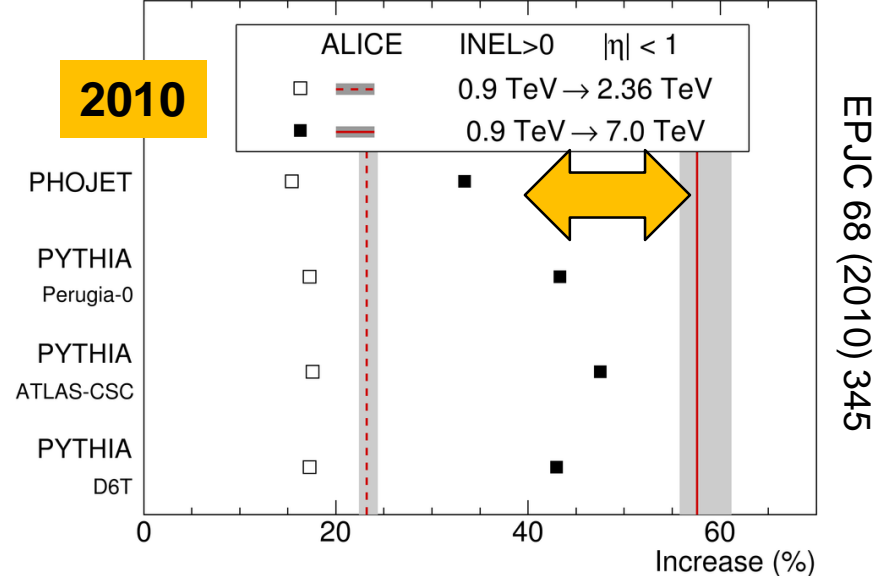
- $\langle N_{ch} \rangle$ grows almost linearly with #PI
- Multiplicity distribution strongly depends on number of PI
 - Larger values not reached with few PI
 - Small values not reached with many PI
- Multiplicity distribution, in particular its tail, has large influence on MPI related parameters in MC tuning
- Unfortunately, not possible to measure $P(N_{ch})$ as a function of #PI





Average Multiplicities

- Average multiplicities at LHC energies
 - Faster increase than expected by MCs
- Indication for higher MPI activity
- MCs retuned affecting MPI
 - p matter distribution
→ affects impact parameter distribution
 - $p_{T,min}(\sqrt{s})$



EPJ C 68 (2010) 345

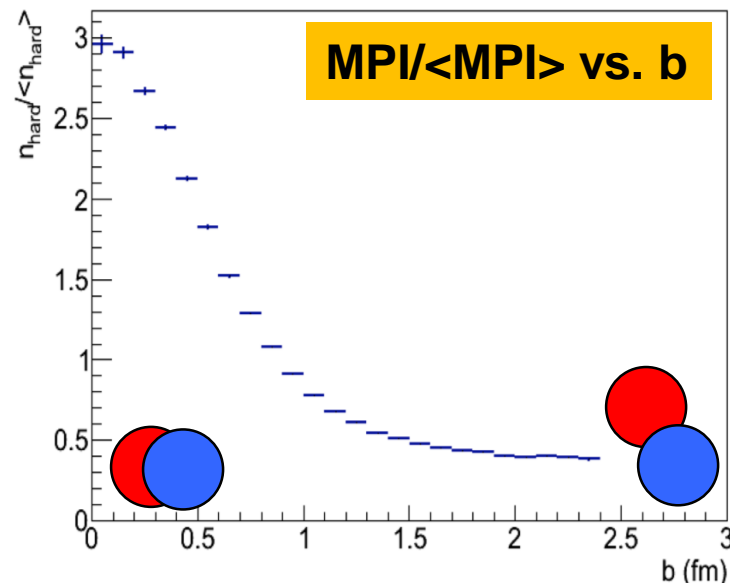
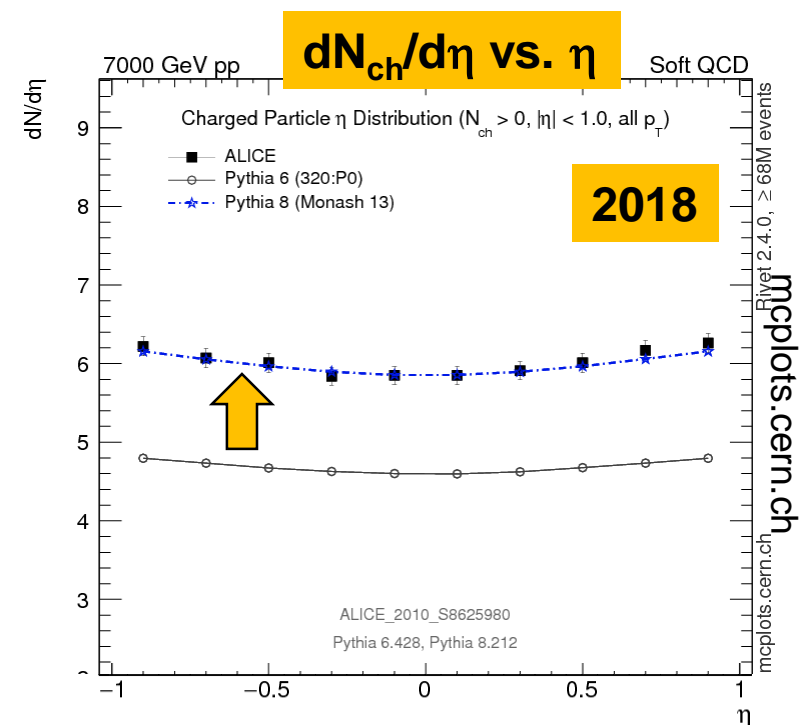


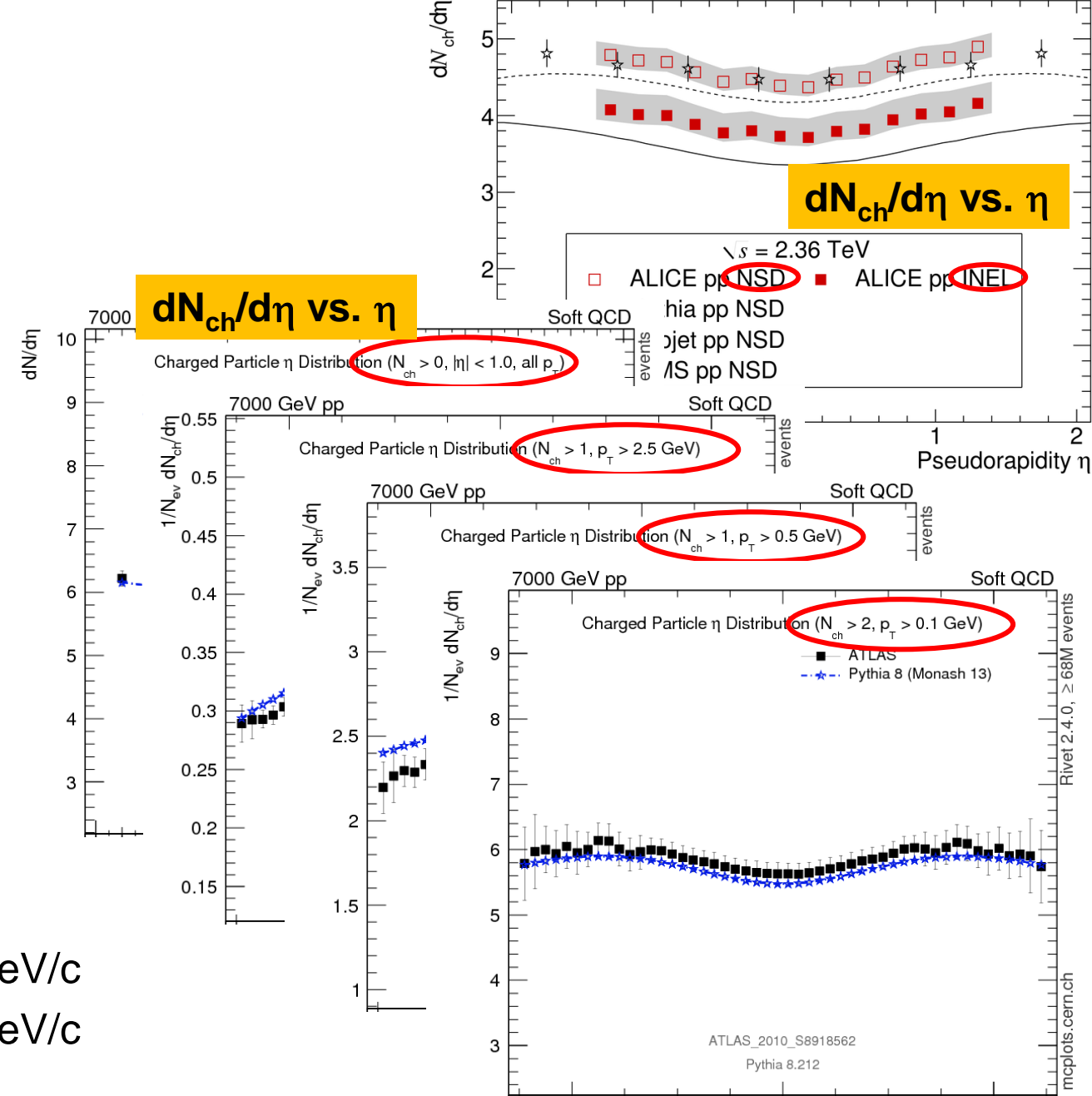
Figure: Andreas Morsch



mcplots.cern.ch
 mcplots.cern.ch
 Rivet 2.4.0, ≥ 68M events

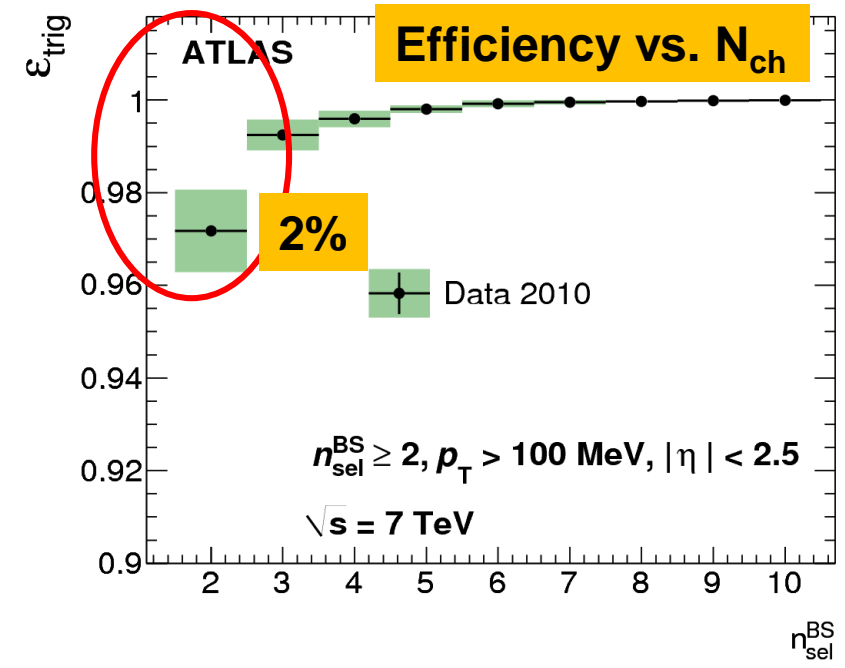
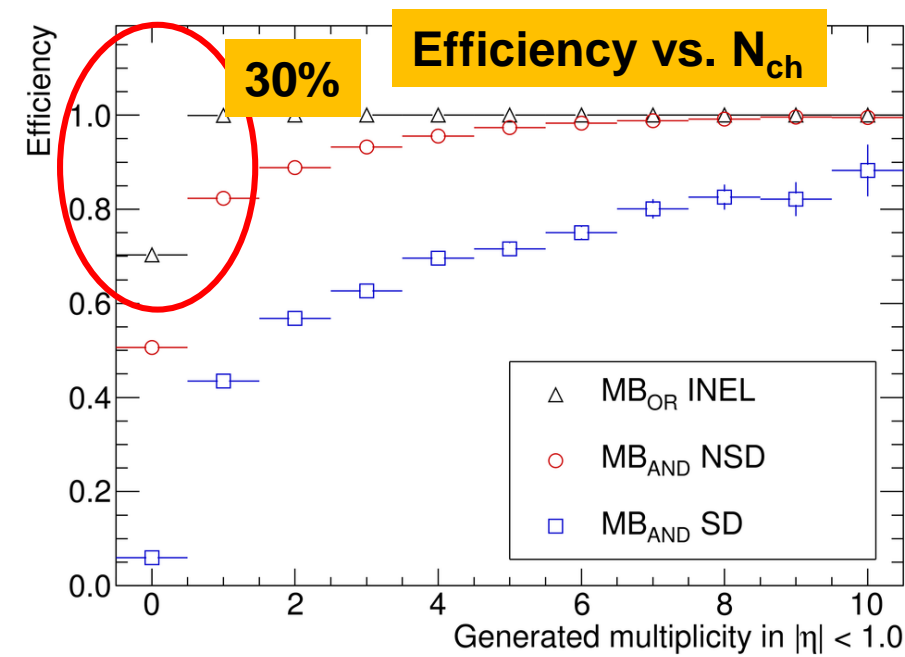
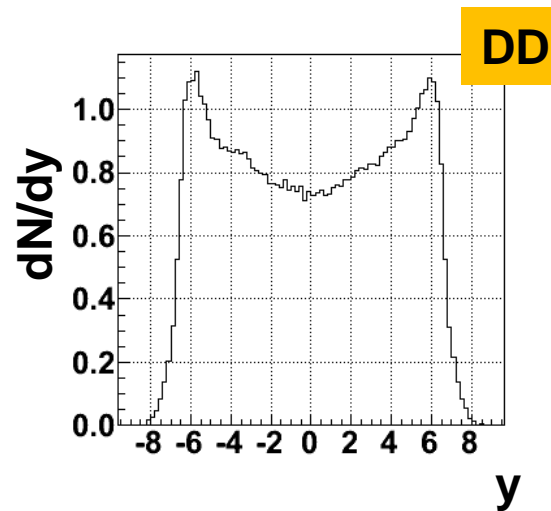
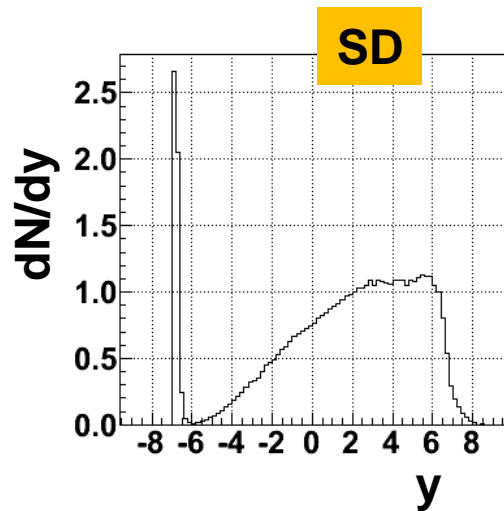
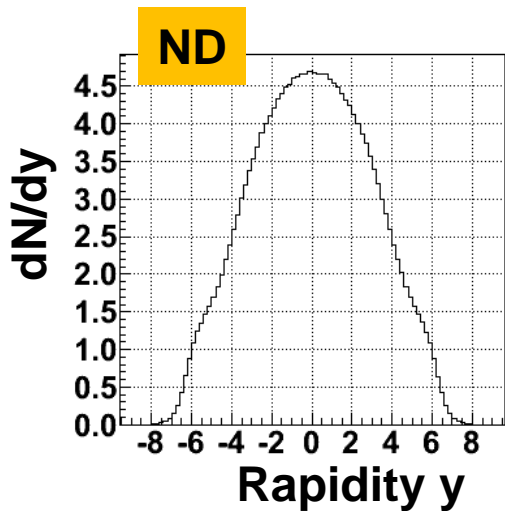
Event Classes

- Inelastic collisions
 - Non-diffractive and diffractive
 - Single and double diffractive, ...
 - Some not measured
- Traditional classes: inelastic (“INEL”) and non-single diffractive (NSD)
- Large uncertainties in corrections
- Avoided by particle-level definitions
 - At least N particles within phase space
- Examples
 - ALICE INEL >0 : $N_{ch} \geq 1$ in $|\eta| < 1$
 - ATLAS: $N_{ch} \geq 1$ in $|\eta| < 2.5$ and $p_T > 0.5$ GeV/c
 - ATLAS: $N_{ch} \geq 2$ in $|\eta| < 2.5$ and $p_T > 0.1$ GeV/c



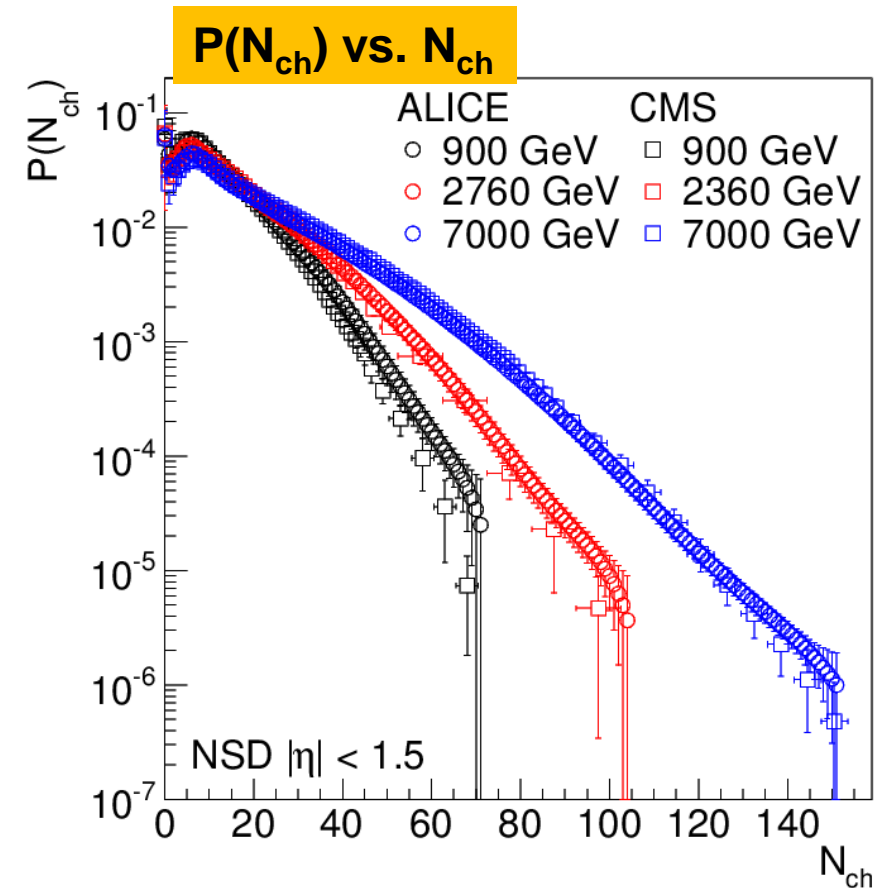
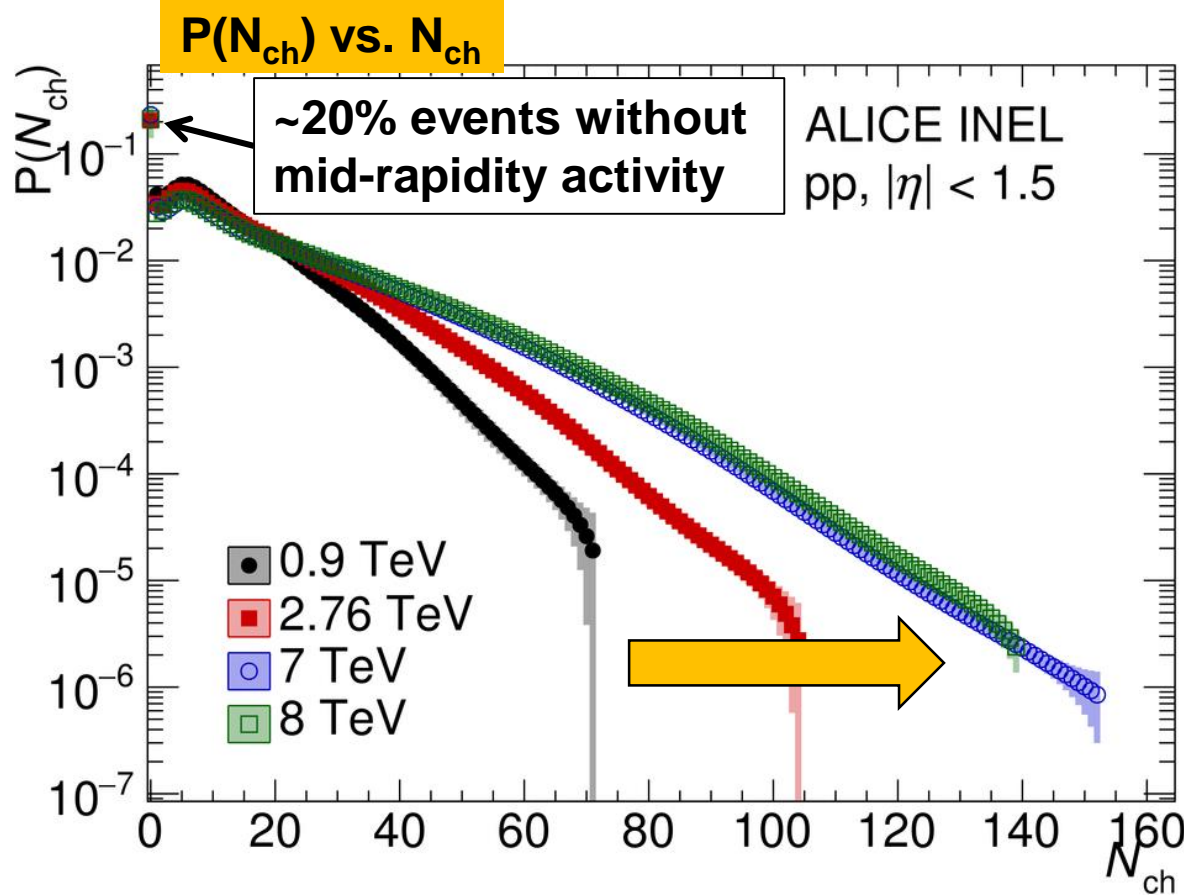
Event Classes & Triggers

- Event types have different topologies
- Non triggered fraction MC dependent
- Particle-level definition reduces not triggered fraction
 - Reduces overall uncertainties



Multiplicity Distributions

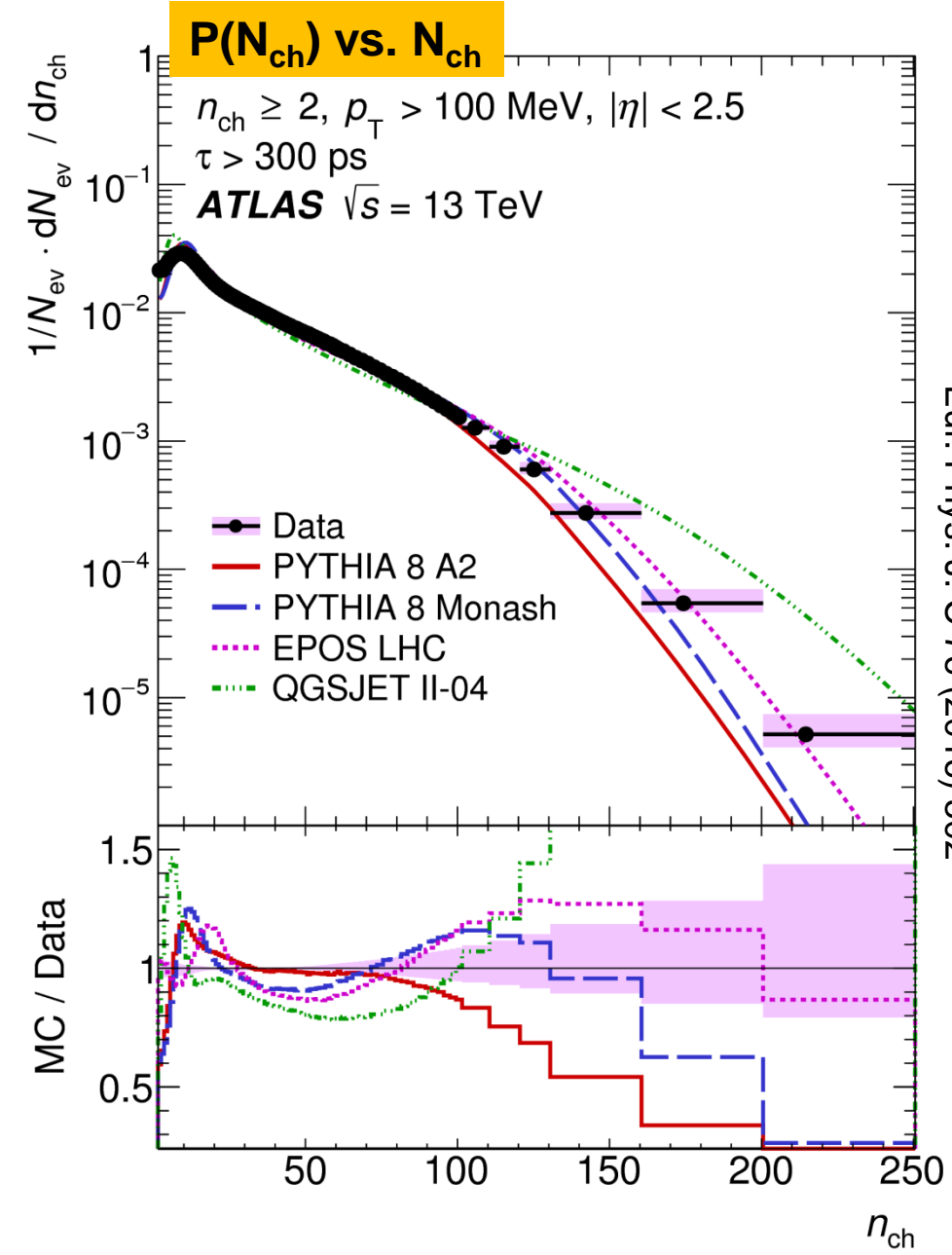
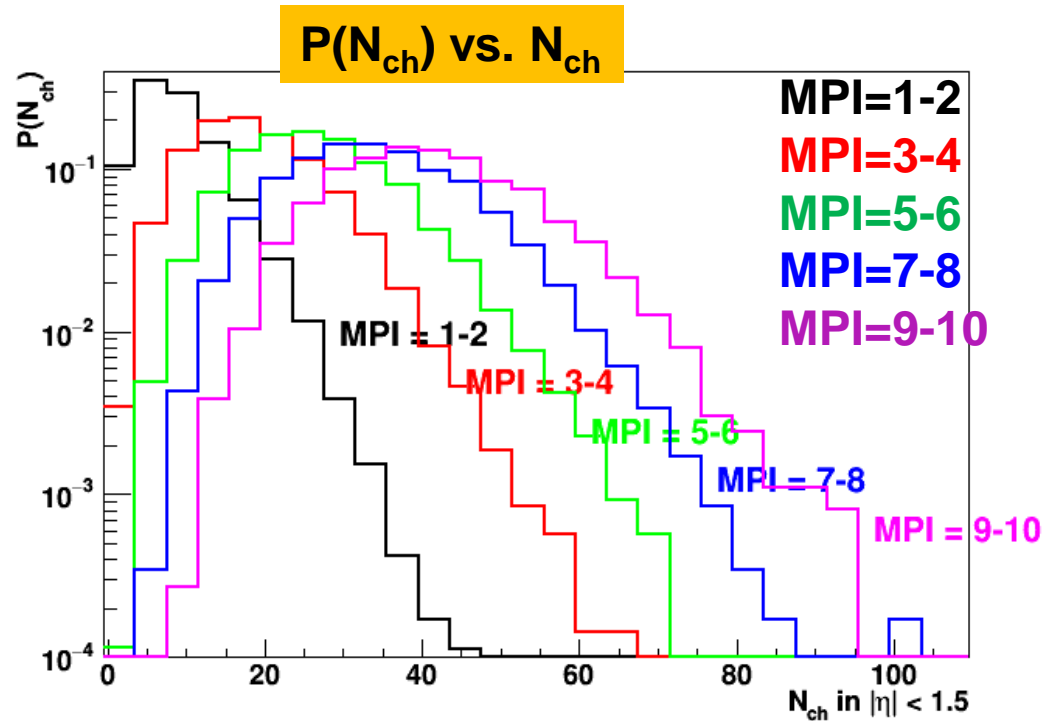
- Tail widens with \sqrt{s}
- Up to 150 particles in $|\eta| < 1.5$
- Agreement among experiments over 5 orders of magnitude





... and MCs

- Even state of the art MCs have a hard time for an exact description
 - Deviations of 20...50% easily occur
- Recap: tail is sensitive to large number of PI

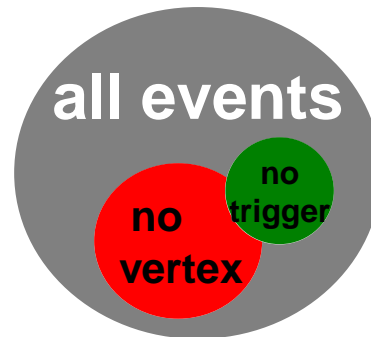


Eur. Phys. J. C 76 (2016) 502

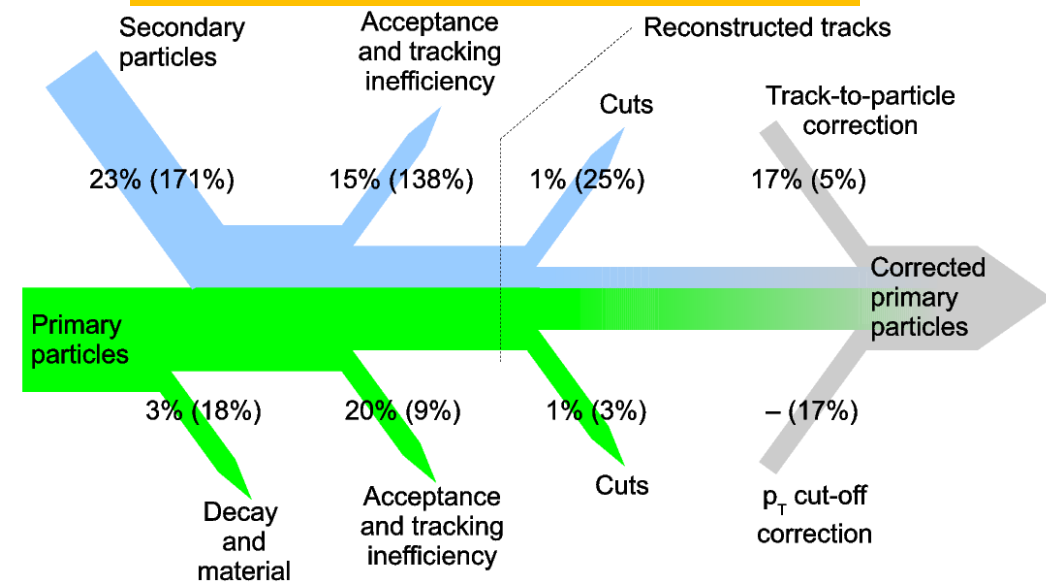
Corrections

How to measure

- Published multiplicity distribution \neq raw measurement
 - Usually causes lots of stress 😊
- Event-level corrections
 - Events skipped by trigger or vertex reconstruction
 - Migration in and out of desired event class
- Track-level corrections
 - Efficiency, secondaries
- Resolution
 - Track level (p_T) and event level (N_{ch})
→ unfolding



Example for ALICE SPD (TPC)

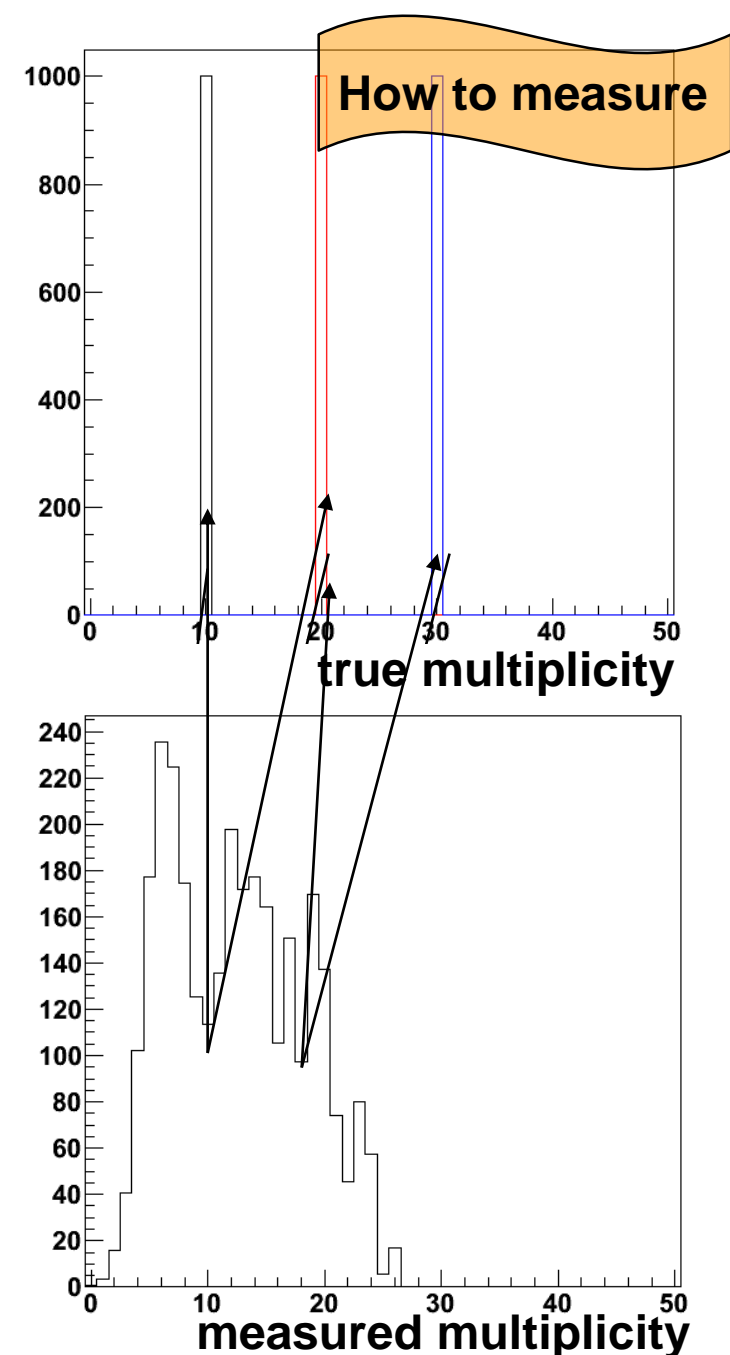


Unfolding is an important concept, I use the example of the multiplicity distribution to introduce it here



Unfolding

- Unfolding is
 - the estimation of a probability distribution for which (usually) no parametric form is available
 - where the data are subject to additional random fluctuations due to limited resolution
- Sometimes discussed as *inverse problem*, sometimes called *deconvolution* and *unsmearing*
- Unfolding
 - reverts bin flow (i.e. tries to recover information which you don't have)
 - assigns events or tracks in a reconstructed bin to their originating (true) bin on a statistical basis
 - probability distributions are transformed
 - no information about the origin of a *single* event is obtained





Unfolding - Mathematically

How to measure

- Measurement = folding with detector response
- Almost all practical purposes
 - Binning, discrete case \rightarrow matrix / vector notation
- Unfolding
 - Inversion of the folding by the detector
 - Discrete: Inversion of a matrix
- T (M) is the expectation value of the true (measured) distribution
- One measurement provides M^* for which $E[M^*] = M$
- Based on M^* we want to find an estimator T^* for T
 - Should be unbiased, i.e. $b = E[T^*] - T = 0$
 - Smallest variance as possible
- NB: this formulation neglects background

$$f_{meas}(x) = \int R(x | y) f_{true}(y) dy$$

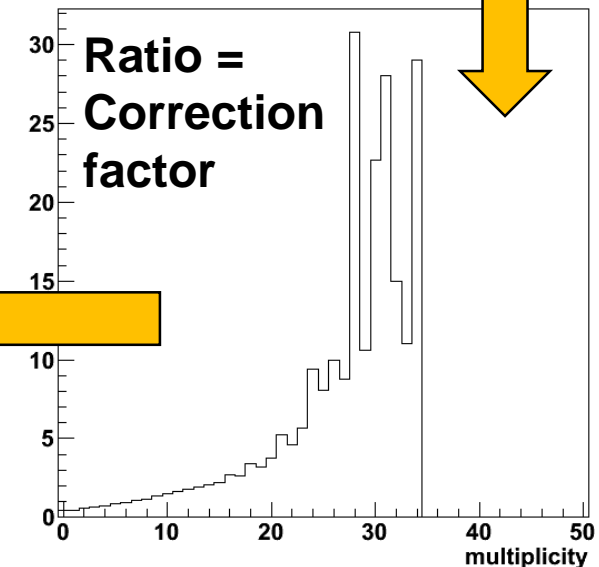
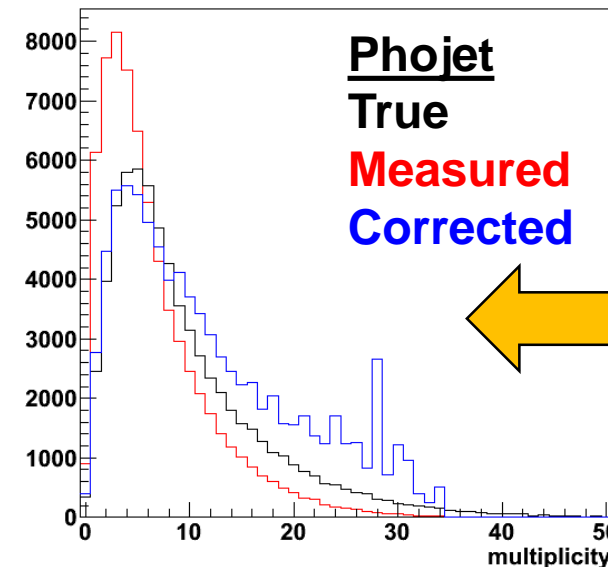
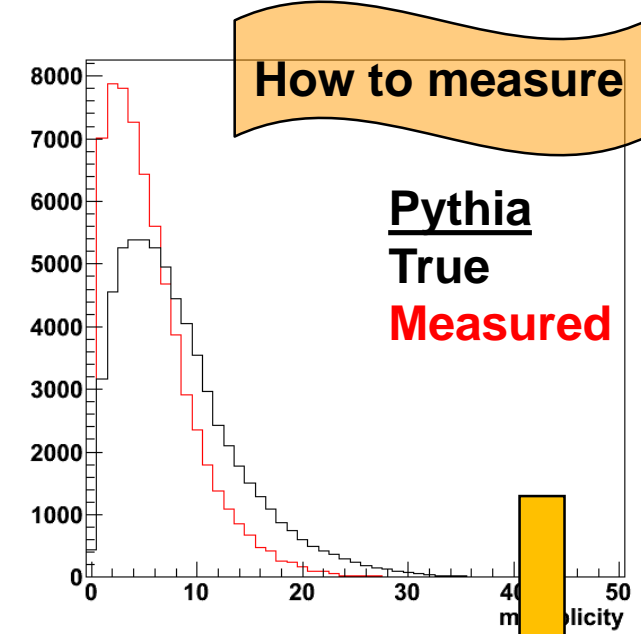
$$M = RT$$

$$R^{-1}M = T$$

$$M = RT + BG$$

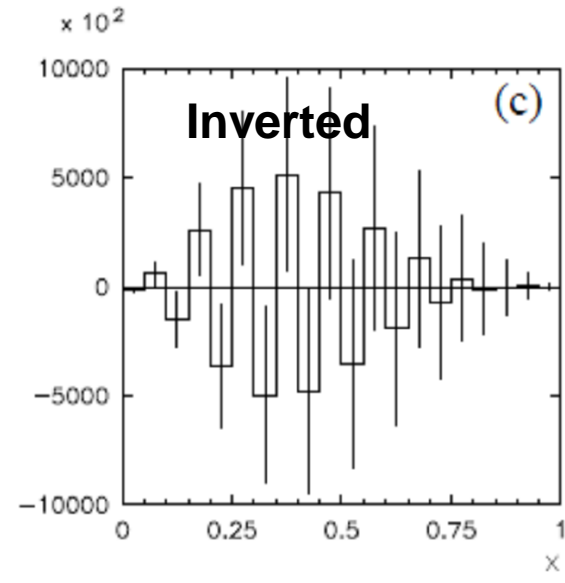
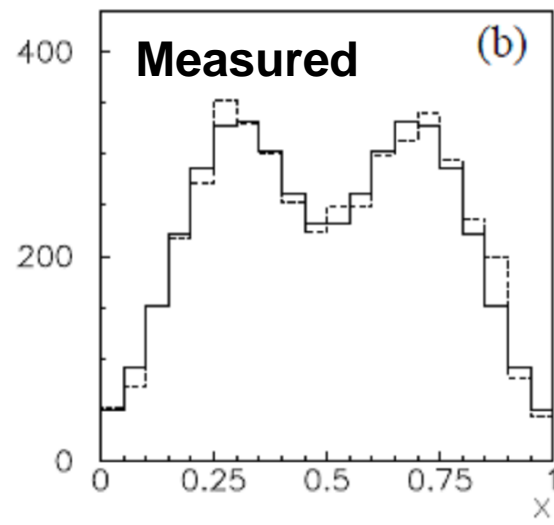
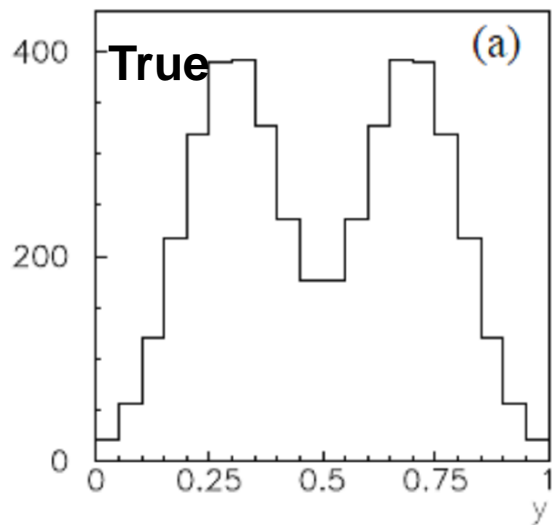
Why is it needed?

- Many analyses correct bin by bin
 - Choose binning appropriate for analysis
 - One correction factor per bin
- Correct when
 - there is only a negligible amount of bin migration
 - distributions are not steeply falling
- Incorrect when
 - there is significant bin migration
 - distributions fall steeply
 - MC does not describe the data
- Example
 - Bin by bin correction factor from Pythia to correct Phojet sample
→ Significant deviation



Why is it difficult?

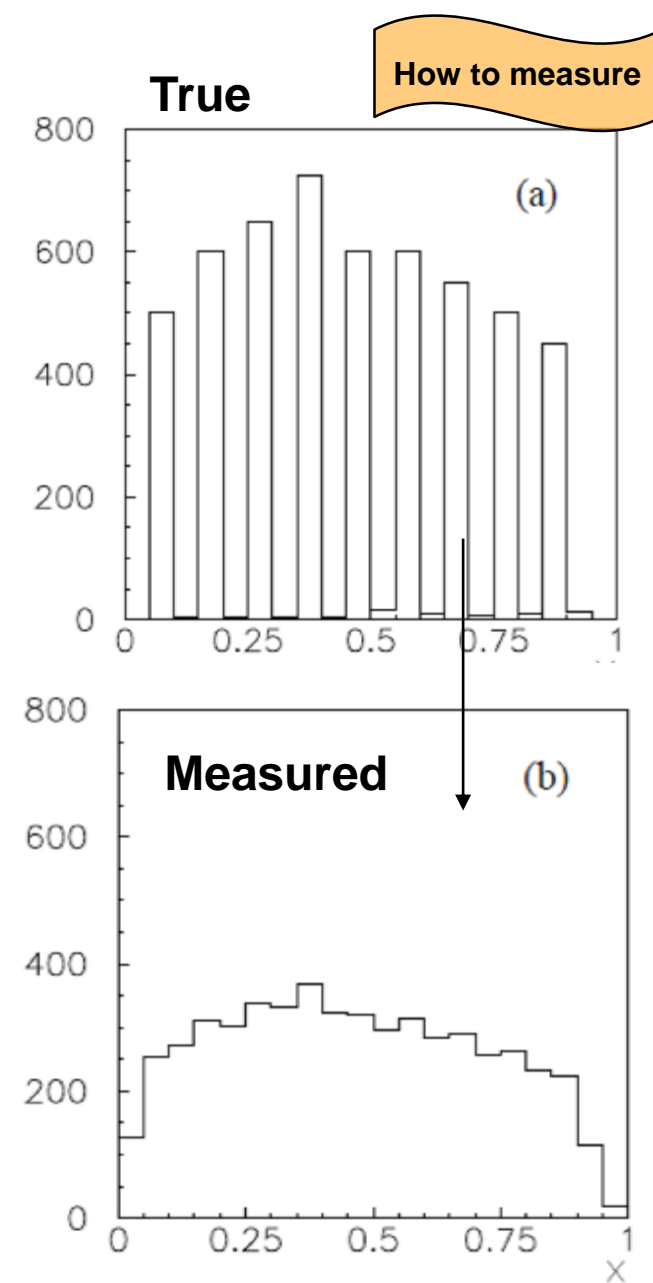
- Easiest approach: matrix inversion $R^{-1}M = T$
- If bin size smaller than resolution
 - Large off diagonal elements in R^{-1}
 - Negative correlations between neighboring bins
- Inverted solution
 - Suffers from large (non-physical) fluctuations
 - Can be understood \rightarrow (potential) fine structure cannot be resolved by detector



from Cowan, A survey of unfolding methods for particle physics

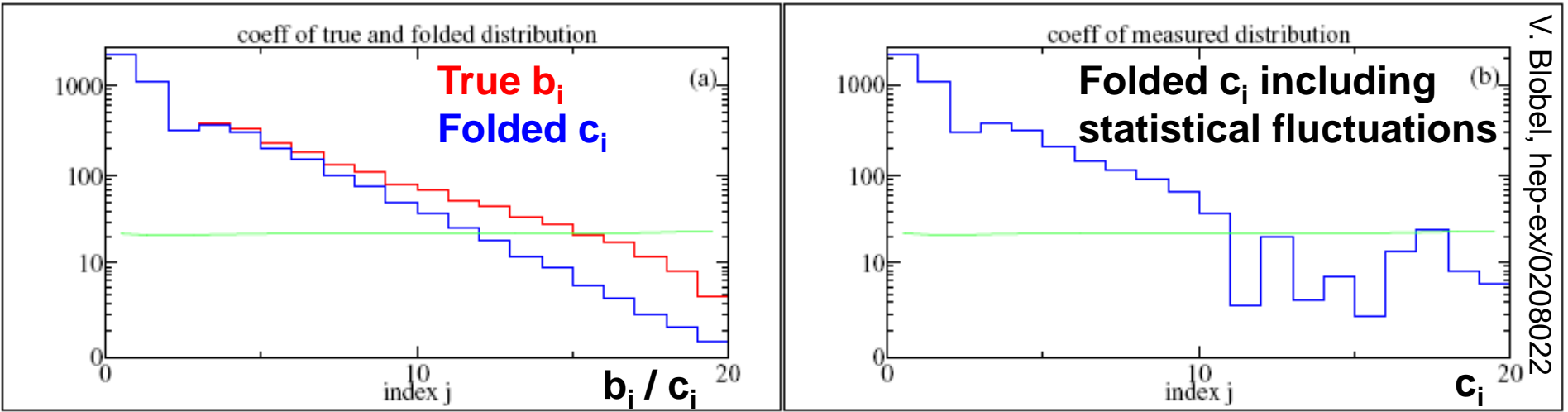
Why is it difficult? (2)

- A true distribution with a fine structure would also appear smooth in the detector
- Solution found by matrix inversion
 - Unbiased $b = E[T^*] - T = 0$
 - Huge variance, but smallest variance of all unbiased estimators
 - Solutions with smaller variance will have a bias
- Need to trade variance against bias
 - unfolding methods discussed today

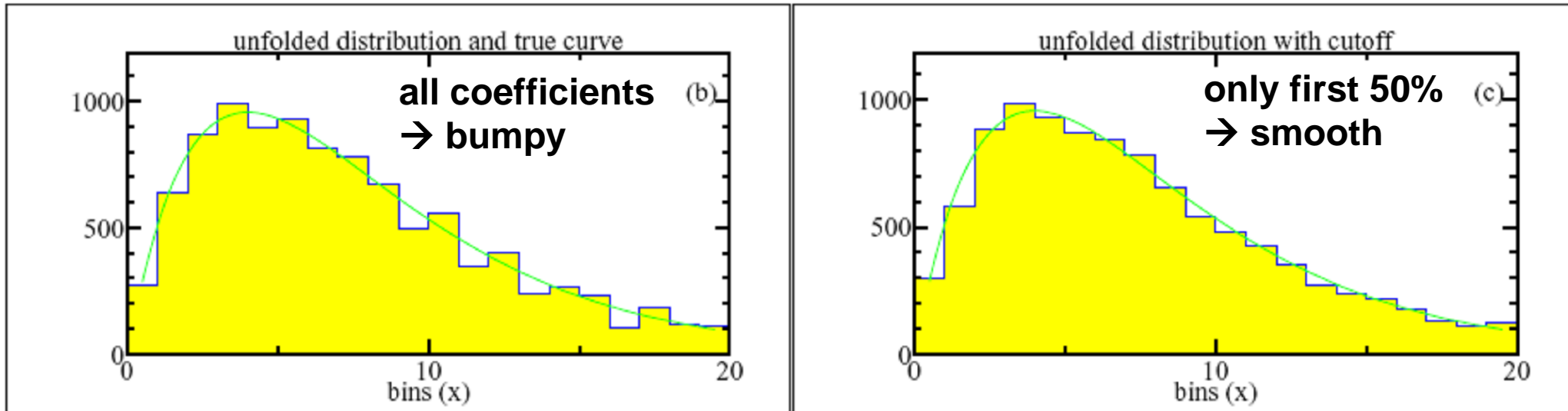


Regularized Unfolding

- Basic equation $M = RT$
- Diagonalise response matrix $R = UDU^T$
 - D diagonal with eigenvalues of R, largest first
- Transformation matrix U with $U^T U = 1$
- Rewrite $M = UDU^T T \rightarrow U^T M = DU^T T \quad c = Db$
- Transformation $b \leftrightarrow c$ (folding) became multiplication with eigenvalues



- Regularization = select which coefficients to keep



- How to select coefficients in unfolding?
 - χ^2 minimization with regularization (acts like a smooth cut-off)
 - Iterative Bayesian unfolding with limited number of iterations
 - Small eigenvalues converge slower than larger ones!



χ^2 -Minimization with Regularization

How to measure

- Find the spectrum by minimizing a χ^2 function

$$\chi^2(T^*) = \underbrace{\sum_m \left(\frac{M_m^* - \sum_t R_{mt} T_t^*}{e_m} \right)^2}_{\text{“Typical” } \chi^2 \text{ term}} + \underbrace{\beta R(T^*)}_{\text{regularization term}}$$

- $R(T^*)$ only depends on unfolded guess T^*
- Weight β balances the two terms
- Without regularization term, same result as found by matrix inversion
 - One can show that the solutions are equivalent



Regularization

How to measure

- Simple functional form which smoothens result

- Don't add information through this term = Don't impose how it should look like
- E.g. if you look for an exponential, don't regularize with an exponential

- Weight parameter β needs to be tuned

$$R(T) = \sum_t (a_t)^2$$

$$a_t = \frac{T_t'}{\sqrt{T_t}} = \frac{T_t - T_{t-1}}{\sqrt{T_t}} \quad \text{prefer constant}$$

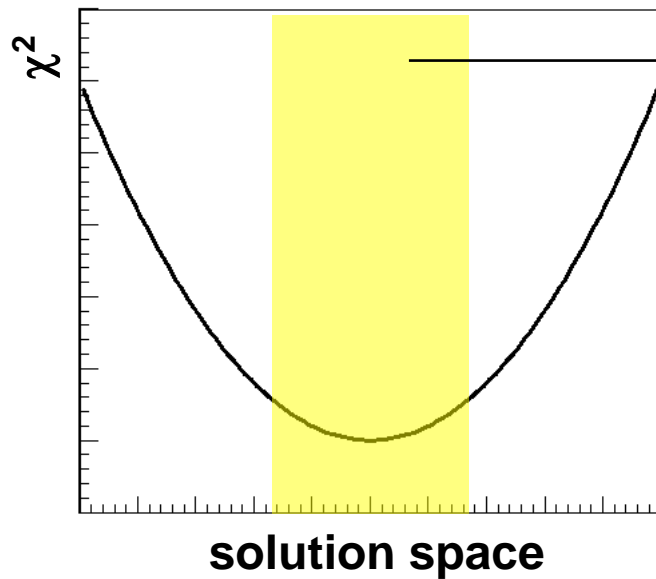
$$a_t = \frac{T_t''}{\sqrt{T_t}} = \frac{T_{t-1} + 2T_t - T_{t+1}}{\sqrt{T_t}} \quad \text{prefer linear least curvature}$$

$$a_t = \frac{\hat{T}_t''}{\sqrt{\hat{T}_t}} \quad \hat{T}_t = \ln T_t \quad \text{prefer exp}$$

$$R(T) = \sum_t T_t \ln \frac{T_t}{\varepsilon_t} \quad \text{reduced cross-entropy}$$

NB: Regularizations based on derivatives can be implemented as matrix operation → optimization

- Conceptually, instead of choosing the solution with the smallest χ^2
 - one accepts a higher χ^2
 - so that the result is smooth



**choose the most smooth
solution in a window defined by
 $\chi^2 < \chi^2_{\min} + \Delta\chi^2$**

Residuals

- Residuals assess if unfolded distribution reproduces measurement

- First part of the χ^2 function (\rightarrow normalized residuals)

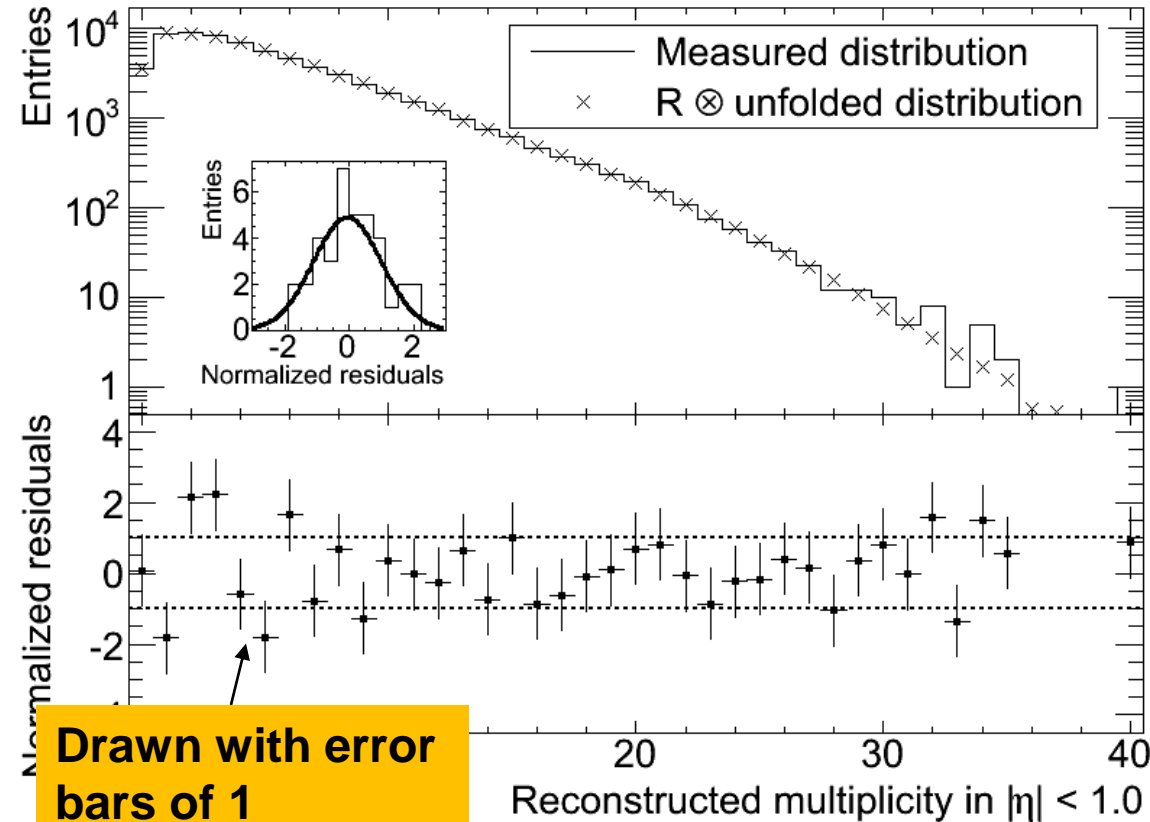
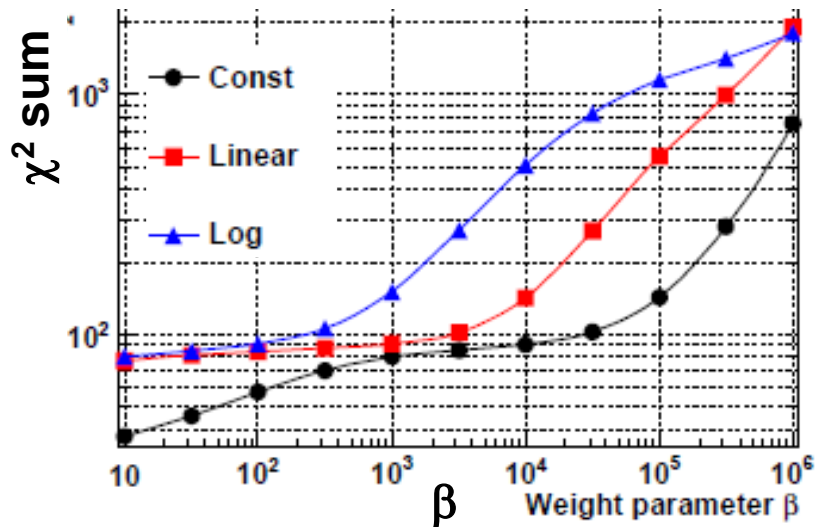
$$\text{Res}_m = \frac{M_m^* - \sum_t R_{mt} T_t^*}{e_m}$$

- Should be a Gaussian with σ of 1

- χ^2/ndf helps to choose β

$$\chi^2 = \sum_m \text{Res}_m^2$$

ndf here about 100



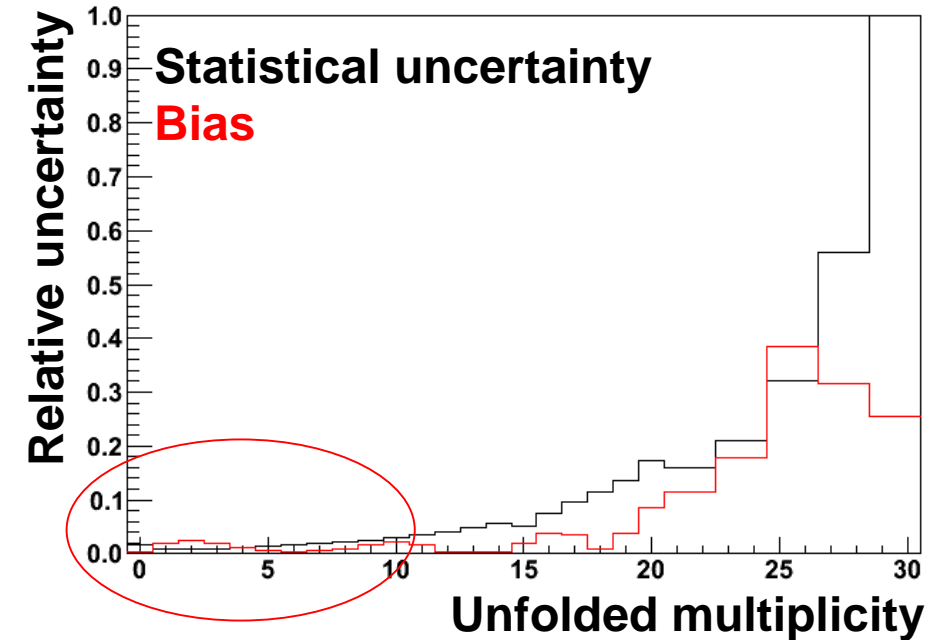
- Once found a good β , check bias

$$b_t = \sum_m \frac{\partial T_t^*}{\partial M_m^*} ((RT^*)_m - M_m^*)$$

- Rule of thumb
 - Bias same or smaller than statistical uncertainty
- NB. Evaluate derivative numerically:

$$\frac{\partial T_t}{\partial M_m} = \frac{1}{6d} \left[8 \left(f\left(\frac{d}{2}\right) - f\left(-\frac{d}{2}\right) \right) - (f(d) - f(-d)) \right]$$

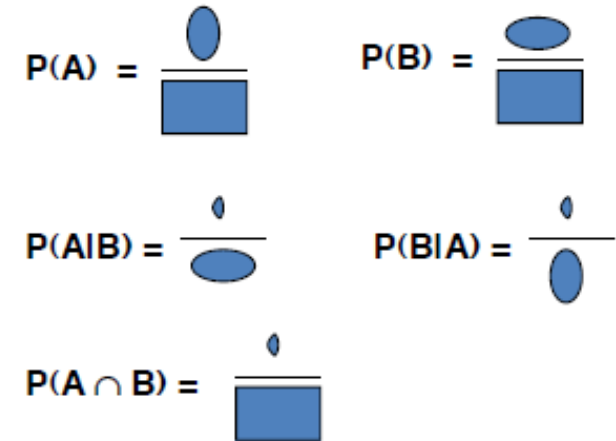
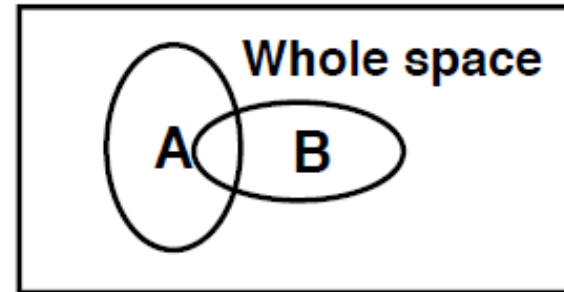
$$f(x) = T_t(M \mid M_m = M_m + x\sqrt{M_m})$$



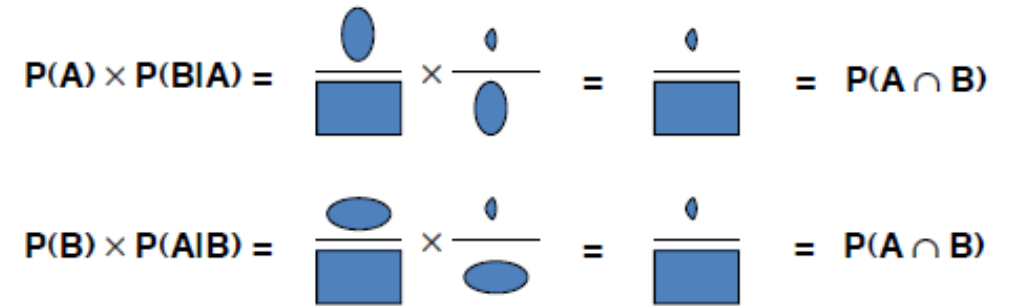
Bayes' Theorem

How to measure

- Bayes' theorem relates
 - the conditional probabilities
 - $P(A|B)$ „A given B“ and
 - $P(B|A)$ „B given A“
 - the marginal probabilities $P(A)$ and $P(B)$
 - of events A and B



$$P(A | B) = \frac{P(B | A)P(A)}{P(B)}$$



$\Rightarrow P(B|A) = P(A|B) \times P(B) / P(A)$

Figure: Bob Cousins

- Rewrite Bayes' theorem for our purposes
 - A = true event (track)
 - B = measured event (track)
- Assume a-priory distribution P, calculate smearing matrix \tilde{R}_{tm}

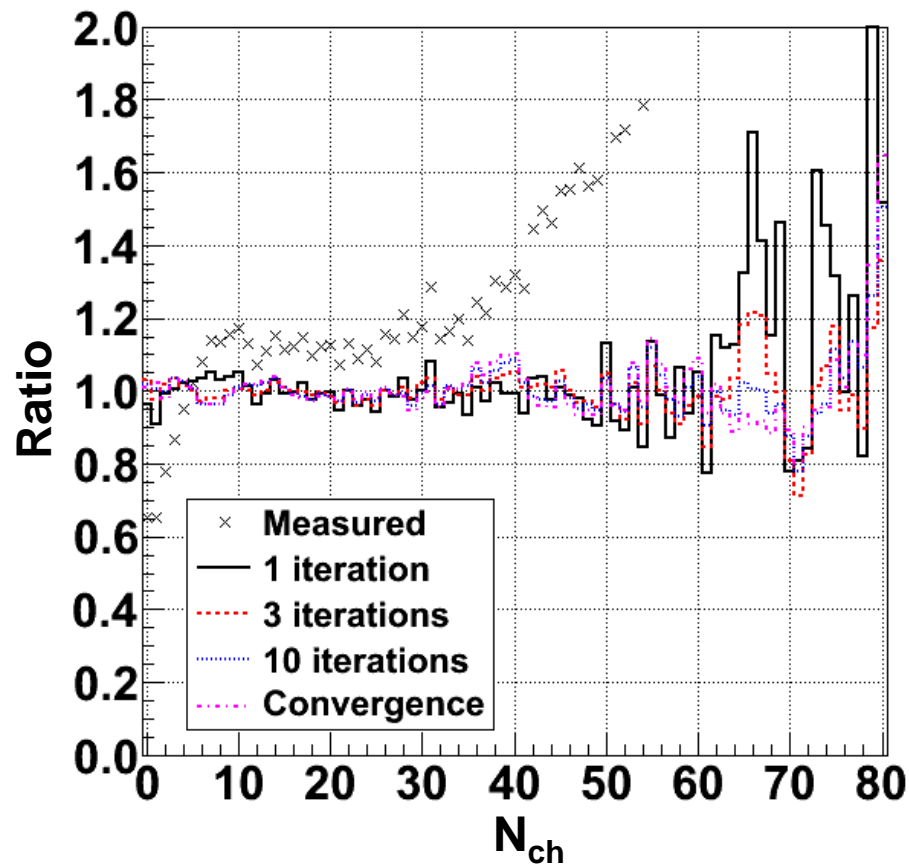
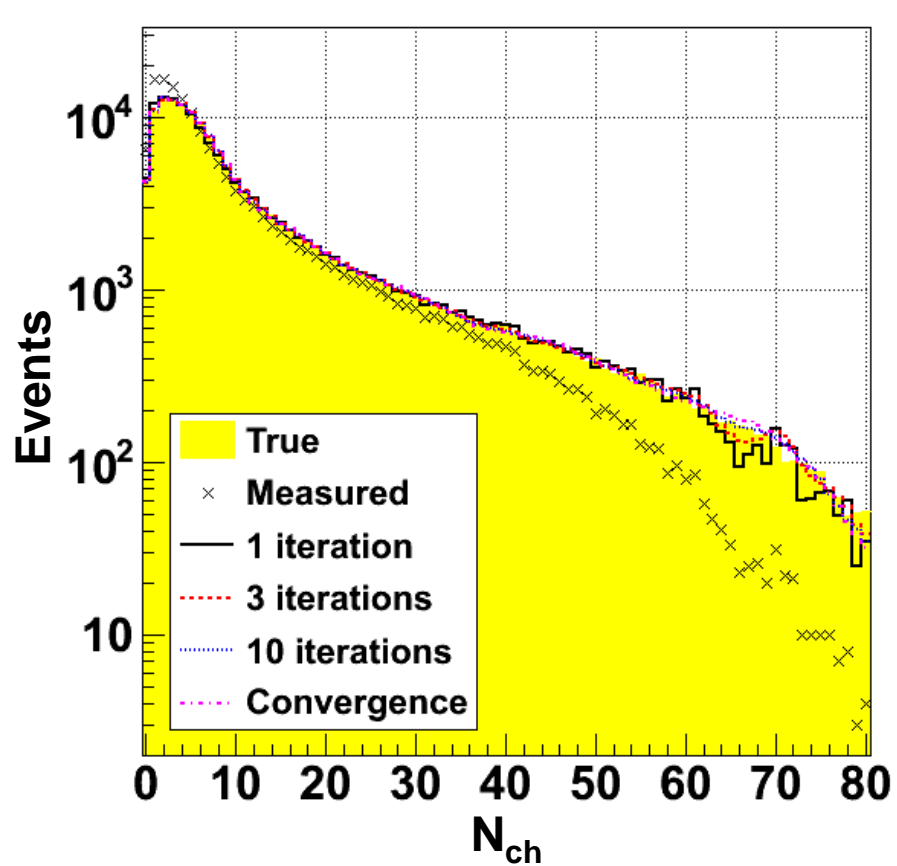
$$\tilde{R}_{tm} = \frac{R_{mt} P_t}{\sum_{t'} R_{mt'} P_{t'}} \quad U_t = \sum_m \tilde{R}_{tm} M_m$$

- Proceed iteratively
 - Choose prior distribution P
 - Calculate \tilde{R}_{tm} and then U_t
 - Optional: apply smoothing
 - Replace P by U, iterate
- Limited number of iterations provides implicit regularization

Optional Smoothing

$$\hat{U}_t = (1 - \alpha) U_t + \frac{\alpha}{3} (U_{t-1} + U_t + U_{t+1})$$

Example of Unfolding using Bayesian Method



already close to input distribution after 1 (!) iteration



Summary

Multiplicity Distributions

- Multiplicity distribution among basic simple observables
- Experimental unfolding procedure challenging
- Multiplicity distribution of events with different number of parton interactions looks very different
- Tail of distribution populated by events with large MPI activity
- But: measurement of multiplicity distribution for specific number of parton interactions not feasible (to date...)

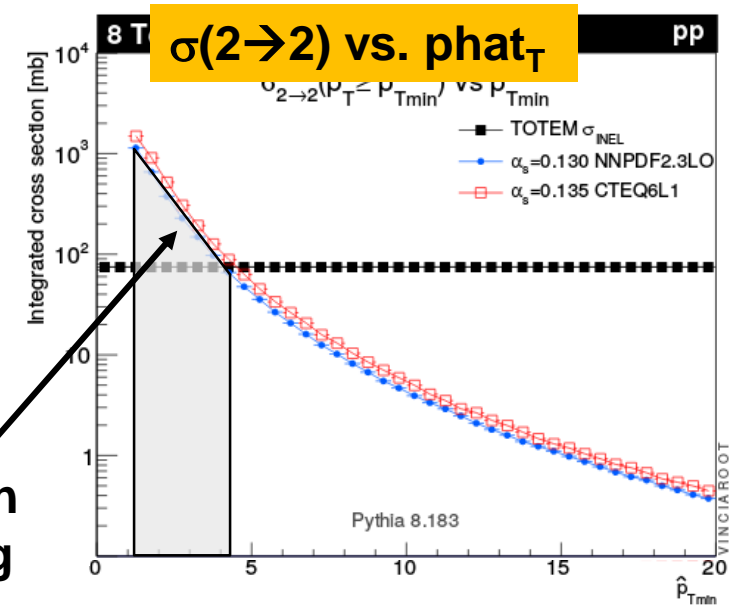
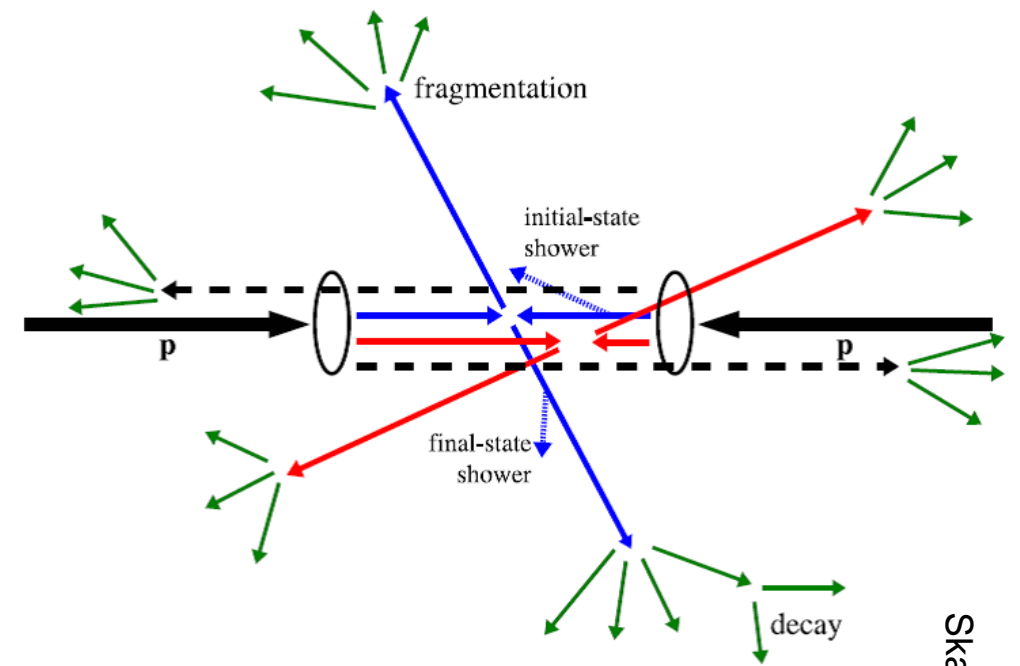


Underlying Event



Underlying Event

- What is the underlying event (UE)?
 - *Anything* below the hardest scattering
- Due to steeply falling cross-section
 - Most events have soft component
 - If there is a hard parton scattering, there are additional soft parton interactions

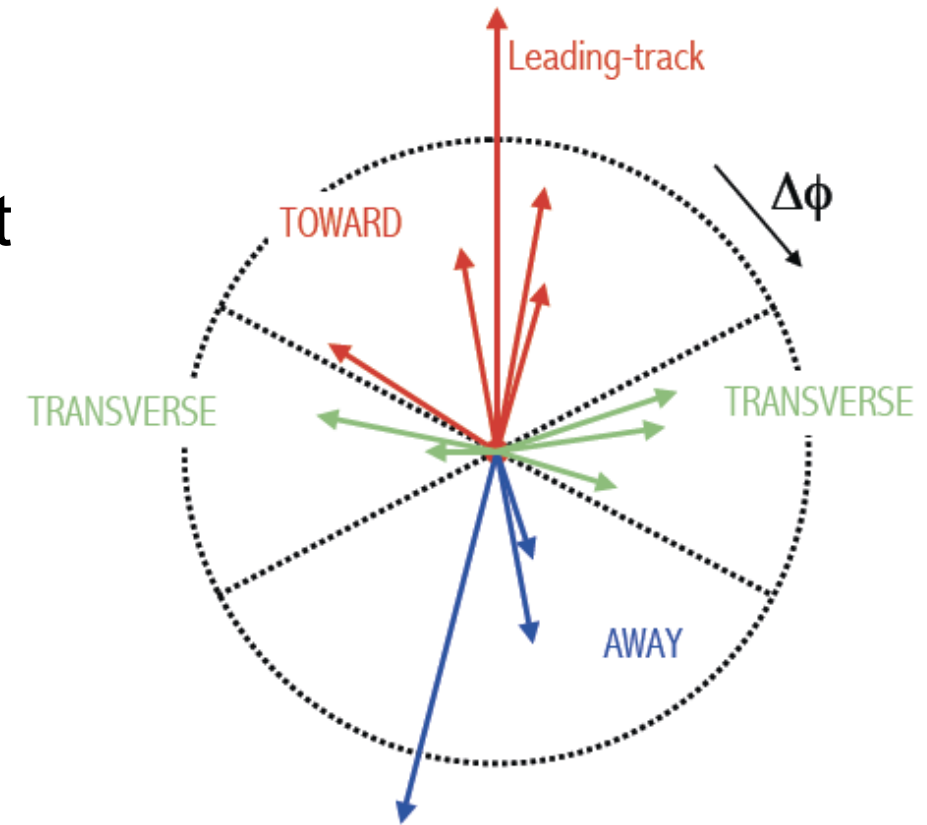


Most events have (more than one) “soft” parton scattering

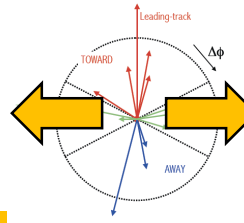
Skands, Carrazza, Rojo, arXiv:1404.5630

Underlying Event (2)

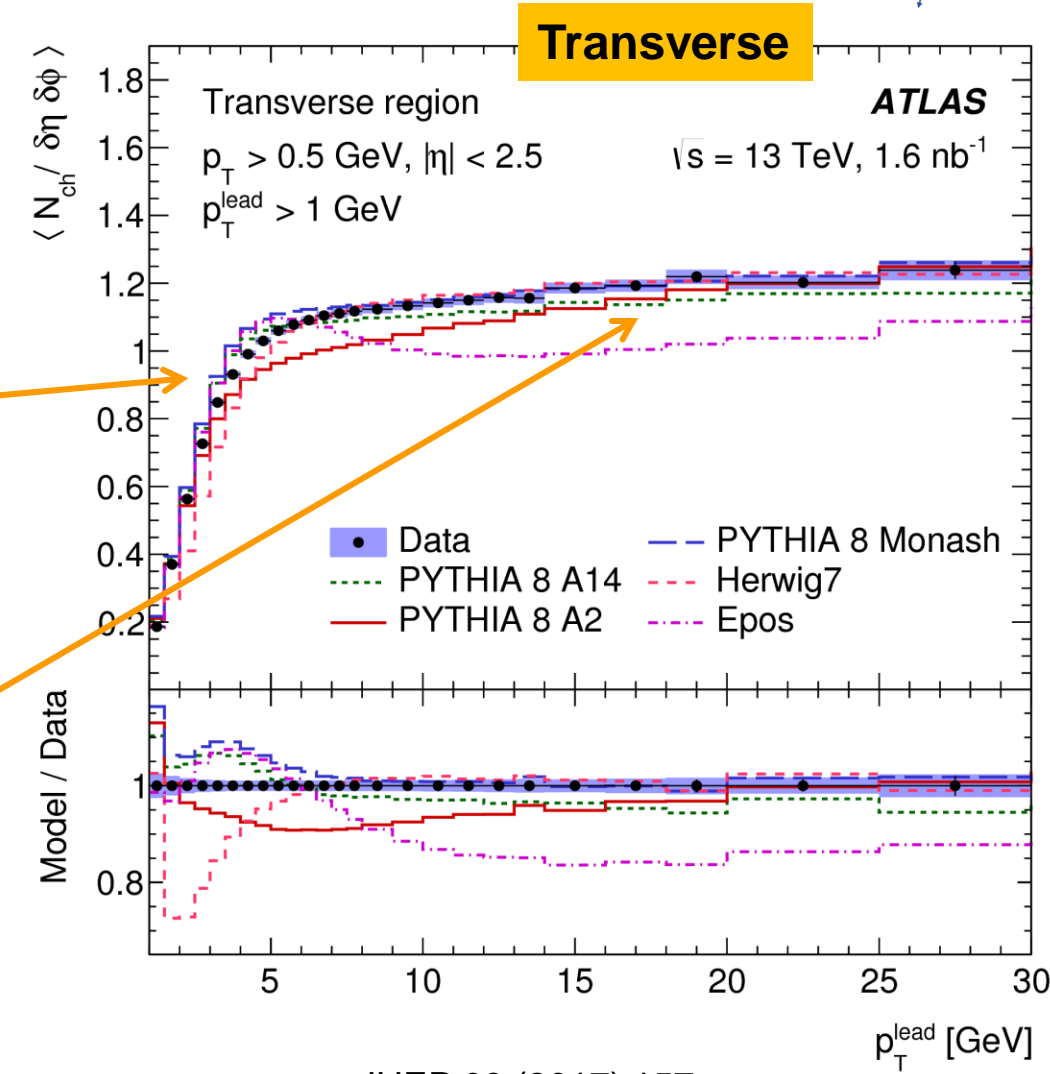
- Find hardest object
 - Charged track, jet, Z, ...
- Study distinct azimuthal regions wrt object
 - Transverse ($1/3\pi < |\Delta\phi| < 2/3\pi$) = UE
 - May be split into MIN and MAX region
 - Towards ($|\Delta\phi| < 1/3\pi$)
 - Back-to-back ($|\Delta\phi| > 2/3\pi$)
- Typical observables
 - Number density, Σp_T , σp_T



Number Density (transverse)



- Activity perpendicular to hard object
- Strong rise at low $p_{T,lead}$
 - Impact parameter dependence → MPI
 - “Trivial” selection bias
- Mild positive slope at large $p_{T,lead}$
 - Initial- and final-state radiation

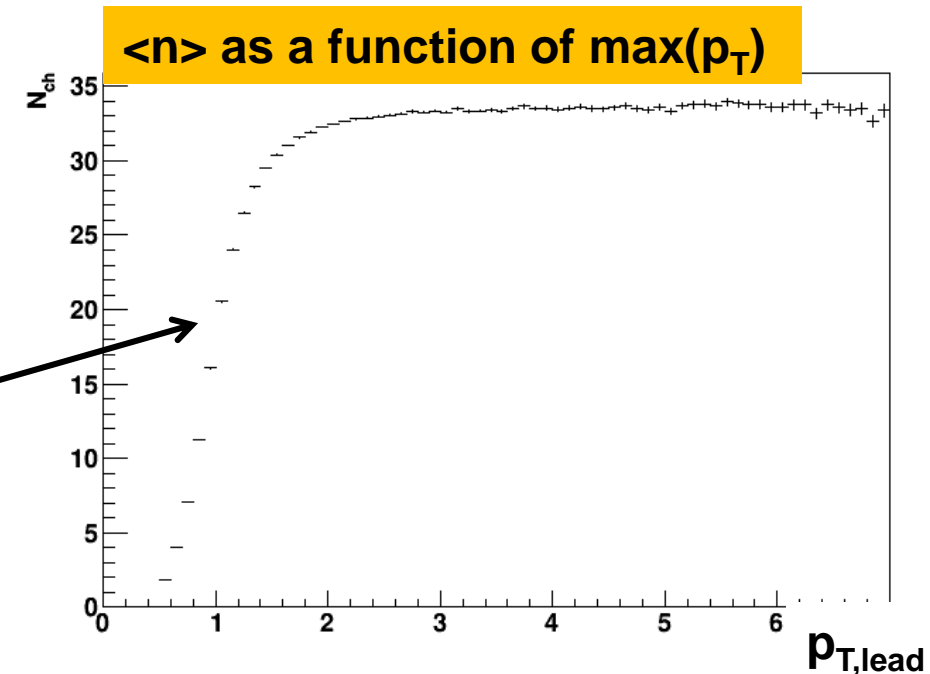
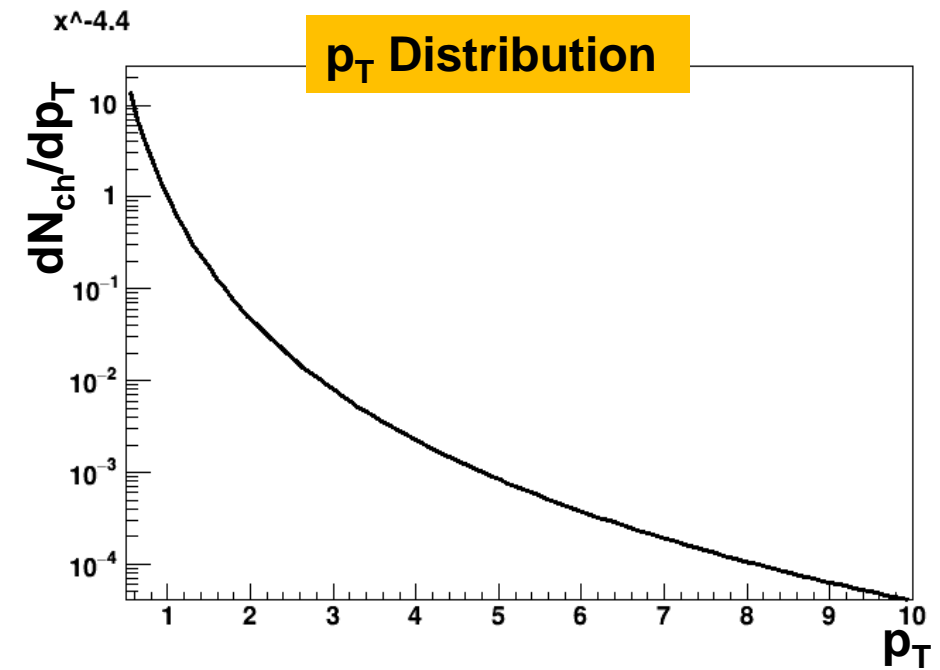


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Selection Bias

- Trivial bias in distribution
 - The more particles drawn, the higher max p_T
- Can be shown with simple toy (~20 lines ROOT, see [backup](#))
 - p_T distribution: $dN/dp_T \sim p_T^{-4.4}$
 - Draw n particles from this distribution
 - Determine $\max(p_T)$
 - Calculate $\langle n \rangle(\max(p_T))$

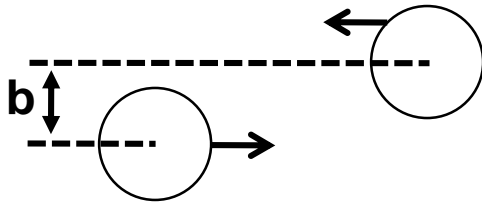


Steep increase as in observed underlying event distribution

 **Onset and level of plateau depends on N_{ch} distribution**

Impact Parameter Dependence

- Chance for parton interactions depends on pp impact parameter



- Reminder: in pp collisions b is not directly accessible (contrary to AA collisions)

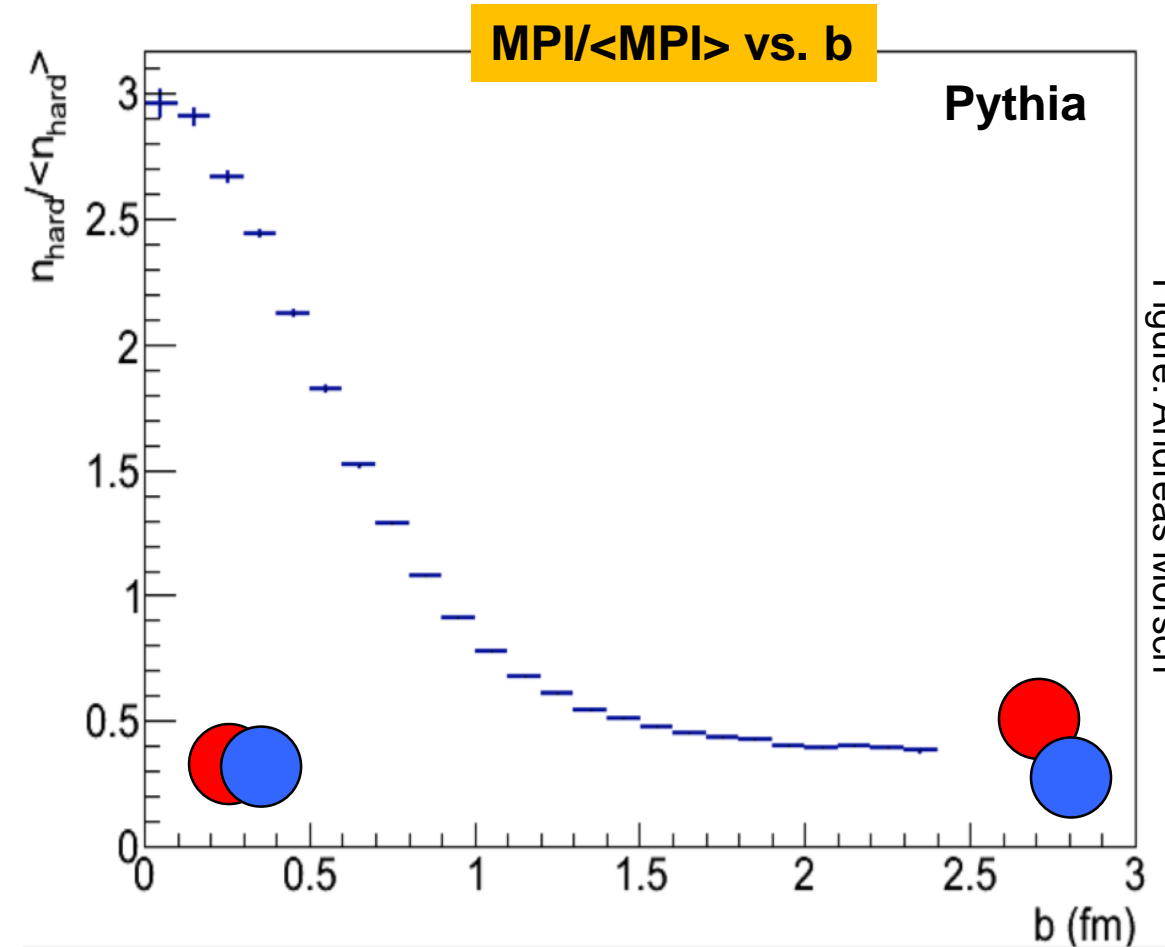
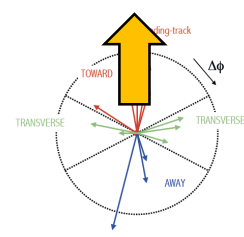
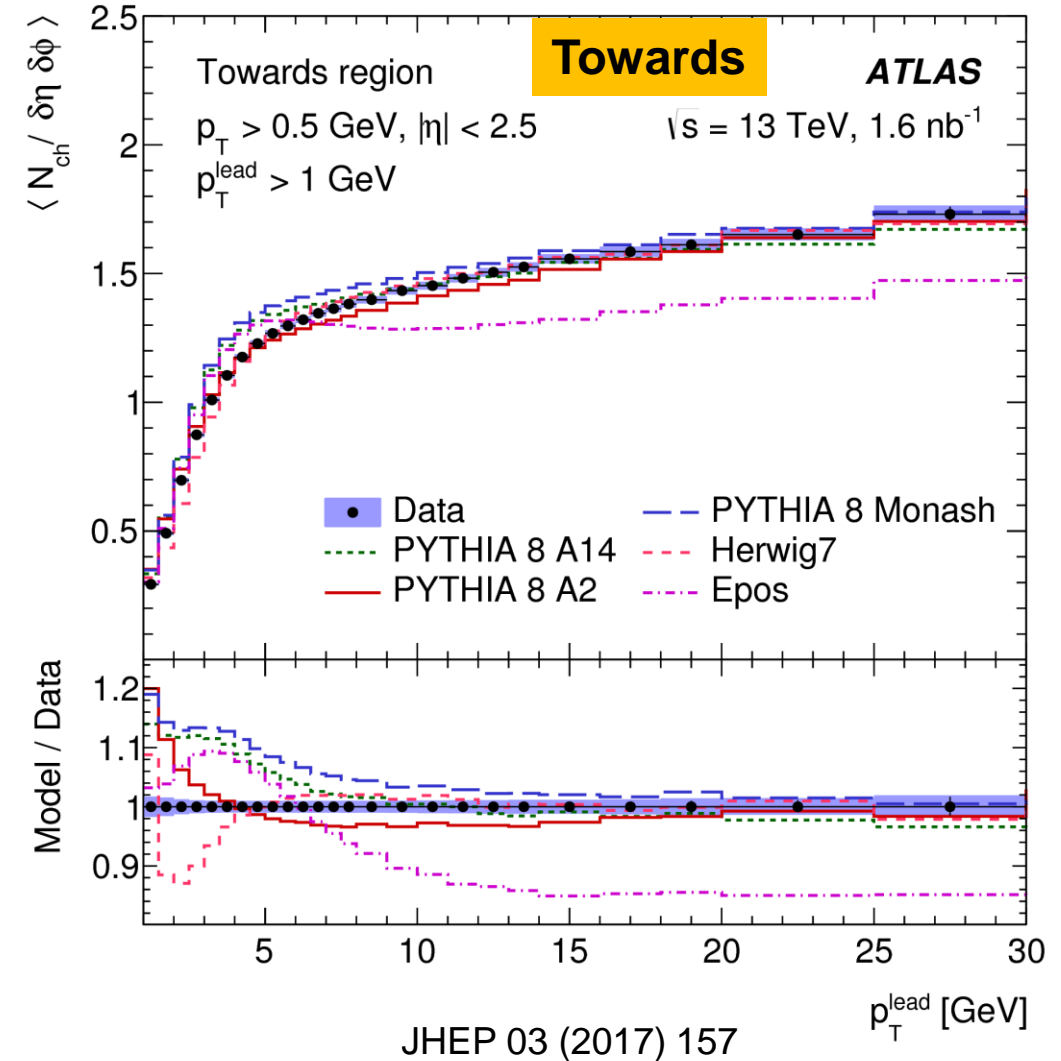


Figure: Andreas Morsch

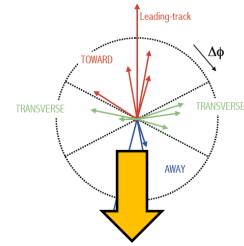
Number Density (towards)



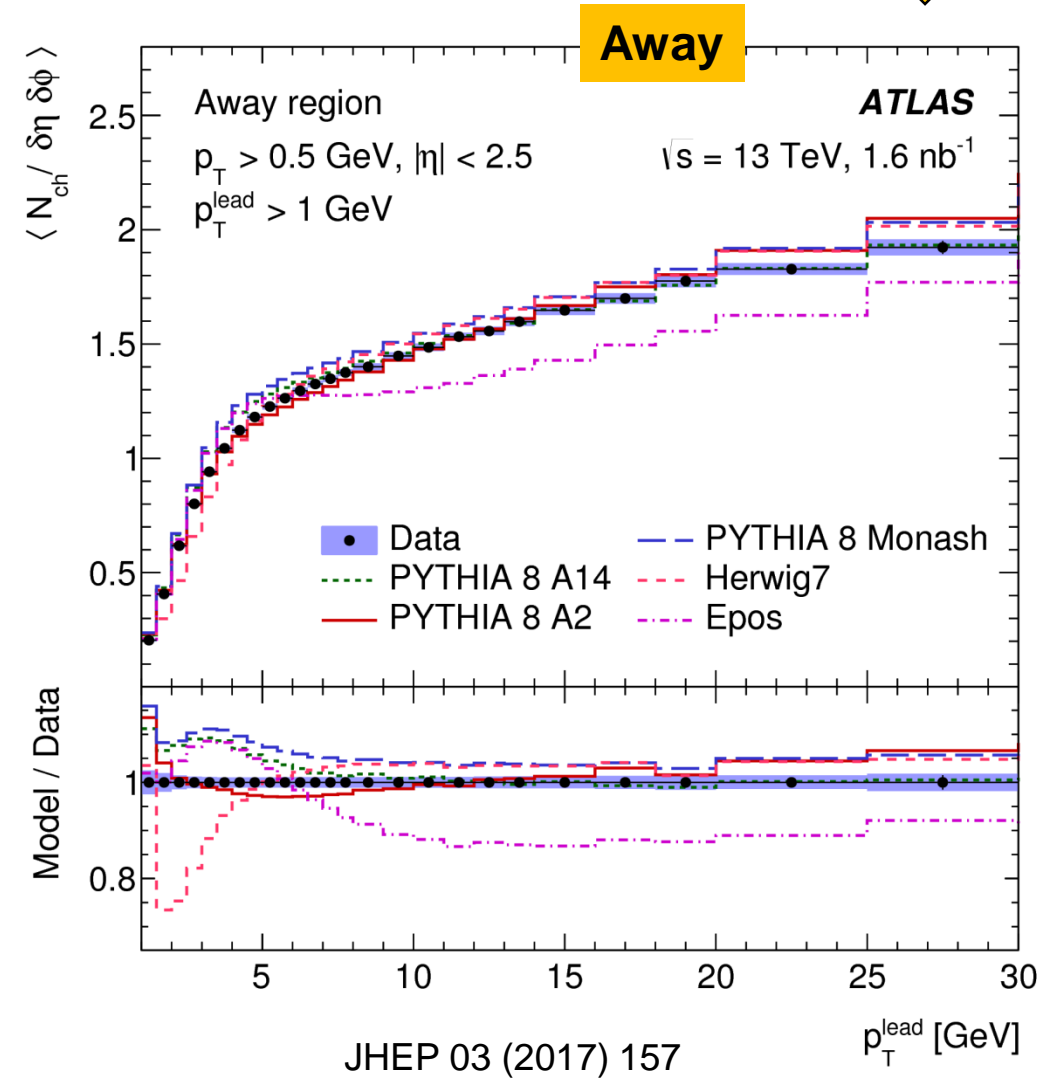
- Activity in direction of leading object
- Overall similar picture
 - Steep increase, then mild increase
- Larger slope at large $p_{T,lead}$ than in the transverse region
- Harder jets fragment into
 - more particles
 - leading object with higher p_T



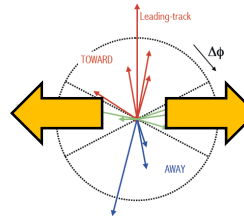
Number Density (away)



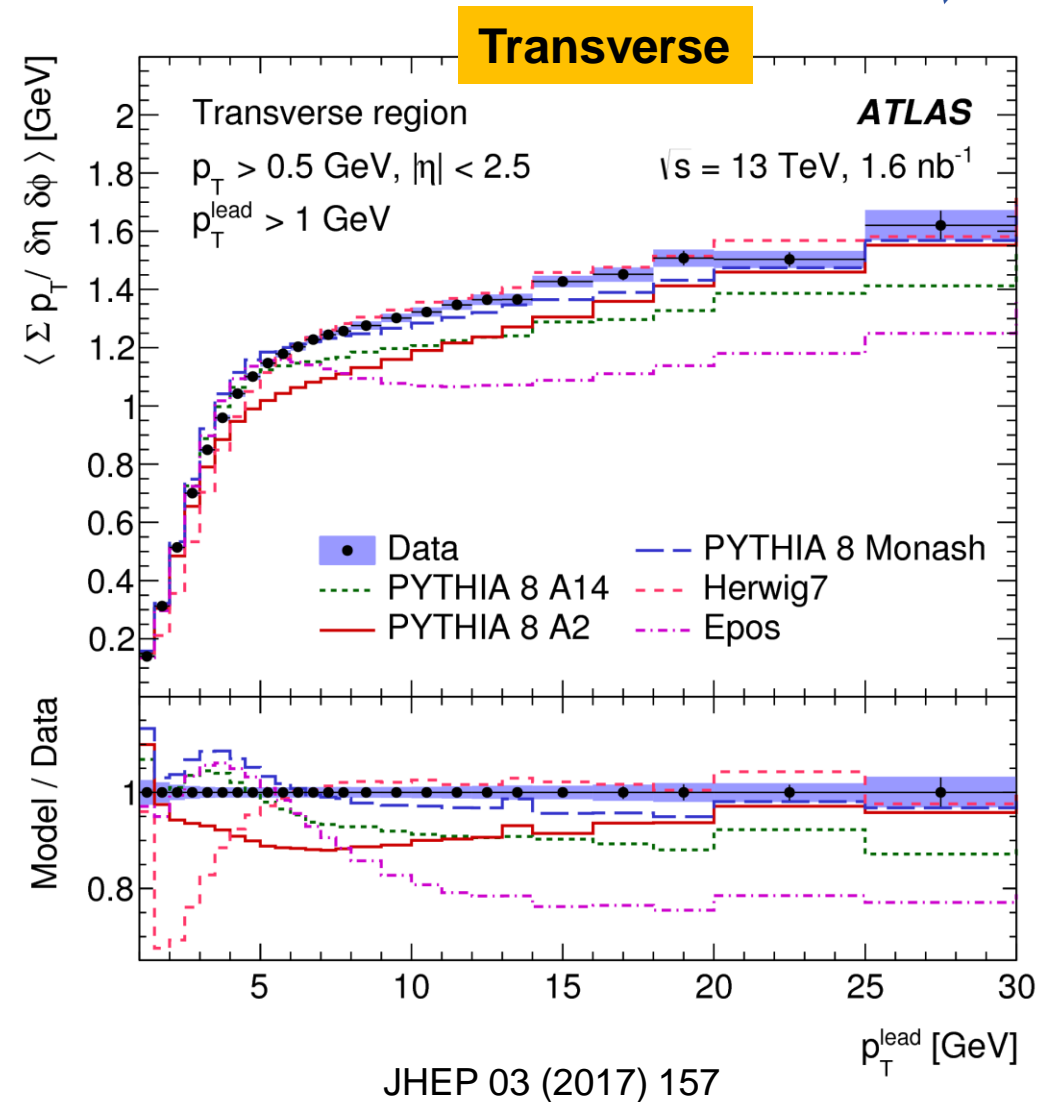
- Activity back-to-back of leading object
- Overall similar picture
 - Steep increase, then mild increase
- Similar slope at large $p_{T,lead}$ than in the towards region
- Conclusions as for towards region
 - Balancing jet has similar p_T



Σp_T (transverse)



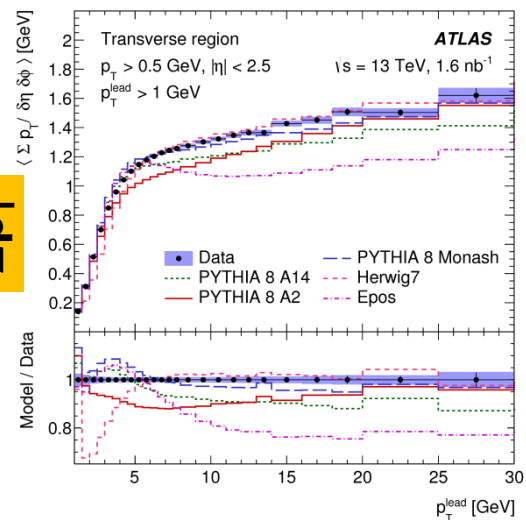
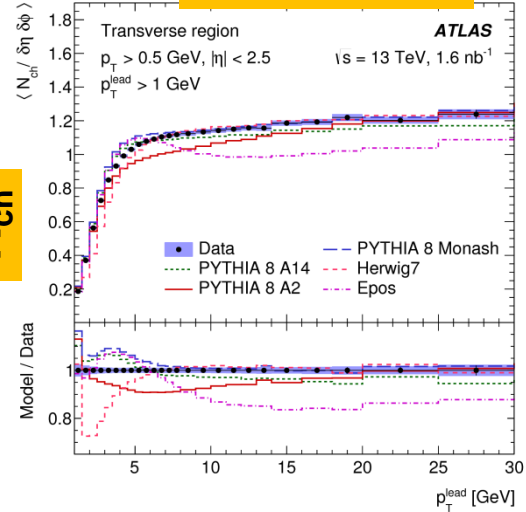
- Instead of counting the particles, measure their Σp_T
- Generally similar trends
 - Watch details in comparison to N_{ch} !



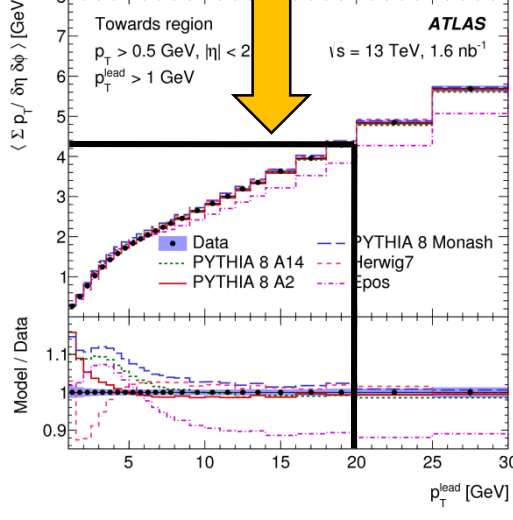
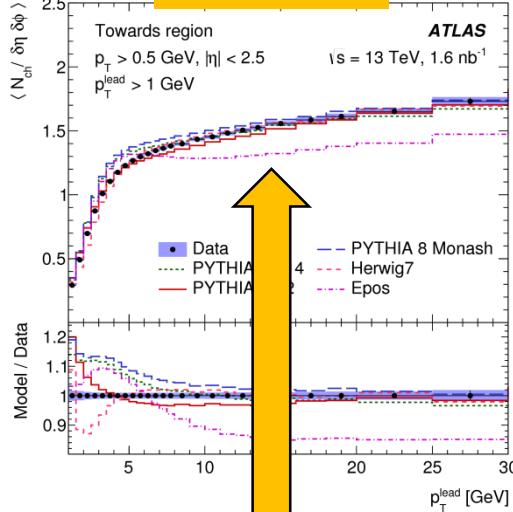


N_{ch} vs. Σp_T

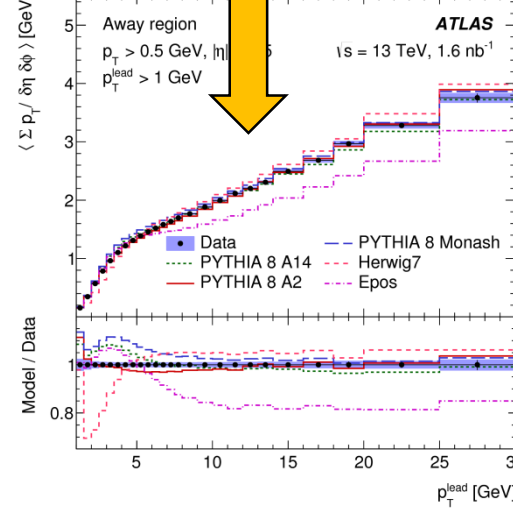
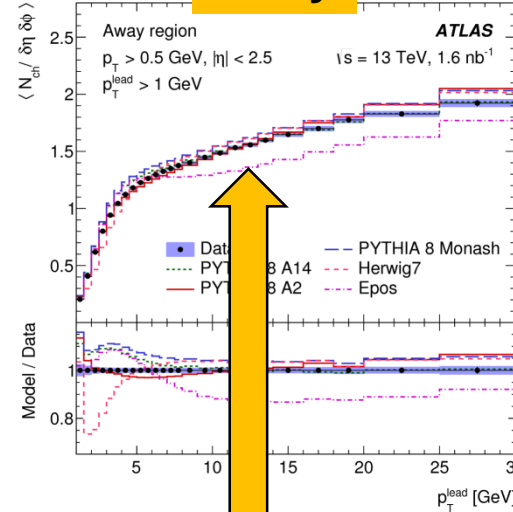
Transverse



Towards



Away



- N_{ch} and Σp_T similar for transverse region
- Differences in towards and away region
 - Σp_T closer correlated to leading p_T
 - Harder jets carry more momentum

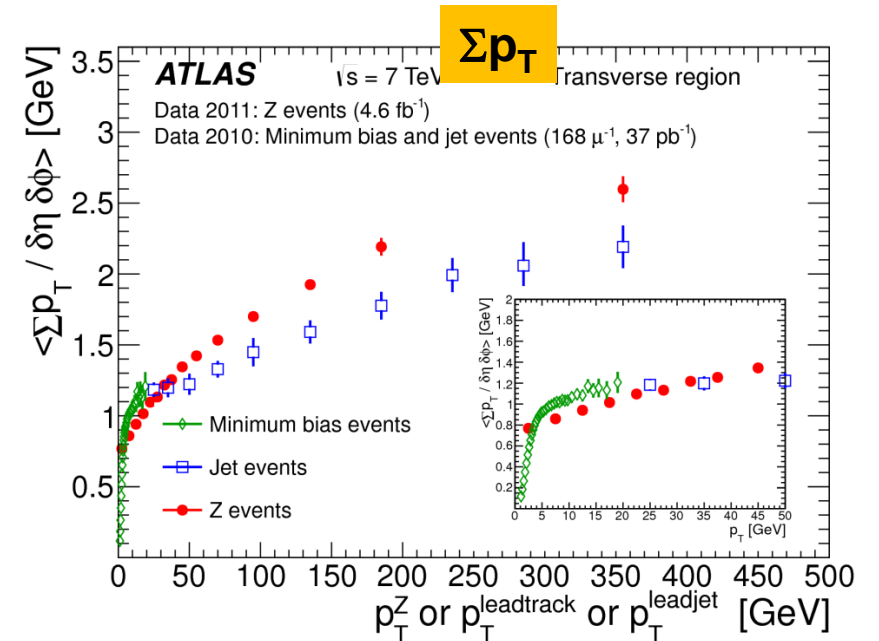
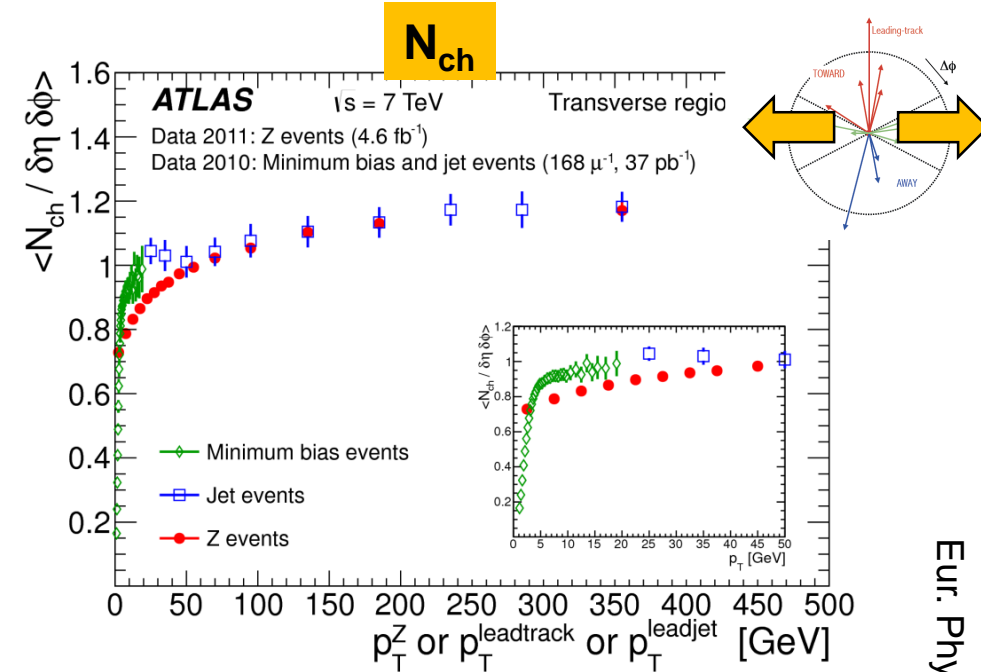
 **Leading object constitutes large fraction of Σp_T (only in towards region)**

- For these plots, phase space factor $\delta\eta\delta\phi = 2/3\pi * 2.5 \sim 5.2$
 $\rightarrow 20 \text{ GeV}/c \rightarrow \Sigma p_T = 3.82$



UE vs. jets and Z

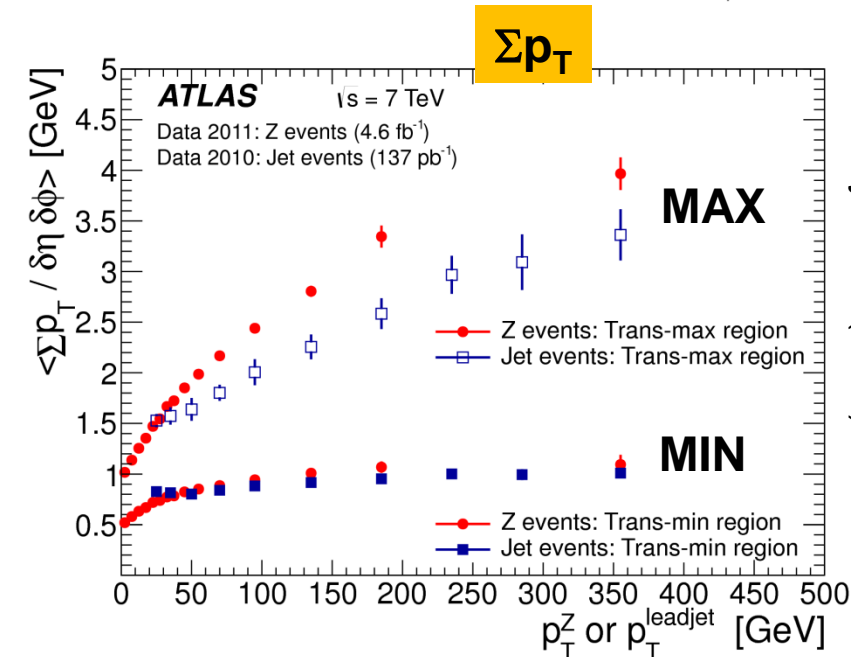
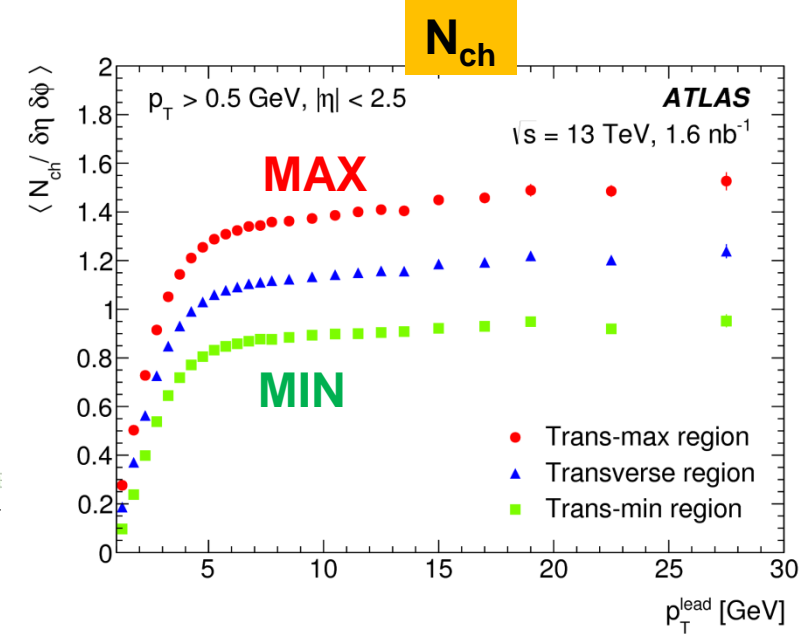
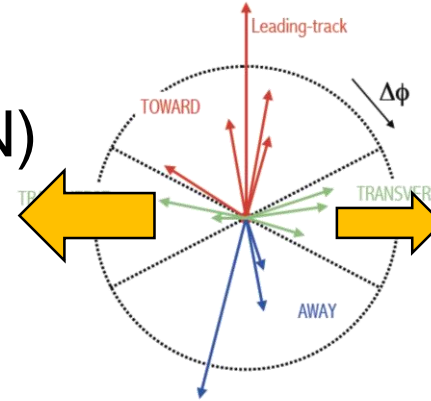
- Leading track and leading jet measurements show similar dynamics
- Leading Z boson p_T different
 - Different turn on in N_{ch}
 - Larger activity in Σp_T



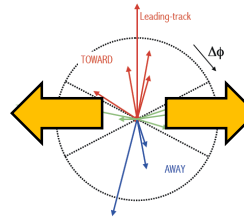
Transverse Min and Max

- Split transverse region
 - more (MAX) and less activity (MIN)
 - measured by Σp_T
 - About 20% effect

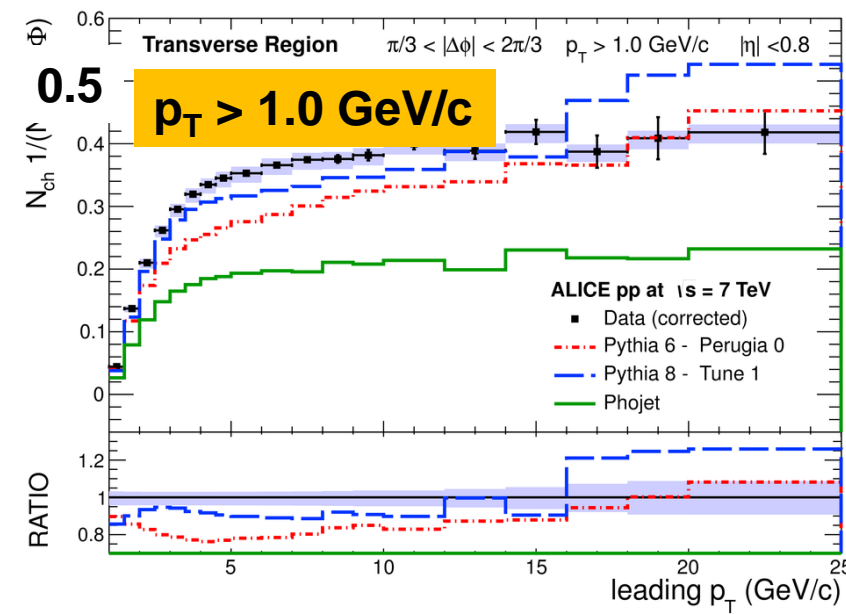
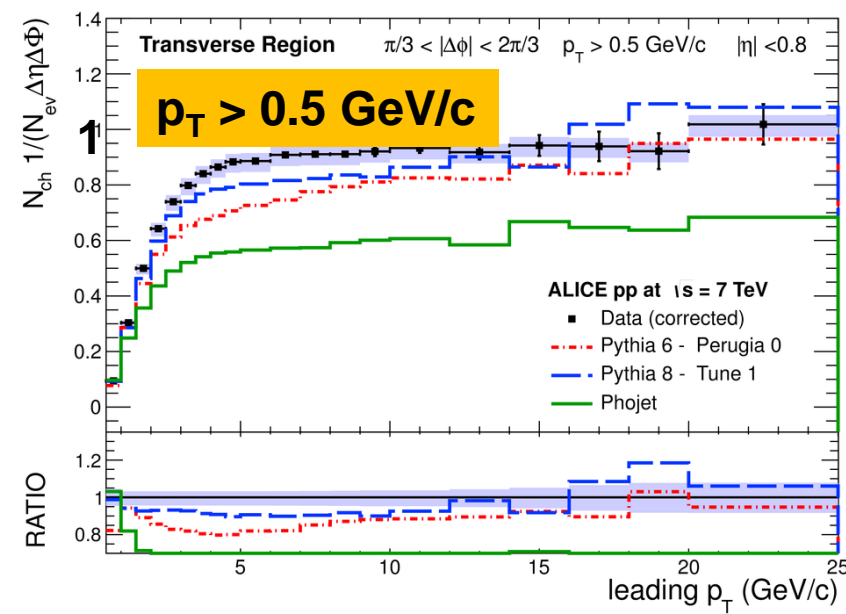
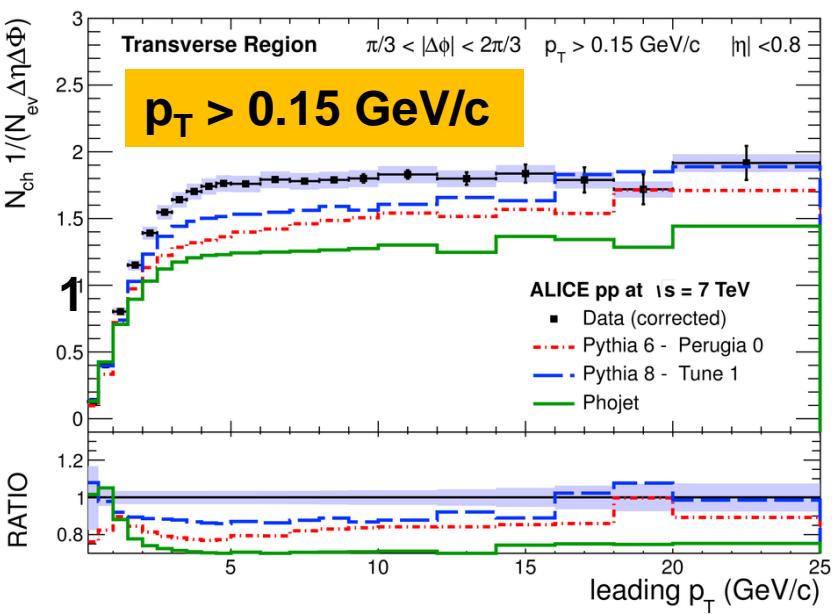
- Differences between Z and jet result vanishes in transverse MIN
 - Most sensitive to other parton interactions independent of the hard object



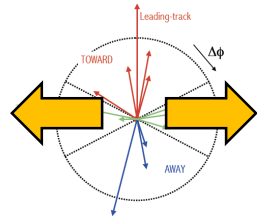
Dependence on p_T cut



- Results with three different low p_T thresholds
- More than 75% of the particles within $0.15 < p_T < 1$ GeV/c
- Particularly important for MC tuning



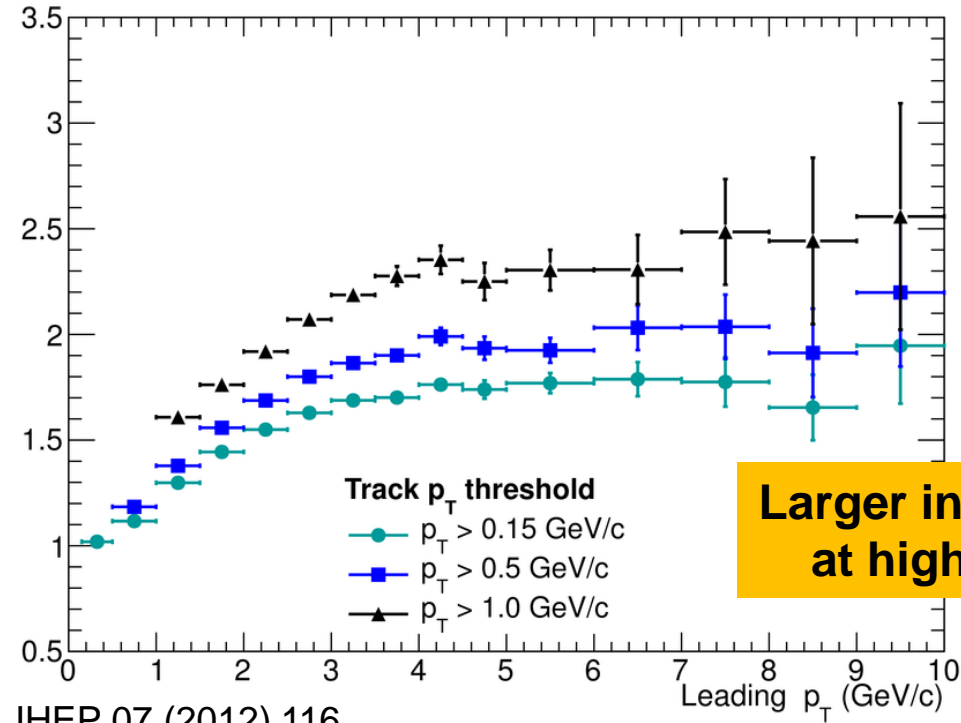
\sqrt{s} Dependence



- Significant increase with \sqrt{s}
 - As overall multiplicity

Number density ratio between 7 and 0.9 TeV in Transverse region

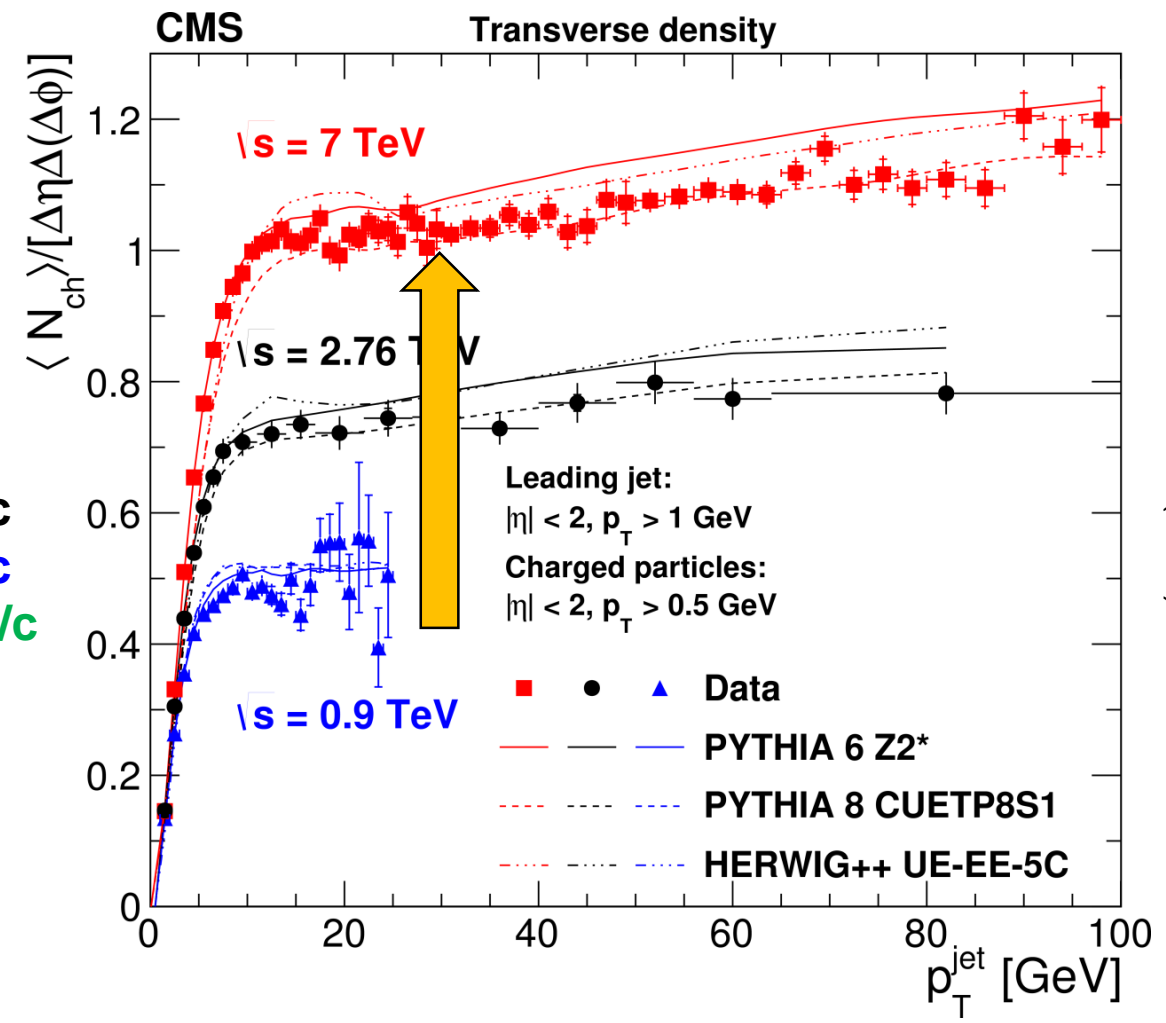
Ratio 7 TeV / 0.9 TeV



Larger increase at higher p_T

$p_T > 1.0$ GeV/c
 $p_T > 0.5$ GeV/c
 $p_T > 0.15$ GeV/c

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Relation of N_{ch} and UE

- Compare
 - Overall average multiplicity (of MB collisions)
 - Plateau in transverse region (the UE contribution)
- Steeper slope in UE than MB
- With increasing \sqrt{s} , UE grows faster than average
- Sensitive to interplay of hard process, ISR, FSR and MPI

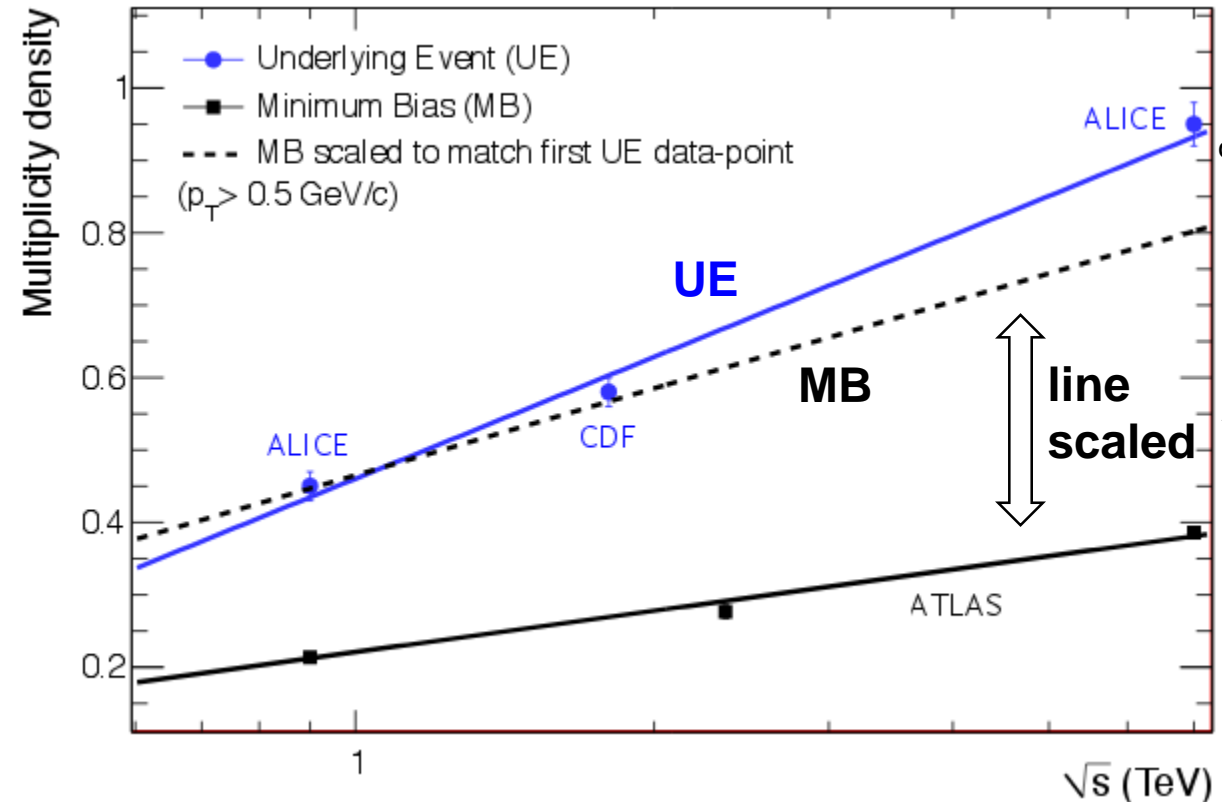
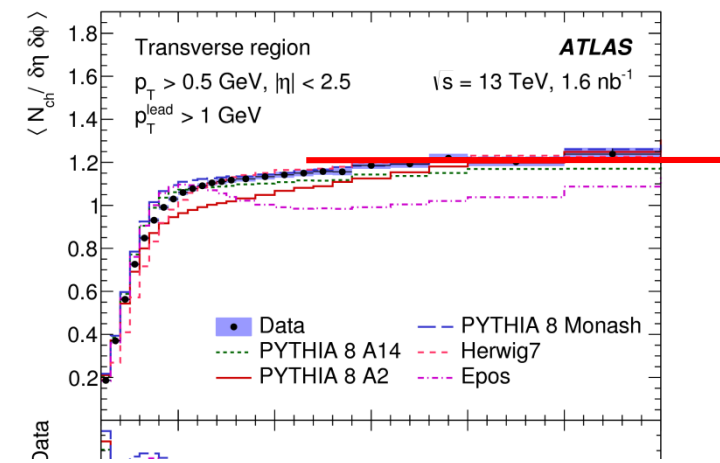
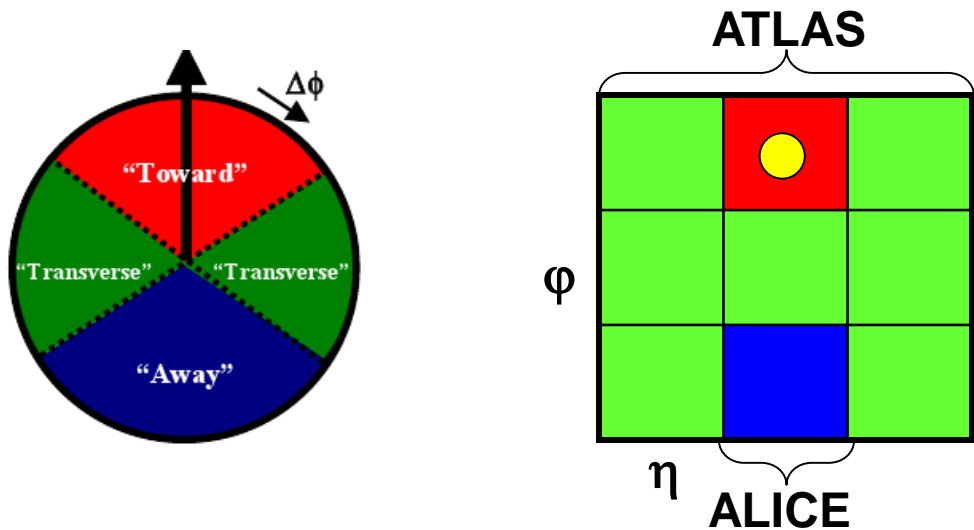


Figure: PhD thesis, Sara Vallero

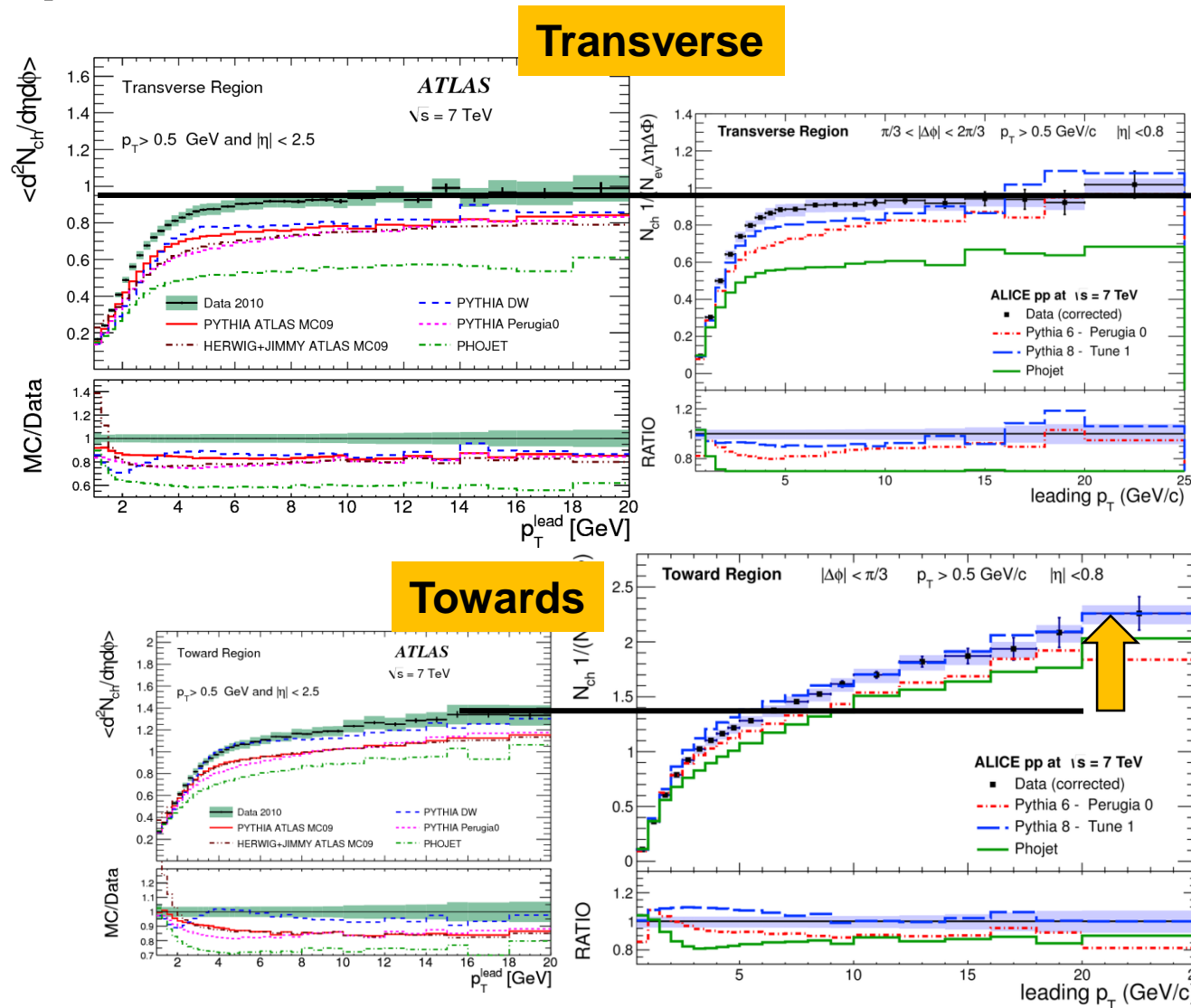
Influence of Acceptance

Acceptance ranges important!



- ATLAS ($|\eta| < 2.5$) vs. ALICE ($|\eta| < 0.8$)
 - Transverse region similar
 - Large difference in towards
- Due to size of jet around leading particle



- Can be checked numerically
 $(1 \times \text{ALICE towards} + 2 \times \text{ALICE transverse}) / 3 = \text{ATLAS towards}$



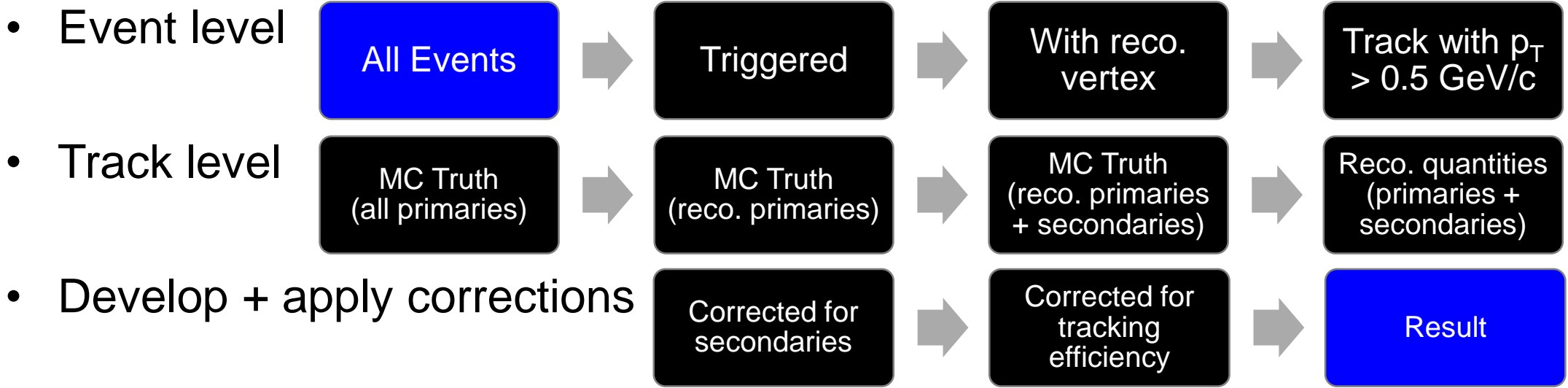
Corrections

- Published underlying event distributions \neq raw measurement
- Let's use this example to understand
 - which detector effects are relevant
 - how to correct for them
- You need two things: 1) brain  2) MC 
- Procedure
 - Make a list of effects which could affect your measurement (involves: previous analysis, discussion with colleagues, papers, ...)
 - Test these on MC



Finding a Correction Procedure

- Testing with MC
 - Construct your observable at many different steps



- Develop + apply corrections
- Compare the distributions at the different levels
 - Reveals effects.
Maybe some negligible → no correction needed
 - MC *Closure*: Do the two blue boxes agree?

Use the same sample to produce corrections and plots → closure should be exact. Very powerful to find issues and bugs!

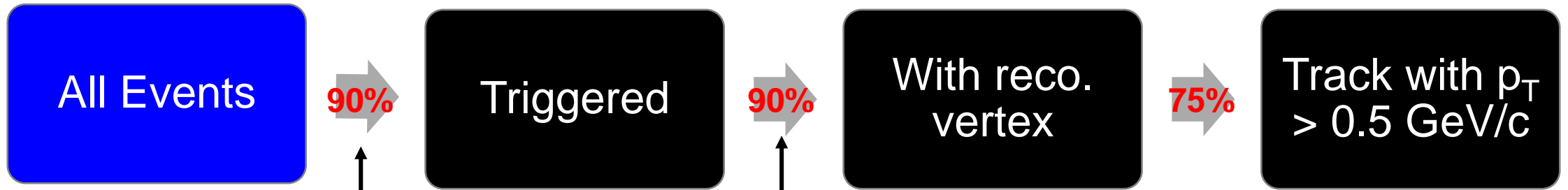


Strength of Detector Effects

How to measure

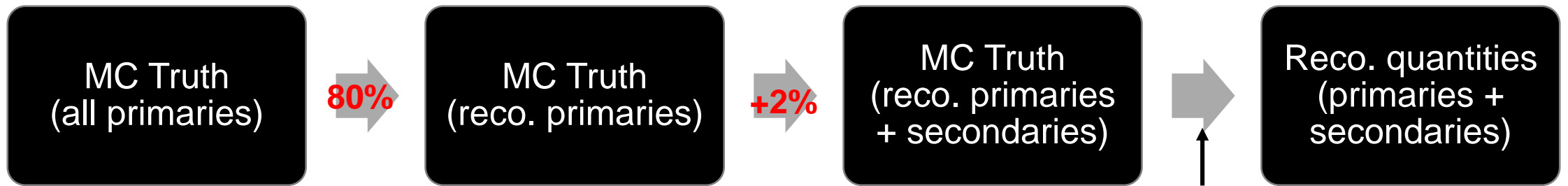
- Example for ALICE, pp, 7 TeV (PhD thesis, Sara Vallero)

- Event level



BUT effect on observable minimal!

- Track level

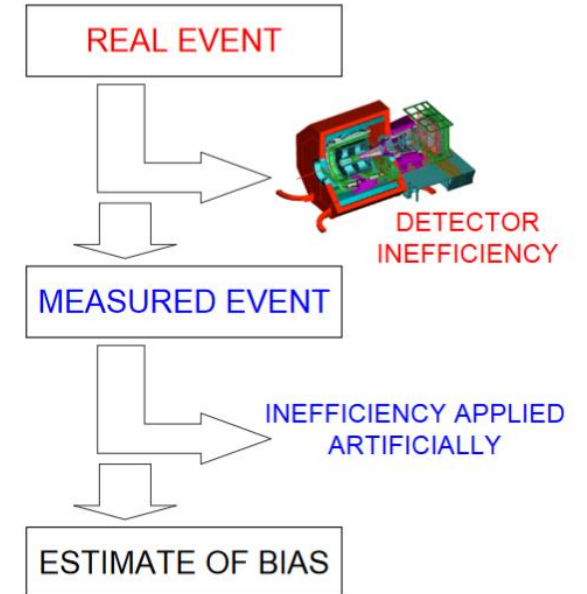
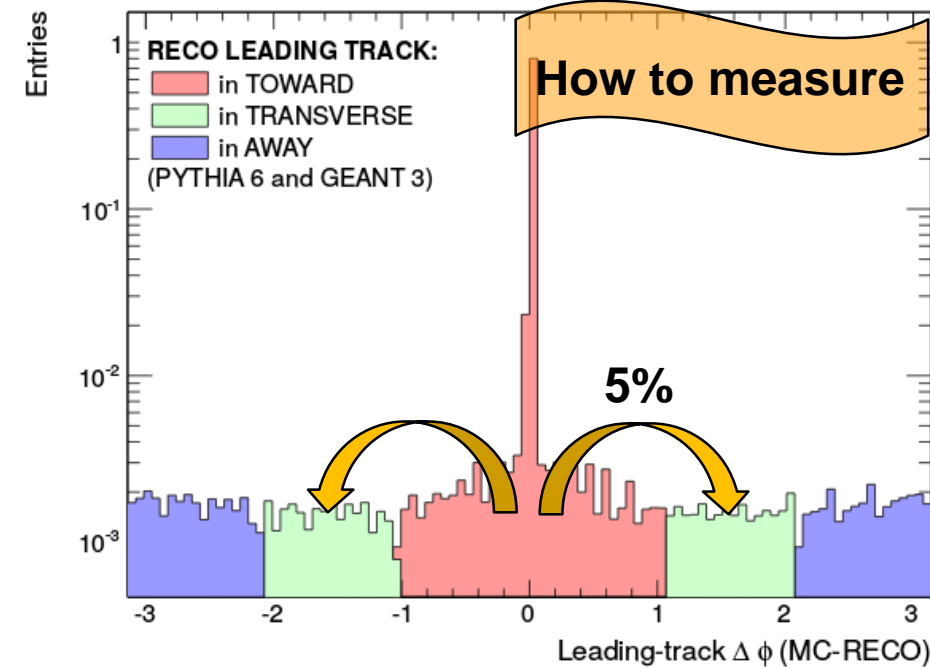


only resolution

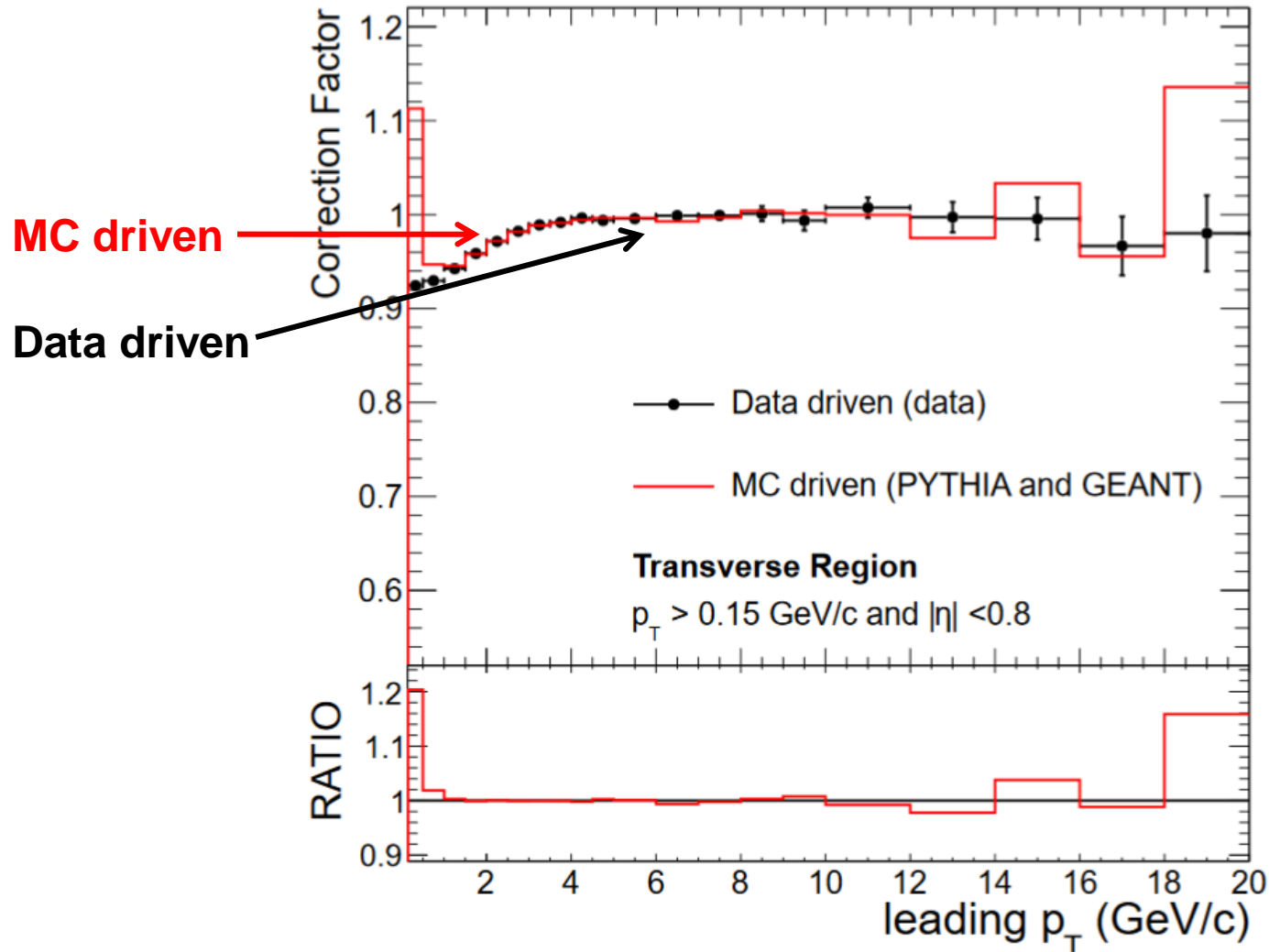


Further Corrections

- Underlying-event specific effects
 - Not reconstructed leading track, leads to re-orientation of towards, transverse, and away region
 - E.g. about 5% migration about towards \rightarrow transverse
- Correction
 - Based on MC (implies MC dependence)
 - Data-driven approach
 - Apply tracking efficiency 2nd time to the leading track
 - If reconstructed, fill normally
 - If not, use sub leading track to orientate event



Re-orientation Correction



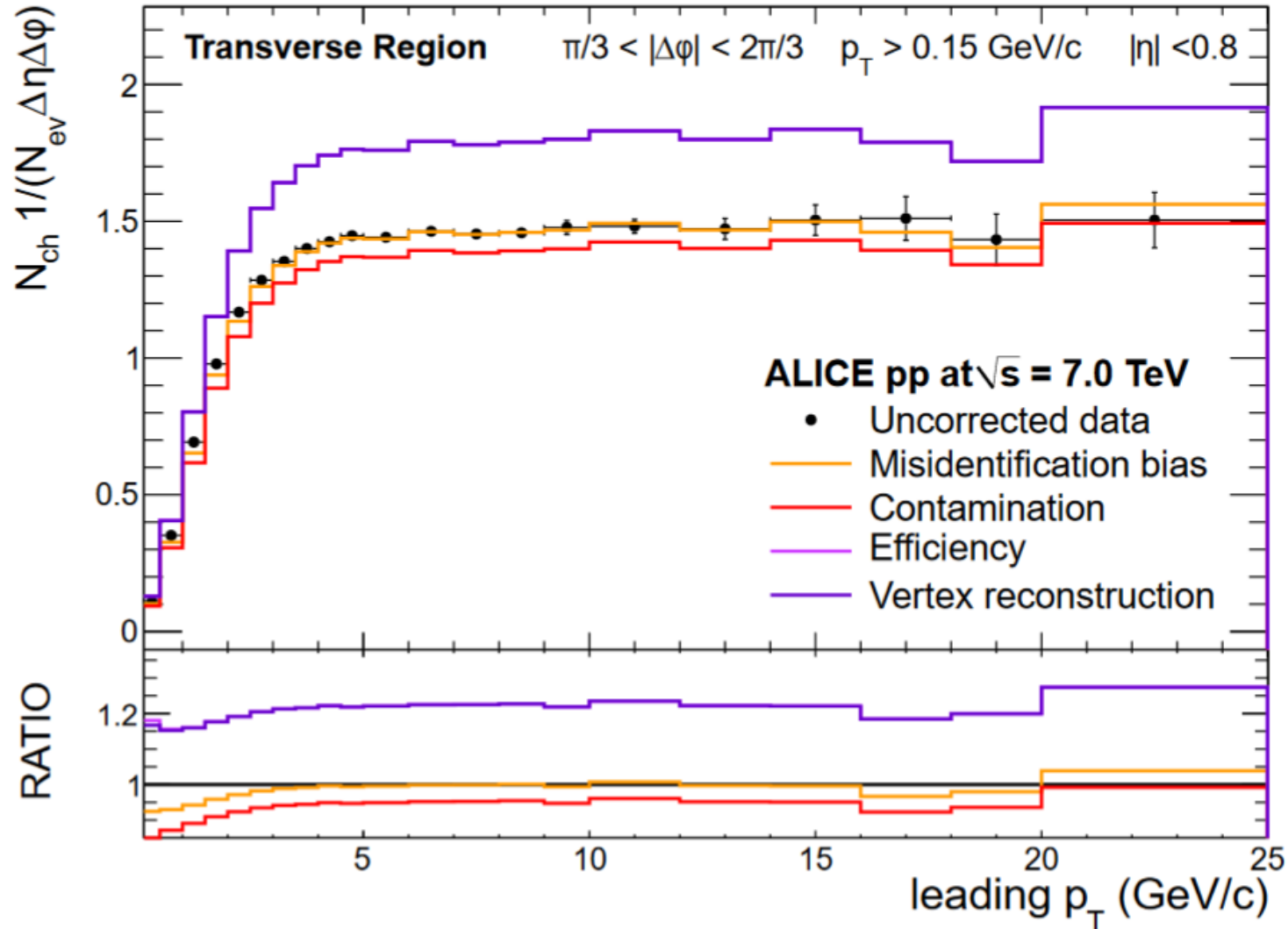
Good agreement except at low p_T (due to “event loss” when efficiency is applied 2nd time)

→ difference considered for the systematic uncertainties



Overview: Corrections on Data

How to measure



Tracking efficiency
Event re-orientation
Contamination

Tracking efficiency
Event re-orientation
Contamination



Summary

Underlying Event

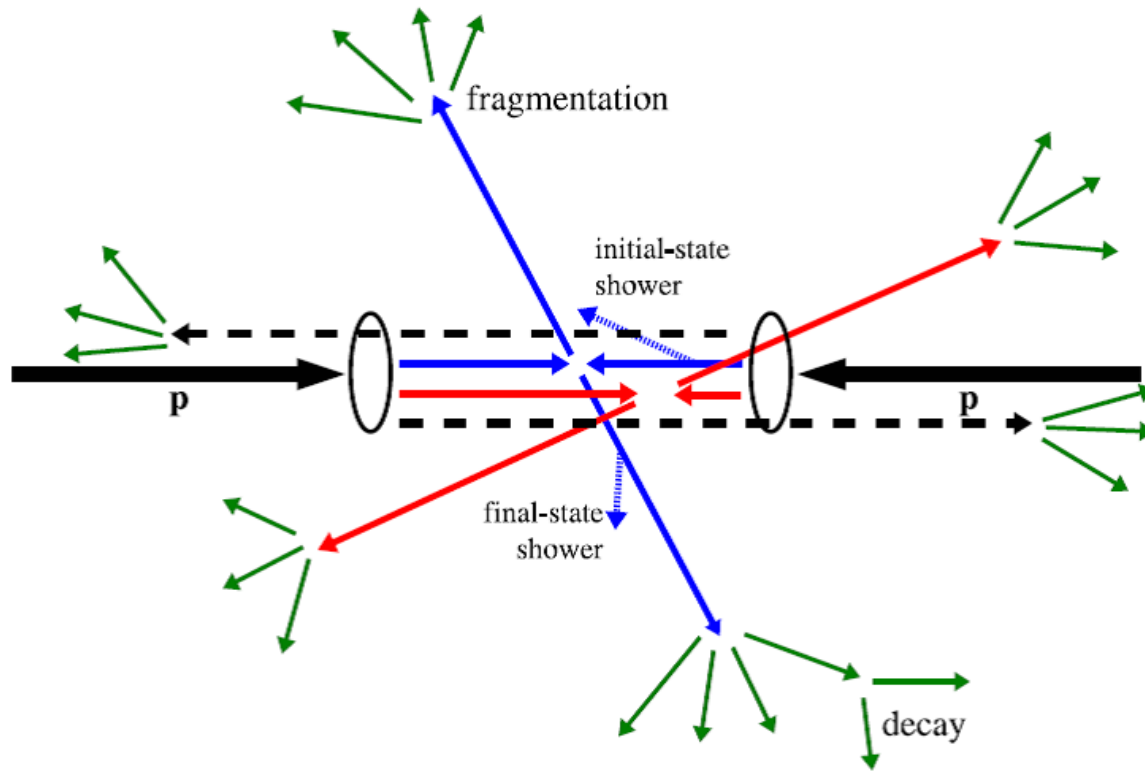
- Underlying event observables characterize activity relative to the hardest scattering
- Important tool for MC tuning and modelling
- Transverse region studies activity from additional parton interactions
 - With increasing \sqrt{s} , underlying event grows faster than average multiplicity



Uncorrelated Seeds

Uncorrelated Seeds

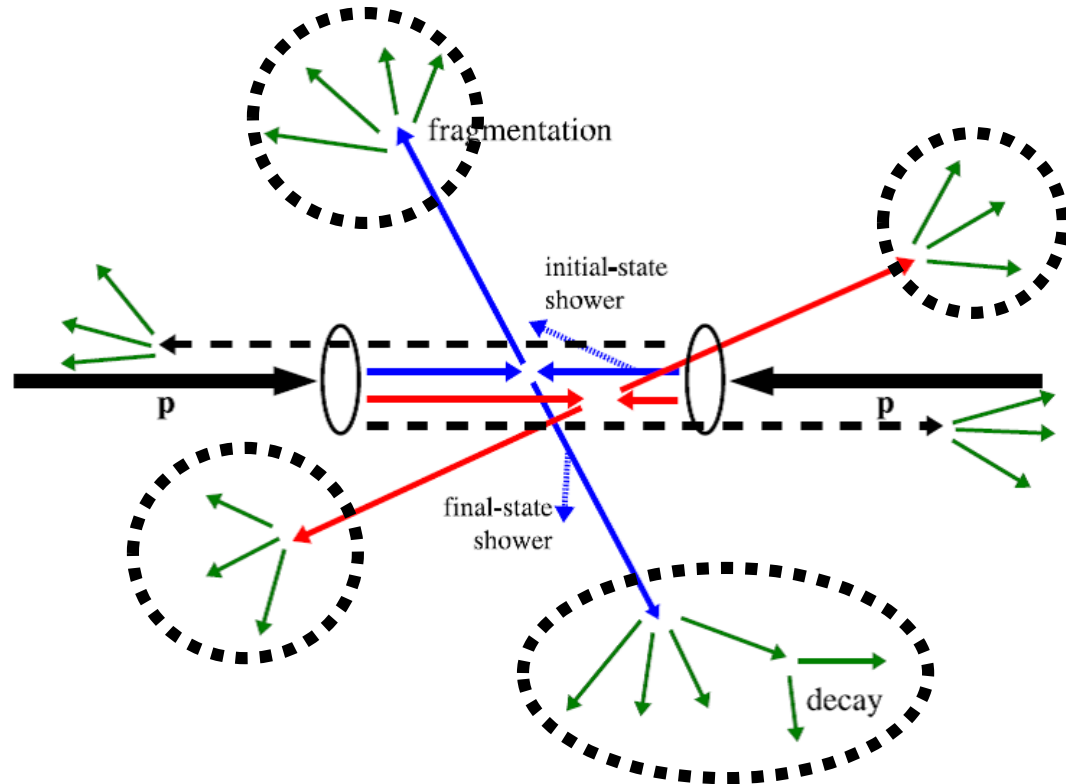
- Large range in Q^2
 - High Q^2 jets
 - Many low Q^2 processes



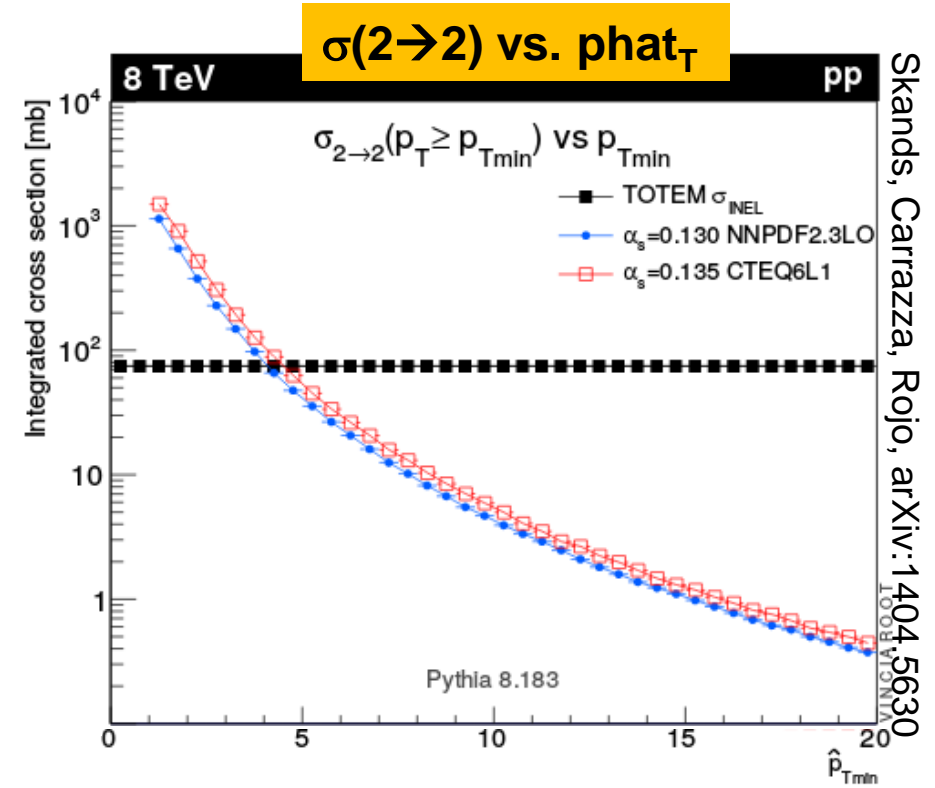
How to experimentally measured number of parton interactions?

Uncorrelated Seeds

- Identify sets of particles stemming from the same parton interactions (= seed)



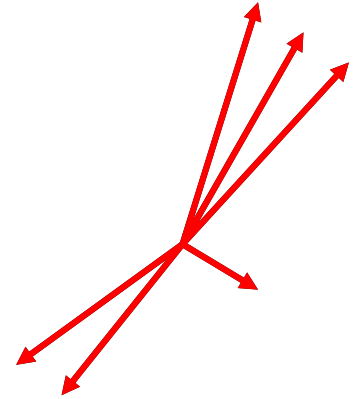
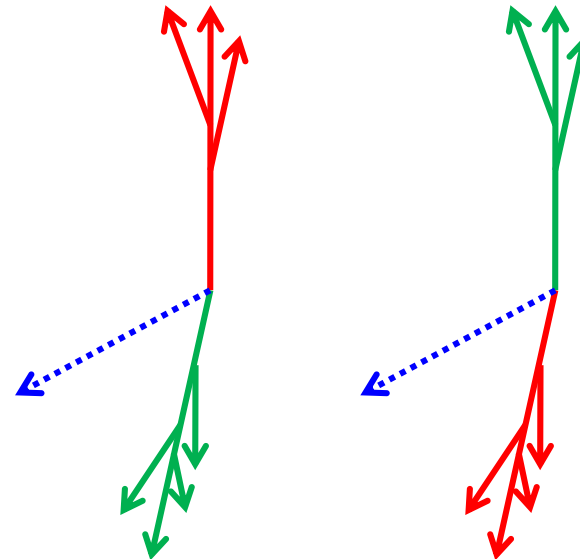
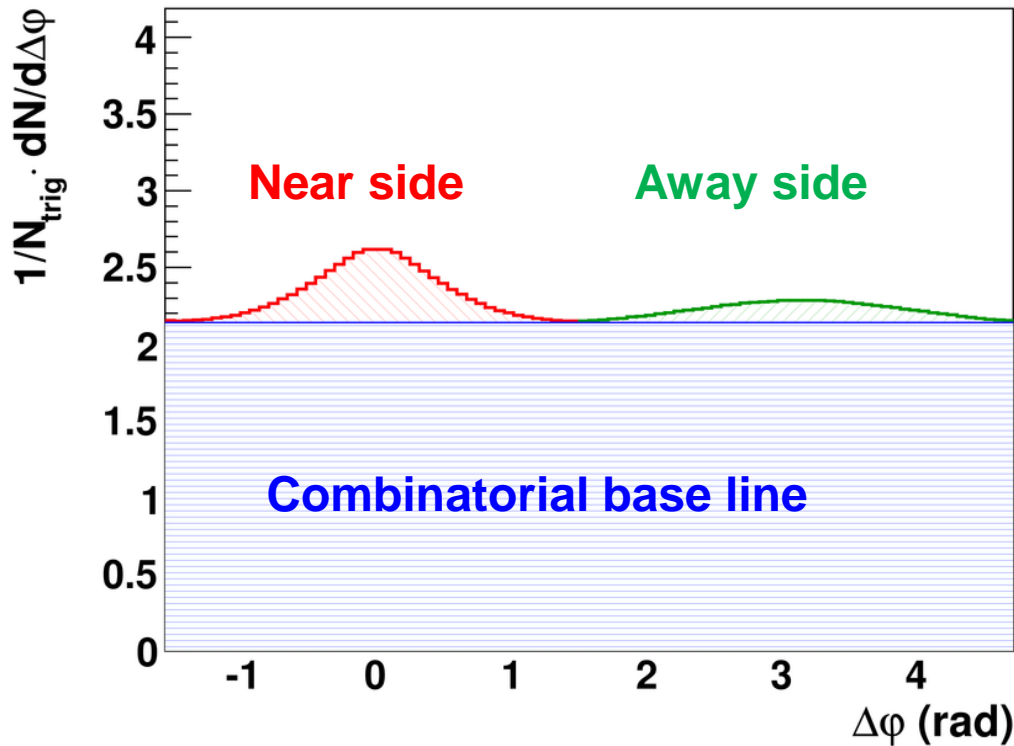
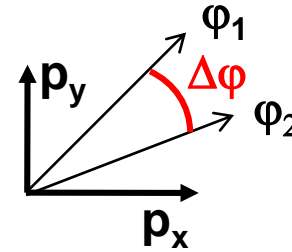
At high Q^2 , traditional jet finding \rightarrow identify each jet
 At low Q^2 , 1-2 particles \rightarrow statistical approach



If we want to get a handle on the overall number of MPI, low Q^2 processes crucial

Experimental Approach

- Correlate pairs of particles
- Record azimuthal differences



trigger particle
associated particle

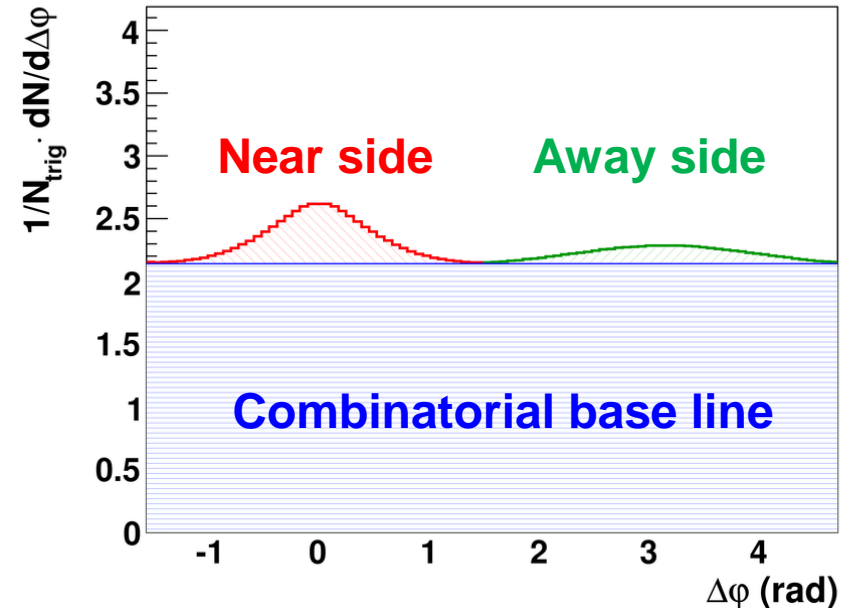
$$p_{T,assoc} < p_{T,trig}$$

 **Both jet sides can contribute to the near side and away side**



Pair Yield & Uncorrelated Seeds

- Pair yield $\frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\phi d\Delta\eta}$
- Number of triggers N_{trig}
- Number of associated particles
 - on the near side
 - on the away side
- Derive uncorrelated seeds



$$\langle N_{uncorrelated\ seeds} \rangle = \frac{\langle N_{trig} \rangle}{\langle 1 + N_{assoc,NS} + N_{assoc,AS} \rangle}$$

← Total number of particles

← How many particles belong “together”

← trigger particle



Pair Yield

- In symmetric p_T bins, with $p_{T,assoc} < p_{T,trig}$
- With n particles within a minijet, $n(n-1)/2$ pairs can be formed

$$\frac{\langle N_{pair} \rangle}{\langle N_{trig} \rangle} = \frac{\langle n(n-1)/2 \rangle}{\langle n \rangle} = \frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right)$$

- Depends on second moment $\langle n^2 \rangle$ of distribution $P(n)$
- Limit: small $\langle n \rangle$ and monotonically falling $P(n)$

$$\frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) \approx \underbrace{\frac{\langle n \rangle}{1 - P(0)} - 1}_{\text{Mean number of particles if at least one particle produced}}$$

Mean number of particles if at least one particle produced



Associated particles to a trigger



Pair Yield (2)

- Test $\frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) \approx \frac{\langle n \rangle}{1 - P(0)} - 1$

- Geometrical row

$$P(n) = (1-q)q^n \rightarrow \frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) = \langle n \rangle = \frac{\langle n \rangle}{1 - P(0)}$$

Exact!

- Poisson distribution

$$P(n) = \frac{\mu^n e^{-\mu}}{n!} \rightarrow \frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) = \frac{\mu}{2} \frac{\langle n \rangle}{1 - P(0)} - 1 = \frac{\mu}{2} - \frac{\mu^2}{6} + \dots$$

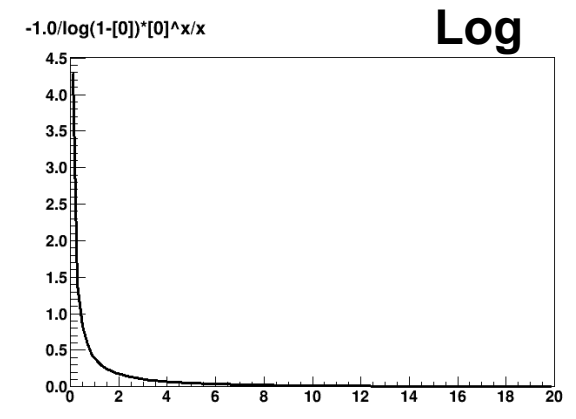
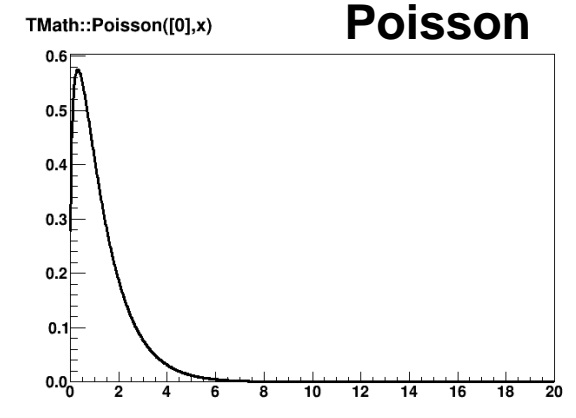
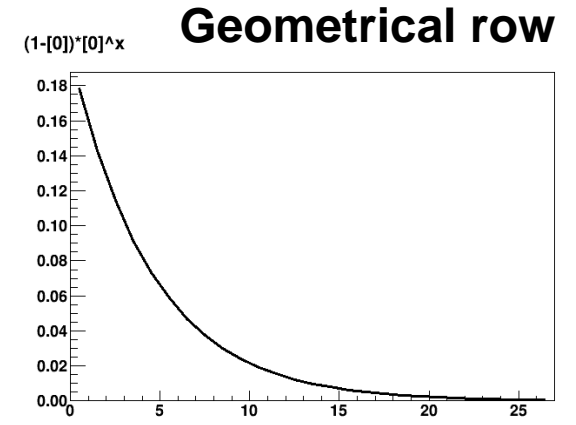
First order

- Log series

$$P(n) = \frac{1}{\ln(1-p)} \frac{p^n}{n}$$

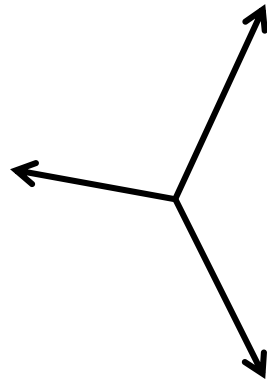
$$\rightarrow \frac{1}{2} \left(\frac{\langle n^2 \rangle}{\langle n \rangle} - 1 \right) = \frac{p}{2(1-p)} \frac{\langle n \rangle}{1 - P(0)} - 1 = \frac{p}{2(1-p)} + \frac{p^2}{3(1-p)} + \dots$$

First order





Uncorrelated Seeds: Numerical Example

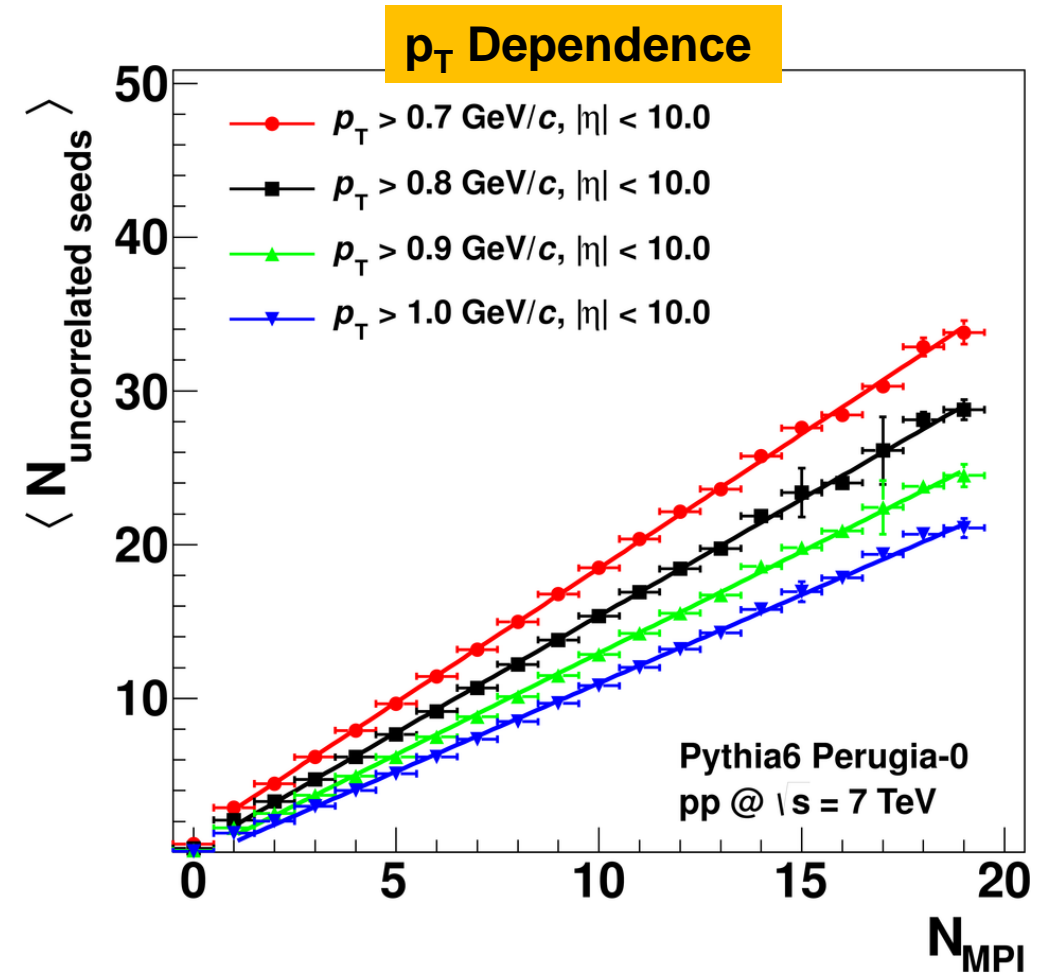
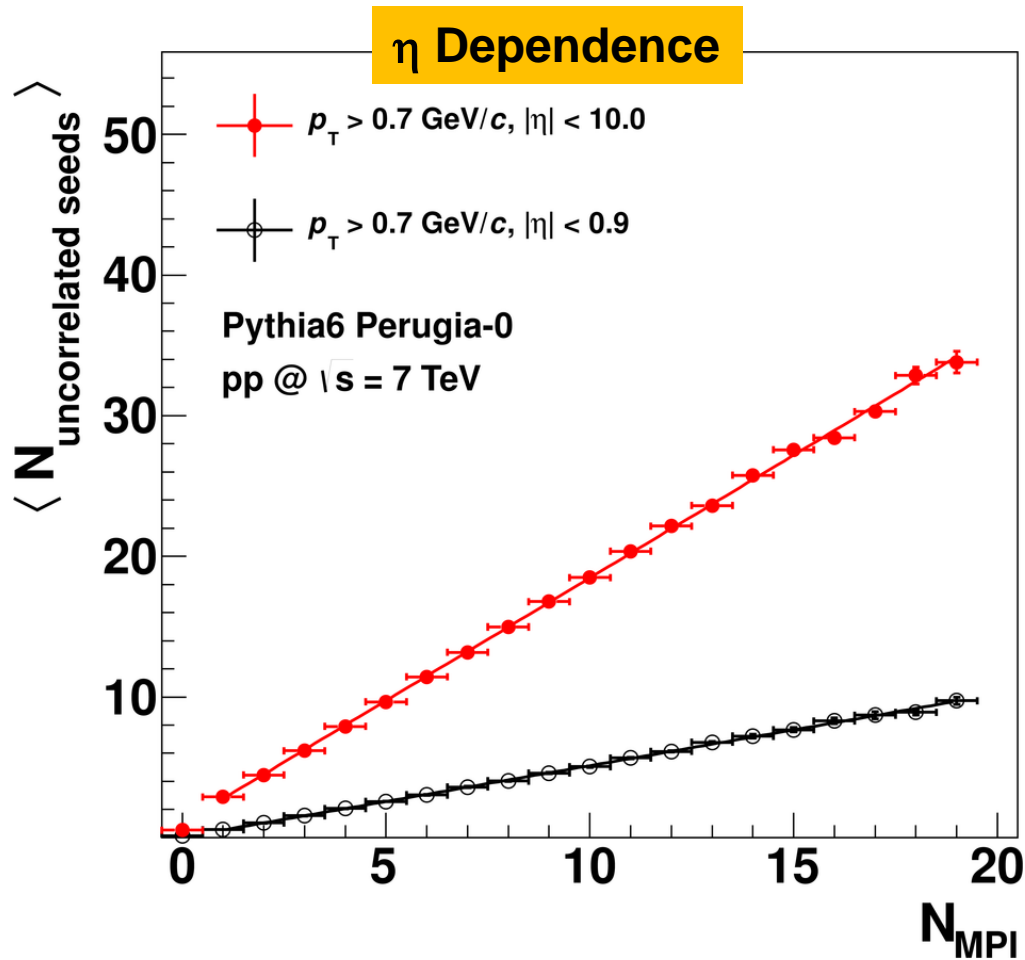


Seeds (true)	3
N_{trig}	3
N_{assoc}	$0 / 3 = 0$
$N_{uncorrelated\ seeds}$	$3 / (1 + 0) = 3$

$$\frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\varphi d\Delta\eta} \langle N_{uncorrelated\ seeds} \rangle = \frac{\langle N_{trig} \rangle}{\langle 1 + N_{assoc,NS} + N_{assoc,AS} \rangle}$$

Approximation!

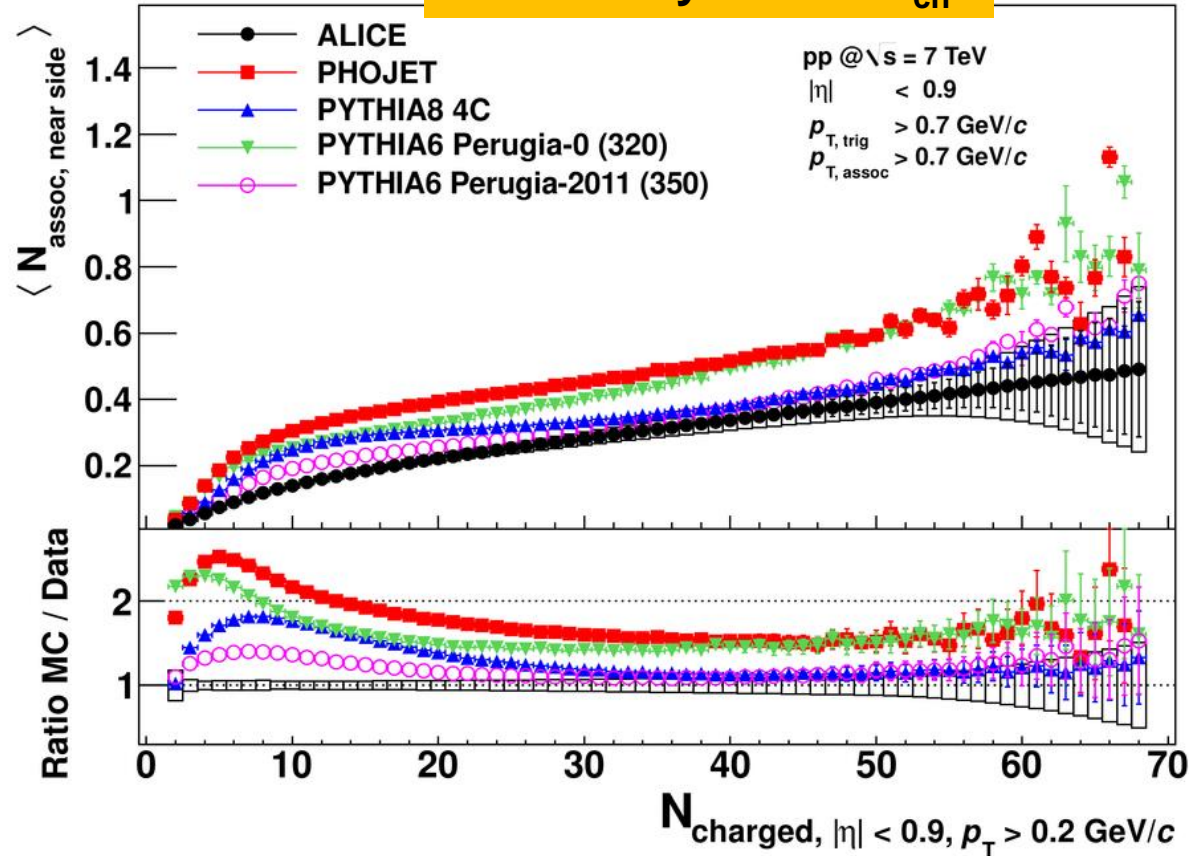
Relation of Uncorrelated Seeds and MPI



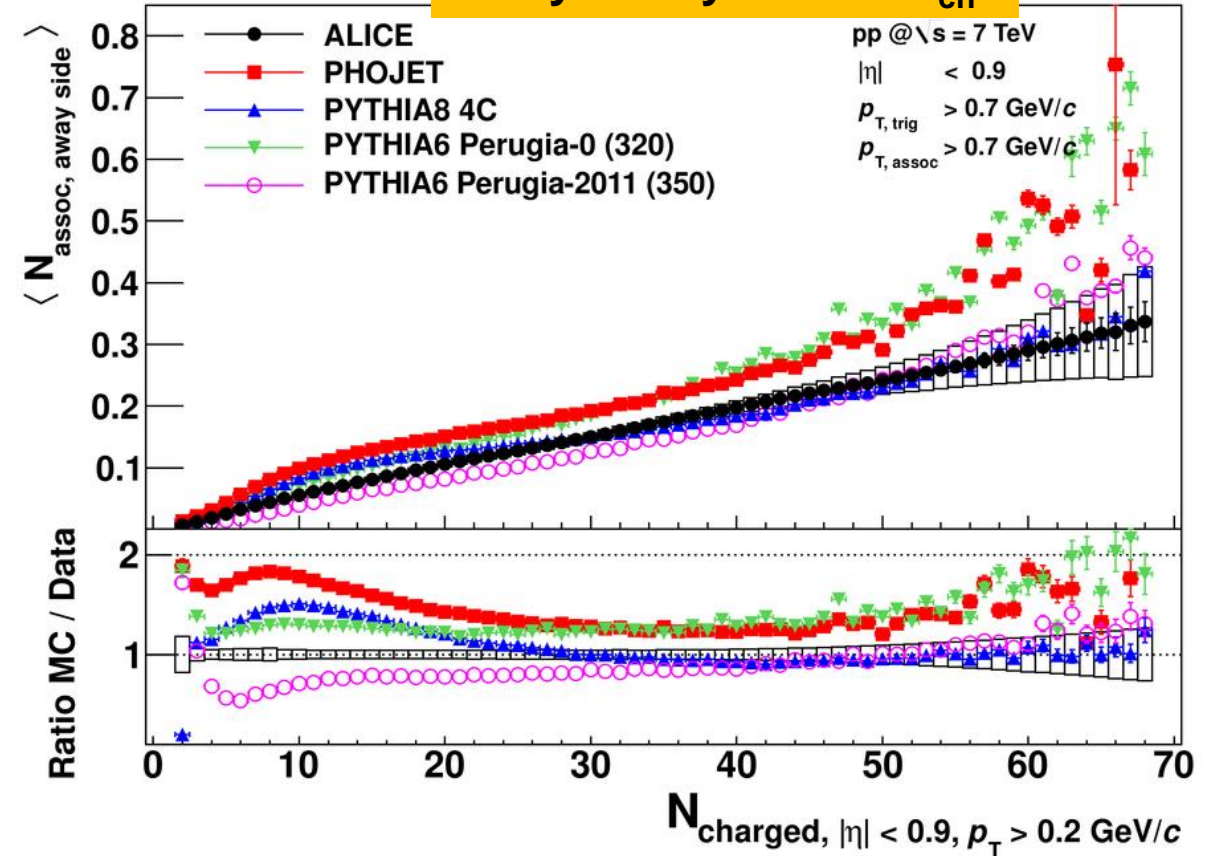
In Pythia, clear proportionality

Results: Pair Yields

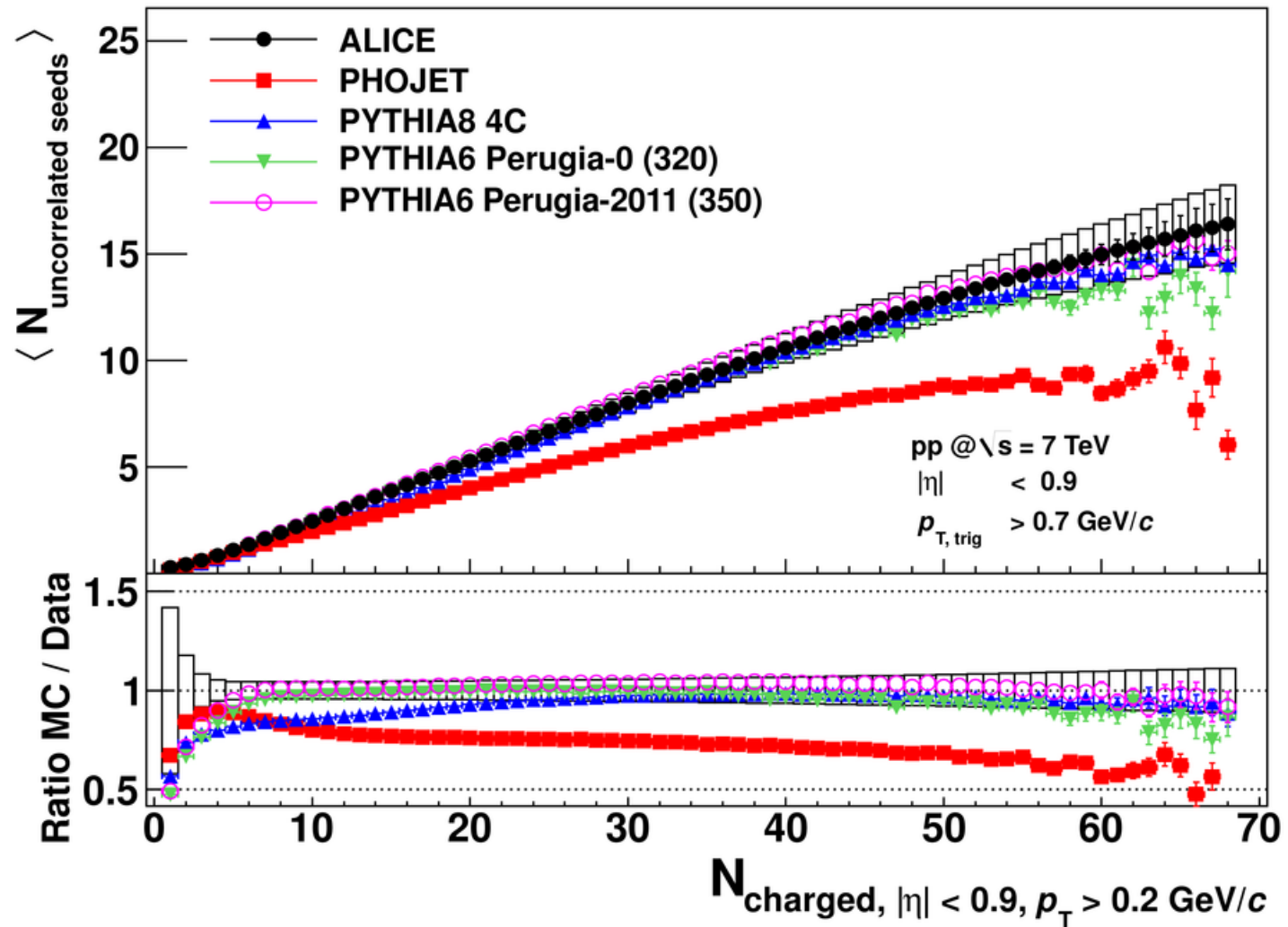
Near-side yield vs. N_{ch}



Away-side yield vs. N_{ch}

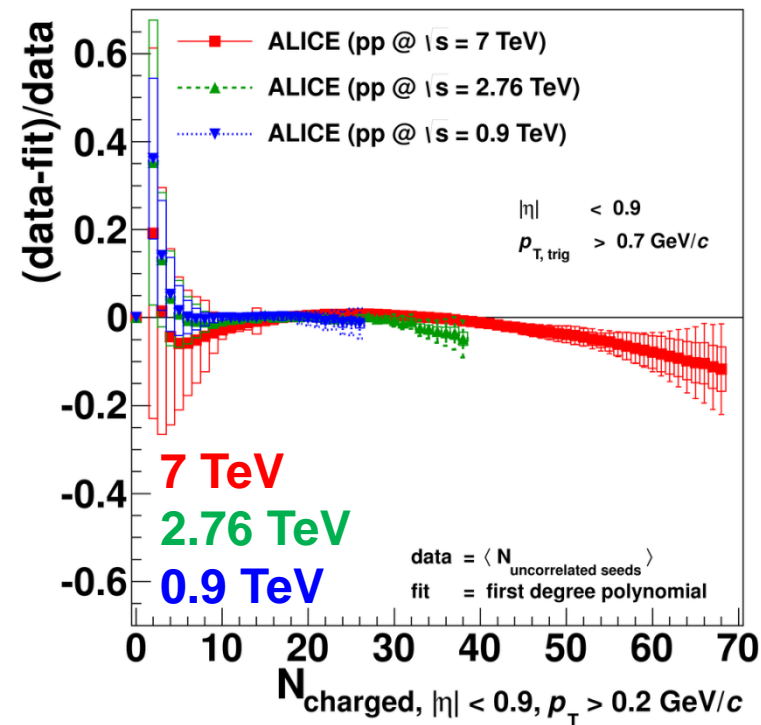
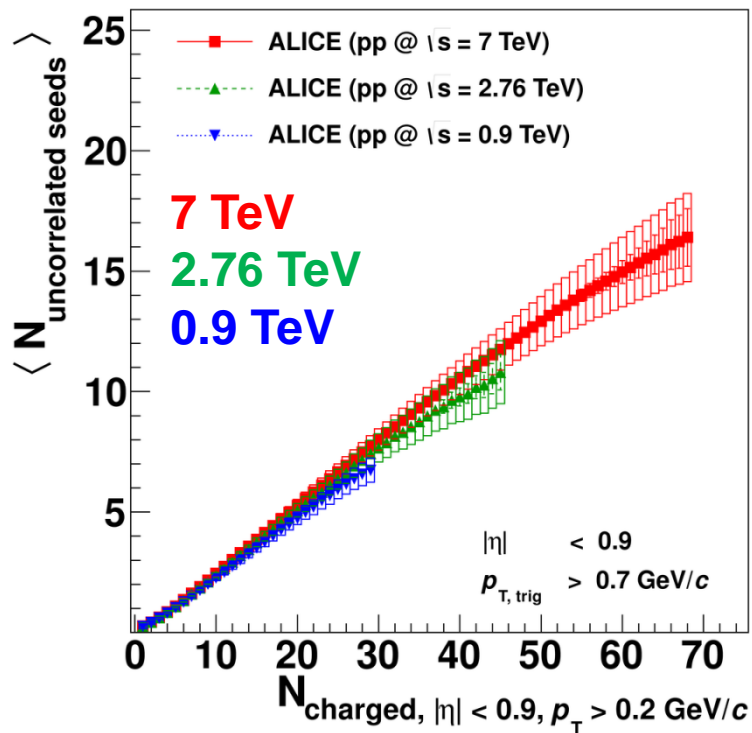


Results: Uncorrelated Seeds



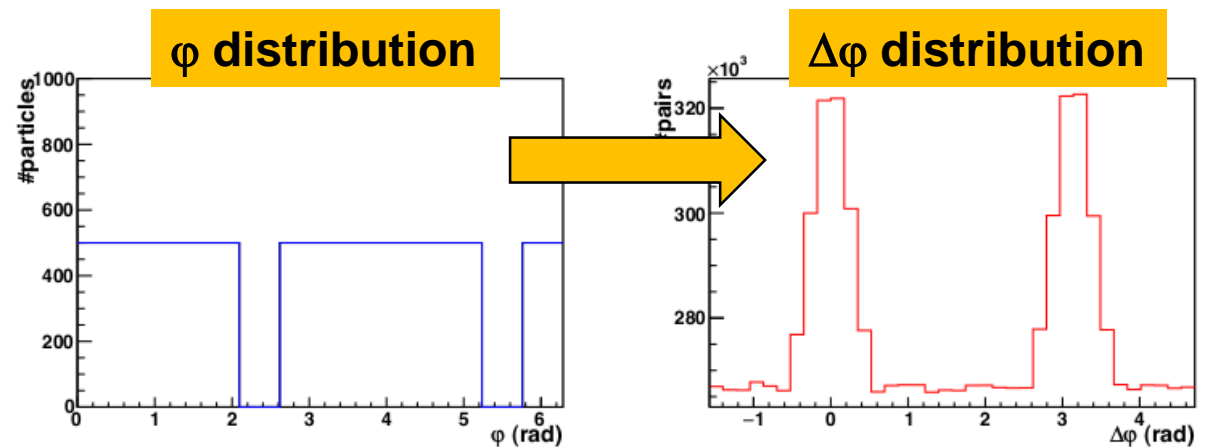
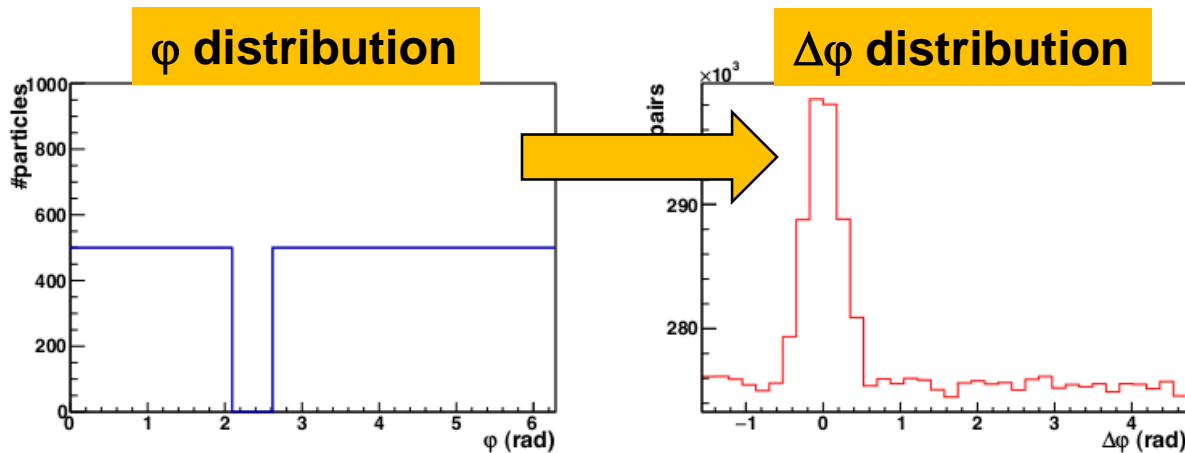
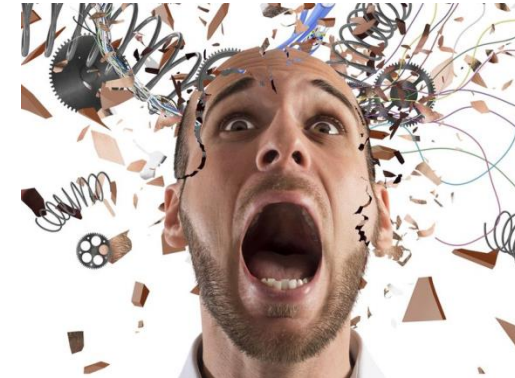
Uncorrelated Seeds

- Uncorrelated seeds (\sim MPI) increase linearly with N_{ch}
- At large N_{ch} , limit of MPI?
(i.e., larger multiplicity by fluctuation, not by additional MPI)



New data will tell...

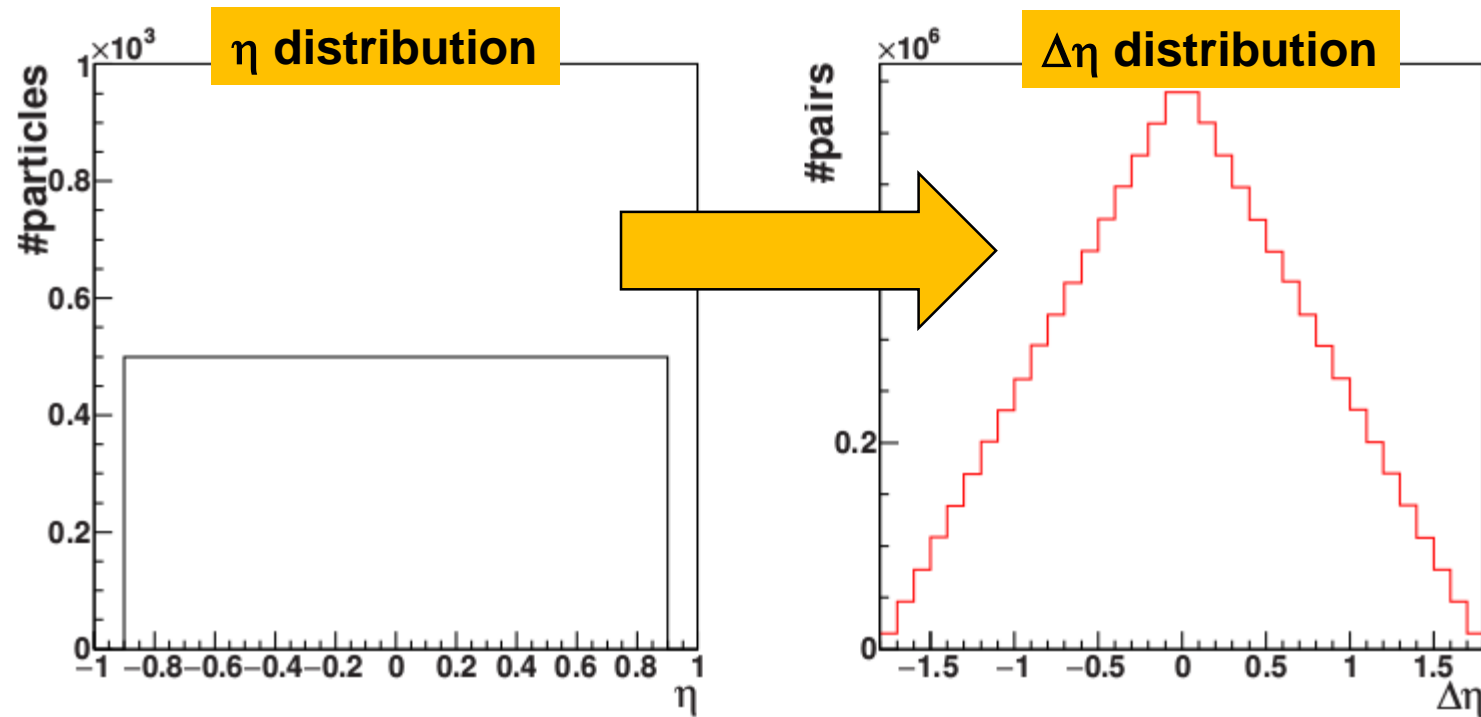
- Correlation measurements sensitive to detector acceptance
 - “Background” from non-uniform detector acceptance easily larger than signal
- Drawing particles from uniform distribution with
 - One gap \rightarrow peak structure in two-particle $\Delta\phi$ distribution
 - Two gaps \rightarrow back-to-back structure in two-particle $\Delta\phi$ distribution



Figures: Emilia Leogrande

Limited η Acceptance

- Detector limit in pseudorapidity
- Leads to tent in two-particle $\Delta\eta$ distribution



Event Mixing



**Not any two events can be mixed!
Similar multiplicity and detector acceptance (z vertex) needed.**

- These effects can be estimated and corrected data-driven
- Signal S contains correlation within an event

$$S(\Delta\varphi, \Delta\eta) = \frac{1}{N_{trig}} \frac{d^2 N_{pairs,same}}{d\Delta\varphi d\Delta\eta}$$

- Background B contains "correlation" between different events

$$B(\Delta\varphi, \Delta\eta) = \alpha \frac{1}{N_{trig}} \frac{d^2 N_{pairs,mixed}}{d\Delta\varphi d\Delta\eta}$$

- Estimates pair efficiency and acceptance
- Normalized such that $B(0,0) = 1$
 - Two particles going in the same direction, see the same acceptance
- Associated yield per trigger particle

$$\frac{1}{N_{trig}} \frac{d^2 N_{assoc}}{d\Delta\varphi d\Delta\eta} = \frac{S(\Delta\varphi, \Delta\eta)}{B(\Delta\varphi, \Delta\eta)}$$

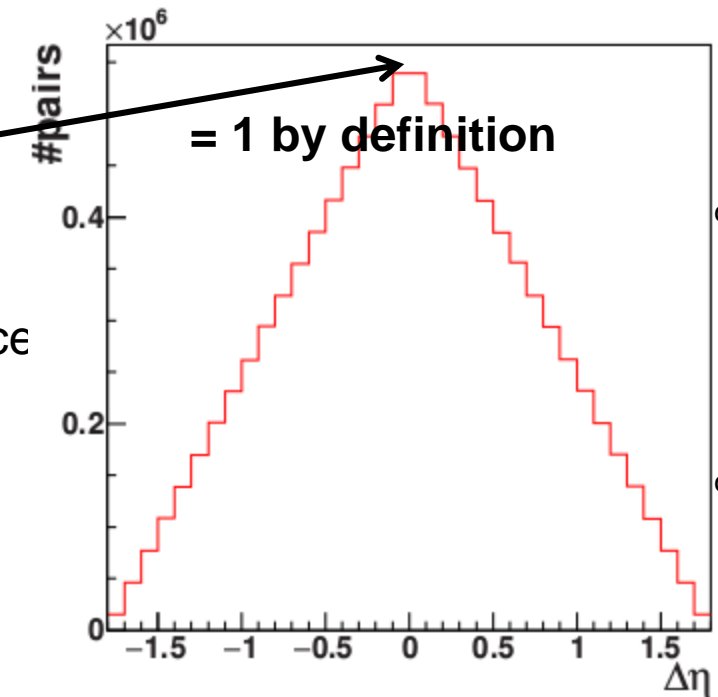


Figure: Emilia Leogrande



Summary

Uncorrelated Seeds

- Two-particle correlations measure associated particle yields
- Allows to calculate uncorrelated seeds

- These are proportional in Pythia to the number of MPI
- Direct access to number of low Q^2 scatterings

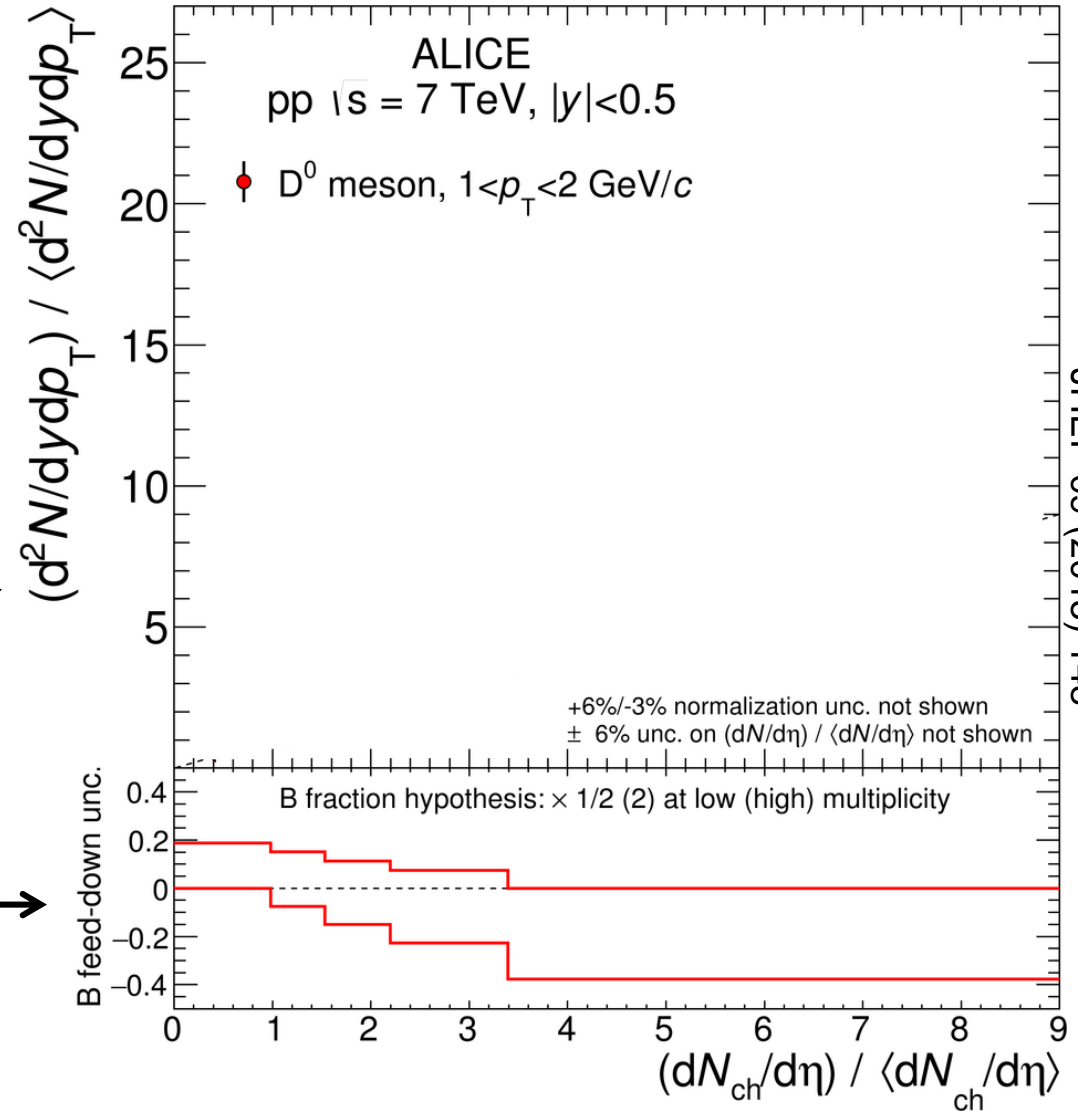
- At high multiplicity, hint of limit in the number of MPI



Hard Probes vs. Multiplicity

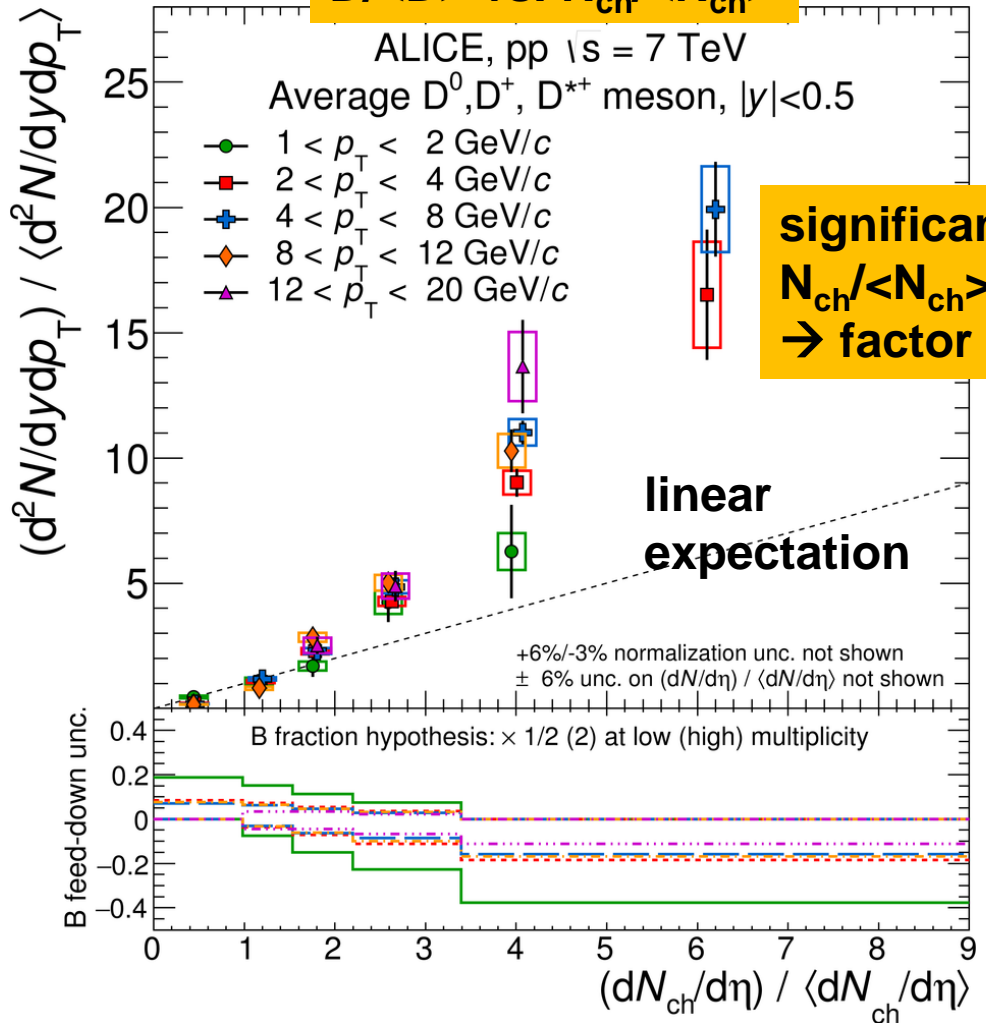
Hard Probes

- Multiplicity, underlying event activity and uncorrelated seeds probe soft part of MPI
- How does hard MPI production behave?
- How are the soft and hard related?
- Measurement of D and J/ψ
 - c produced in hard scattering ($m_c = 1.28 \text{ GeV}/c$)
- Experimentally expressed as $D/\langle D \rangle$ vs. $N_{ch}/\langle N_{ch} \rangle$
- For D: B feeddown fraction relevant ($B \rightarrow D + X$)

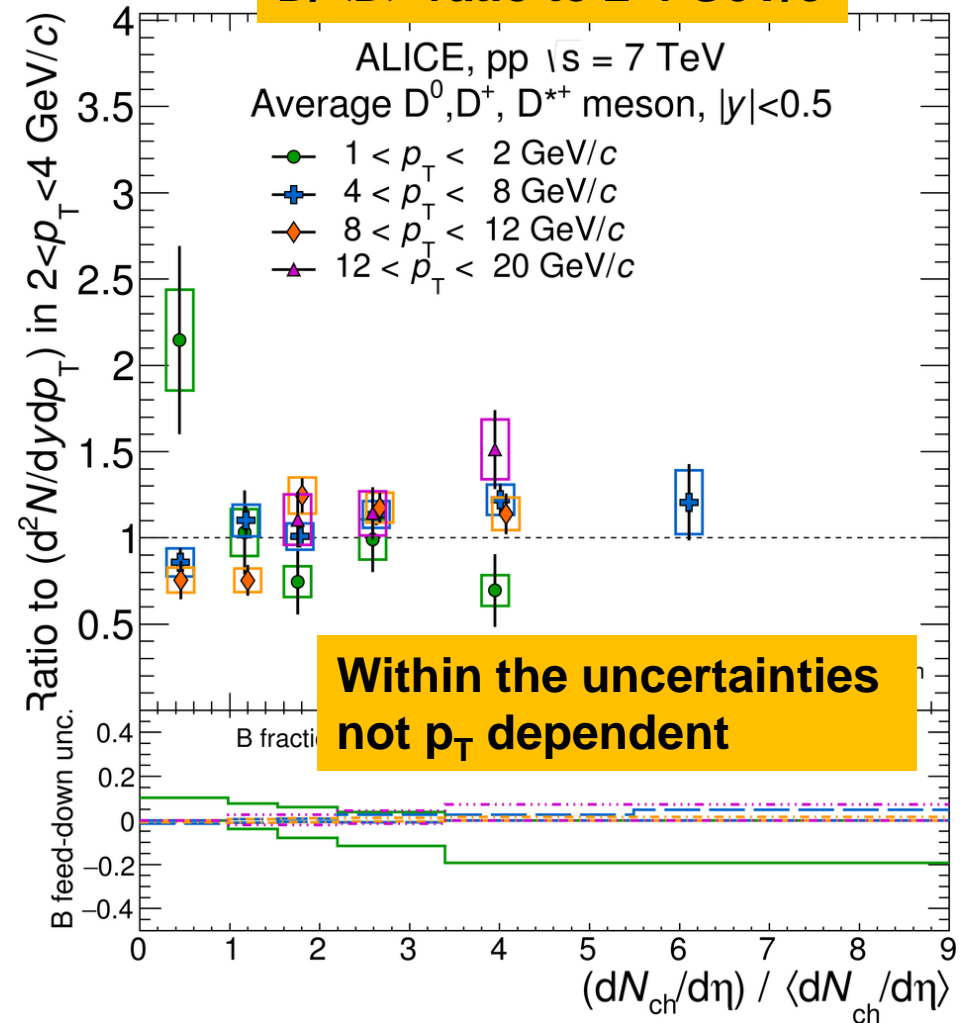


D Production vs. Multiplicity

D/<D> vs. $N_{ch}/\langle N_{ch} \rangle$

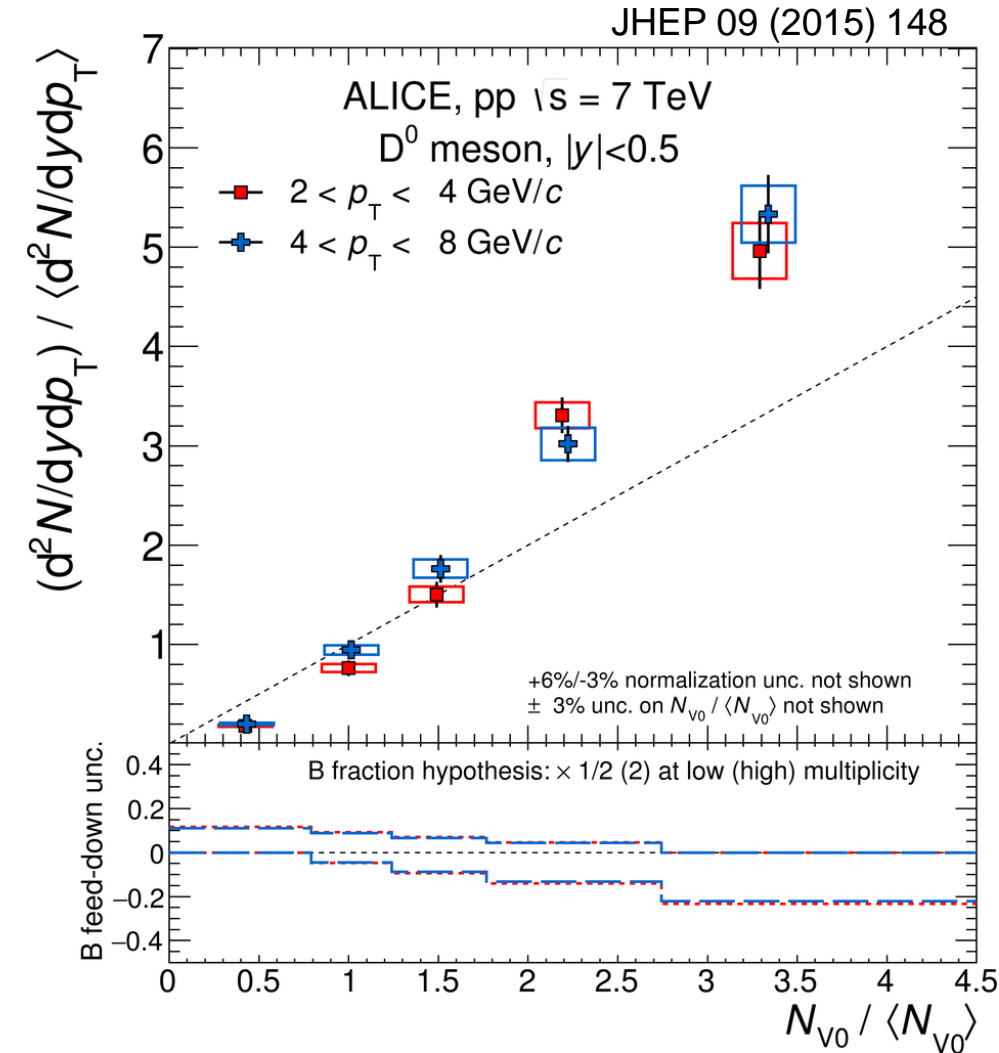


D/<D> ratio to 2-4 GeV/c



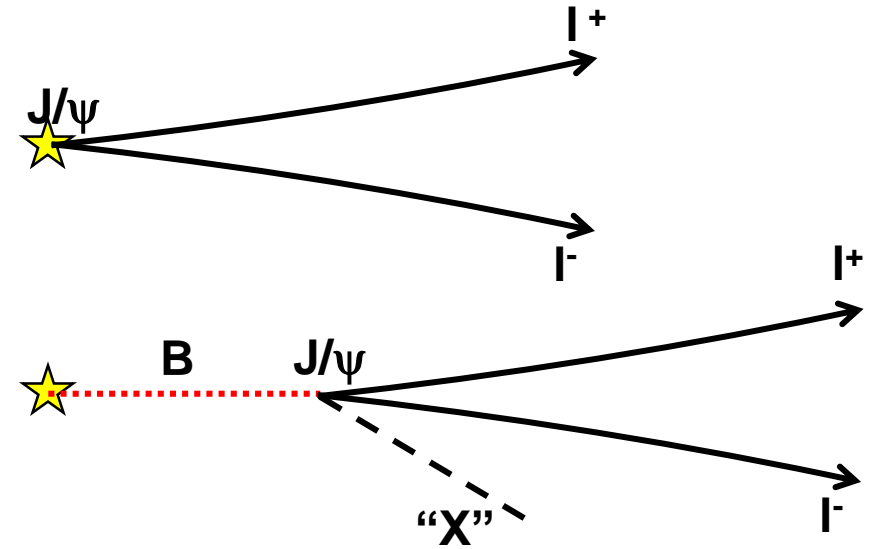
Multiplicity Estimator

- D and N_{ch} measured in same rapidity
 - Autocorrelation bias?
 - Associated soft particle production with D ?
- Measure $D/\langle D \rangle$ vs. forward multiplicity
 - “V0” ($-3.7 < \eta < -1.7$ and $2.8 < \eta < 5.1$)
- Similar increase observed
 - Factor 5 at $N_{ch}/\langle N_{ch} \rangle = 3.5$
 - Multiplicity reach is smaller forward than at mid-rapidity



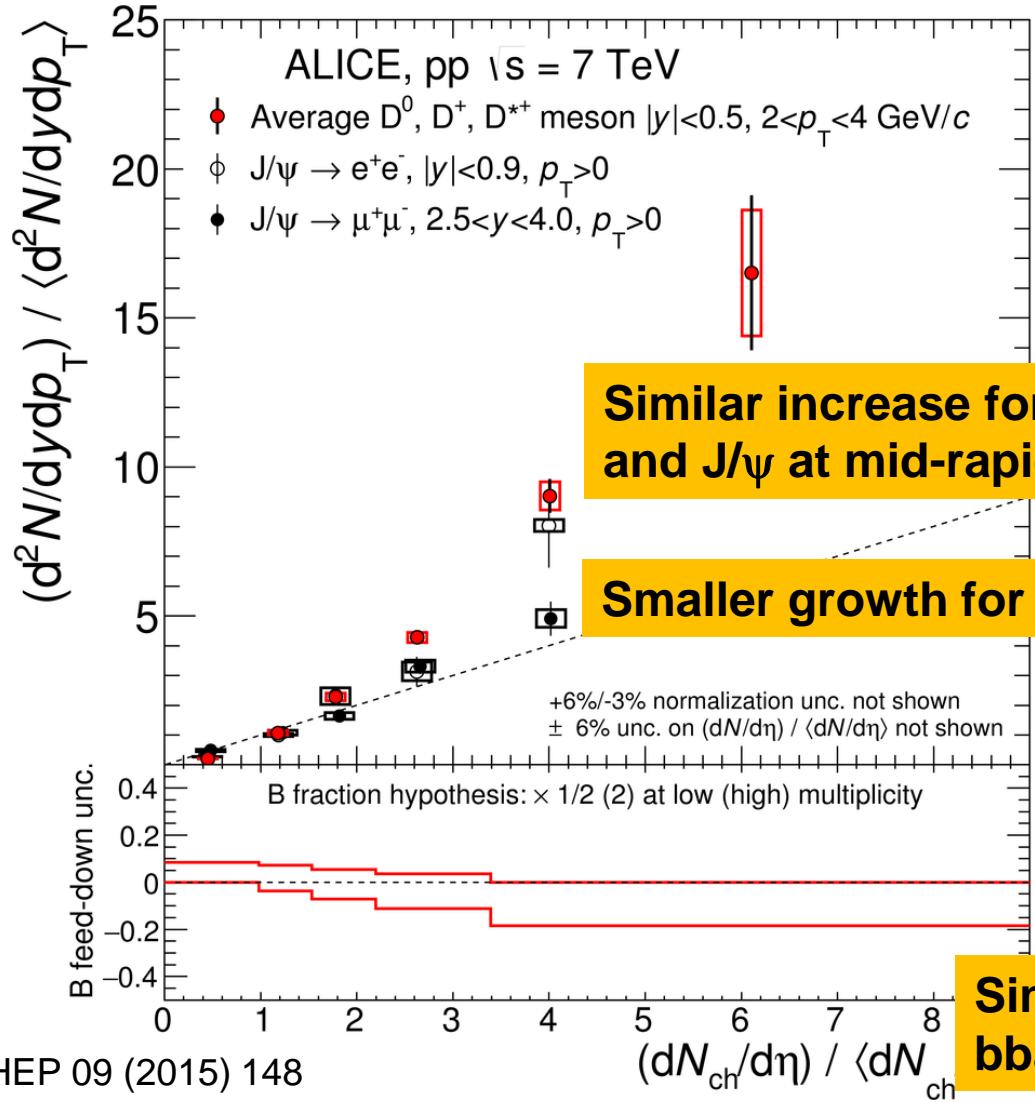
J/ψ Production

- J/ψ are produced
 - in the collision “prompt”
[direct from process producing c \bar{c}]
 - from the decay of a B quark “non-prompt”
[process has produced b quark]



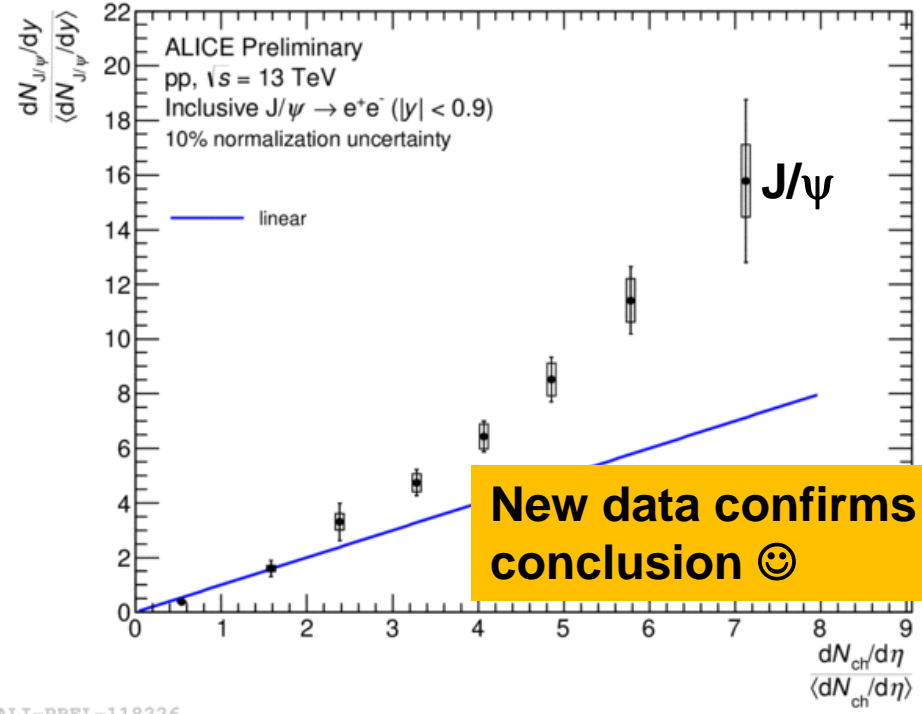
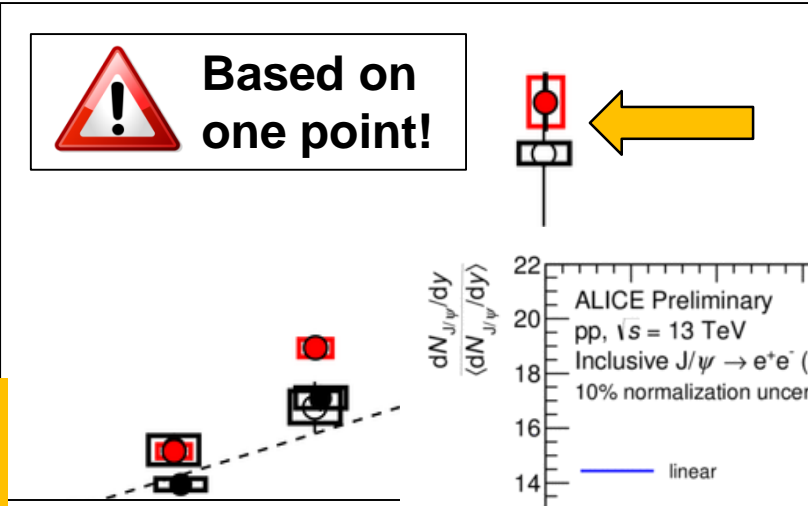
- Different physics
- Can be experimentally distinguished by J/ψ impact parameter

J/ψ vs. Multiplicity



Similar increase for D and J/ψ at mid-rapidity

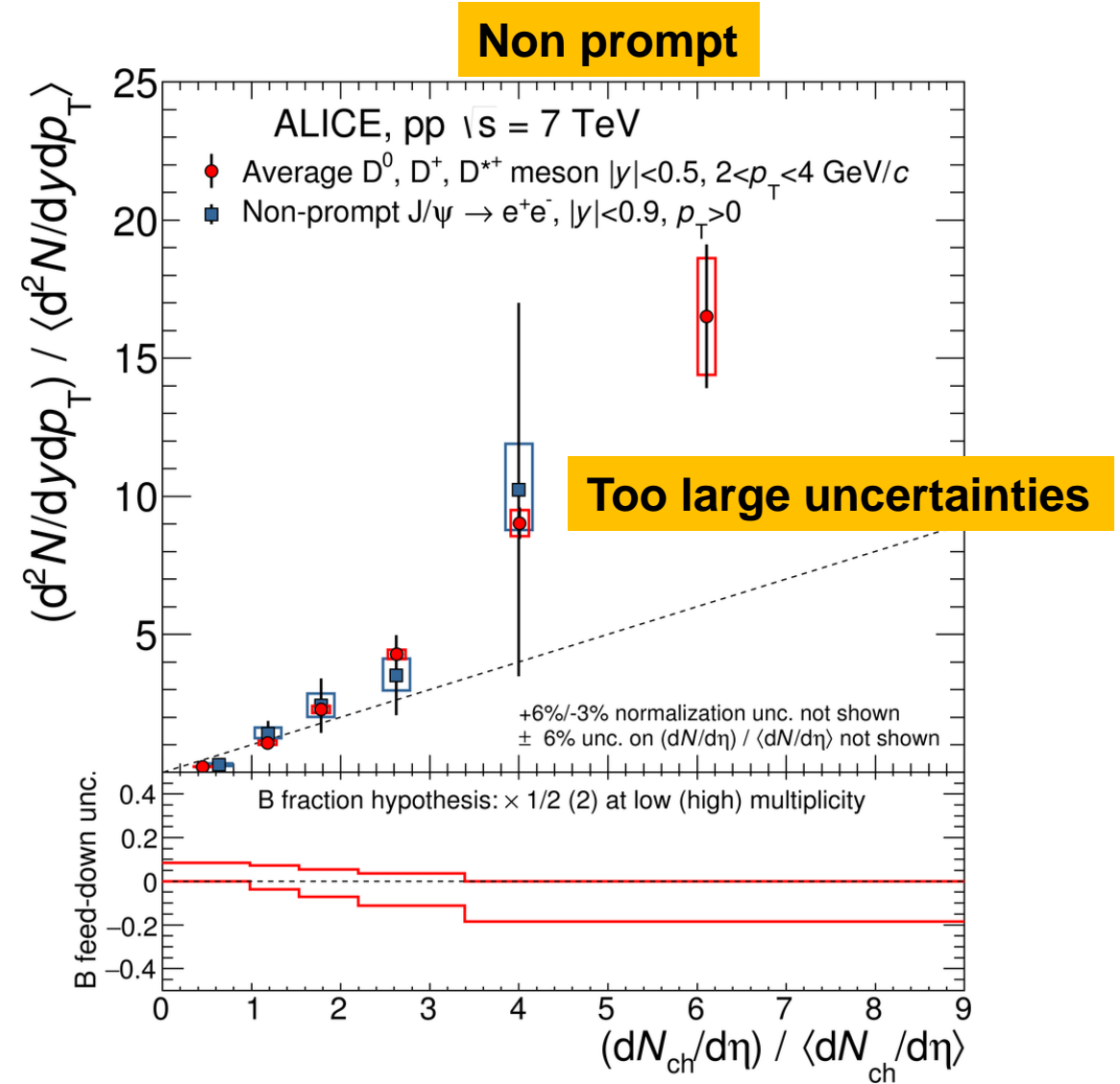
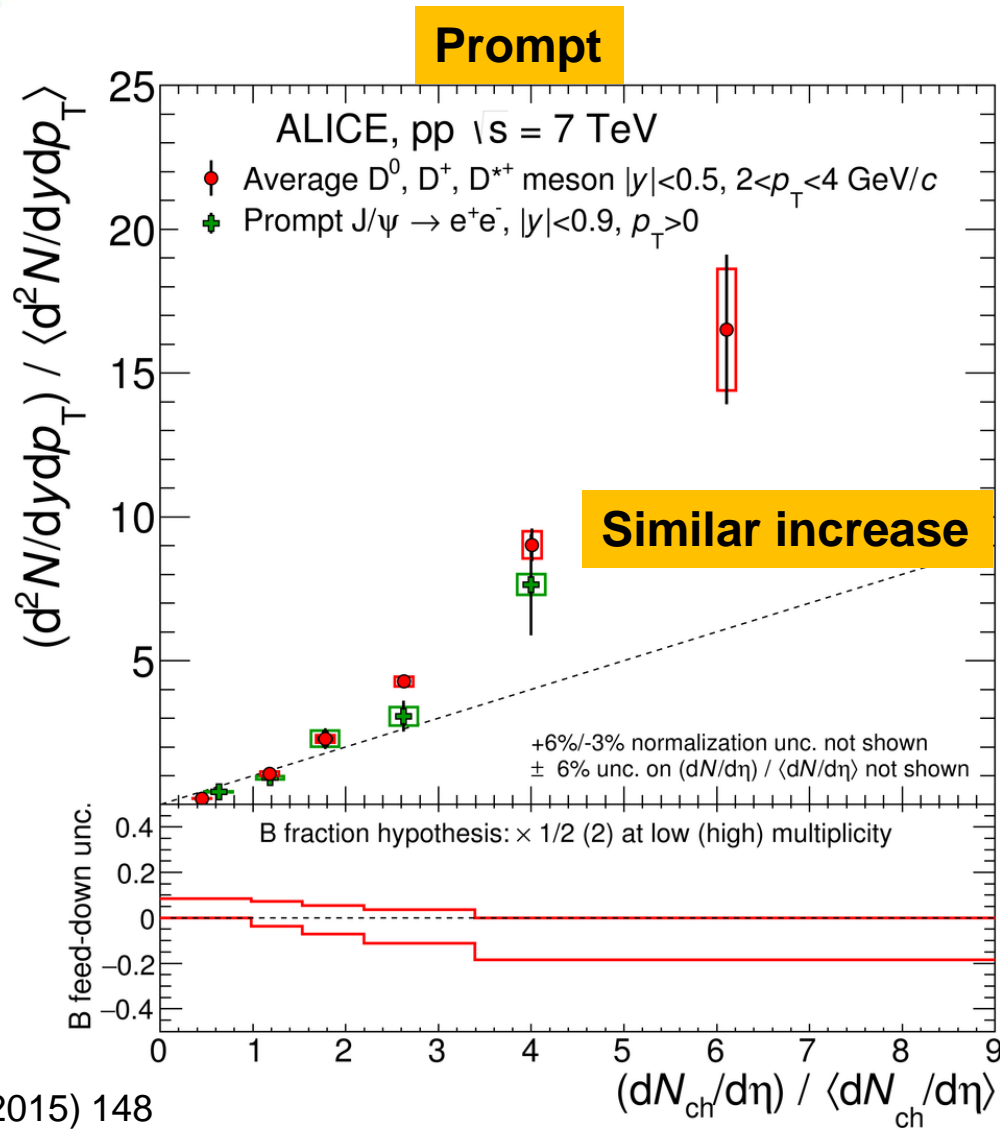
Smaller growth for forward J/ψ



New data confirms conclusion 😊

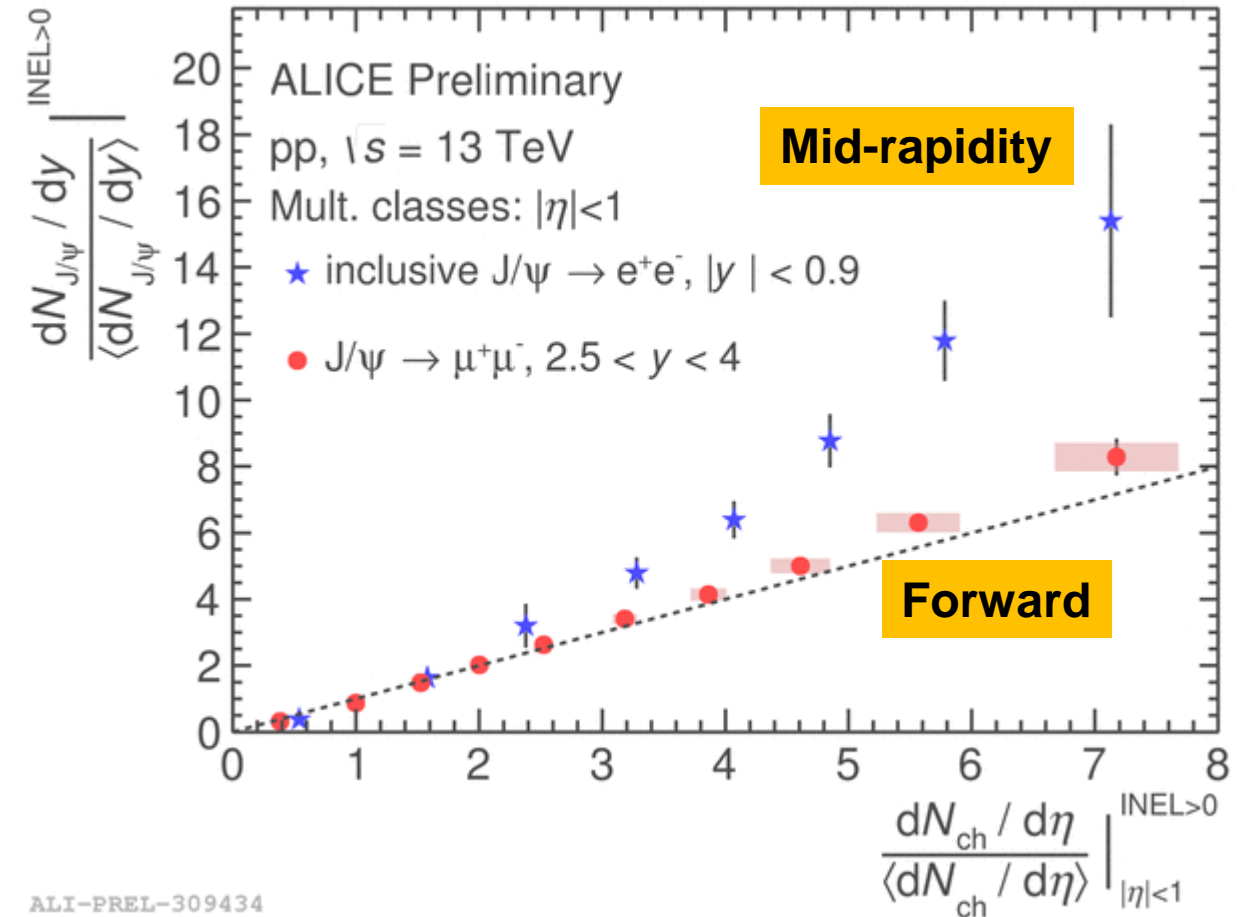
Similar increase for D and J/ψ → increase related to c \bar{c} and b \bar{b} production process (only minor influence of hadronisation)

Prompt and Non-prompt



Rapidity Dependence

- Growth significantly larger at mid-rapidity than at forward rapidity
- Autocorrelation bias
 - Multiplicity measured in same phase space as hard probe
 - Discussed later



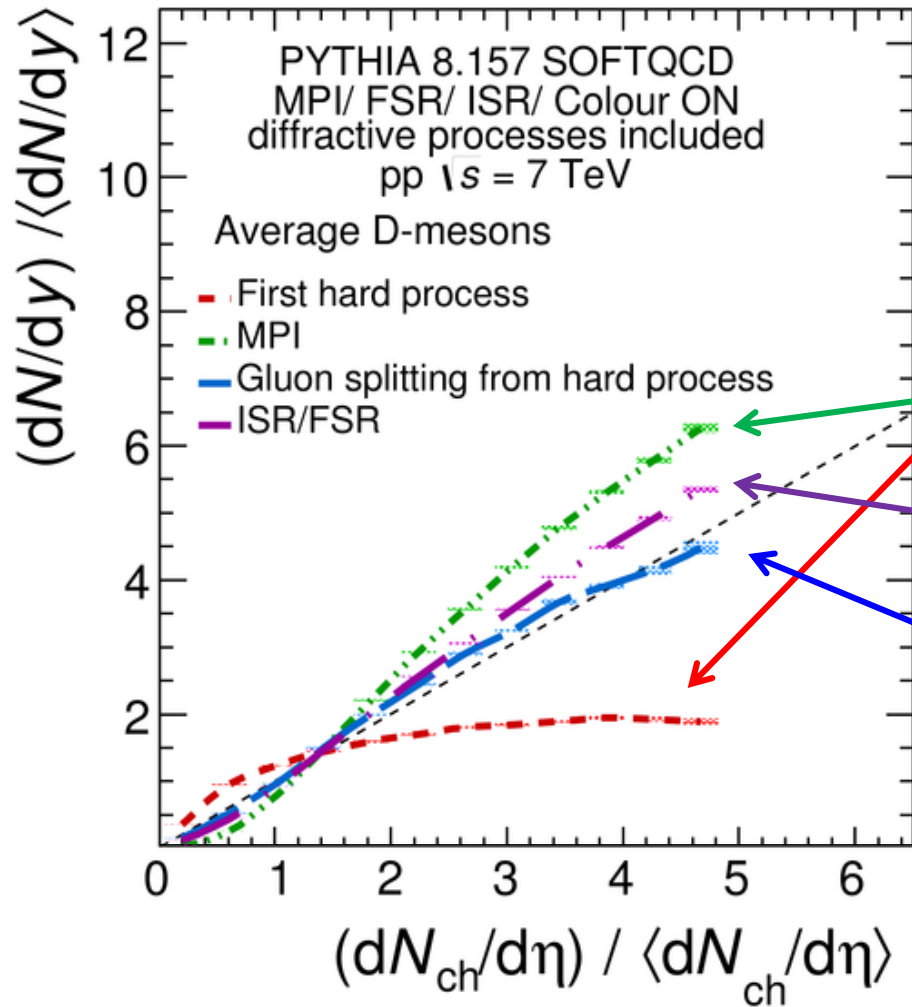


Recap

- D and J/ψ at mid rapidity grow faster than the average multiplicity
 - Within current precision: p_T independent
 - Smaller growth for forward rapidity
 - At least partly an auto-correlation effect
 - Within current precision, no conclusion for non-prompt component
-
- How to interpret this growth within a MC?



D Production in Pythia 8



First $2 \rightarrow 2$ scattering

- Gluon fusion ($gg \rightarrow c\bar{c}$)
- See quark ($cu \rightarrow cu$)

11%

Subsequent $2 \rightarrow 2$ scattering (MPI)

- Gluon fusion ($gg \rightarrow c\bar{c}$)
- See quark ($cu \rightarrow cu$)

21%

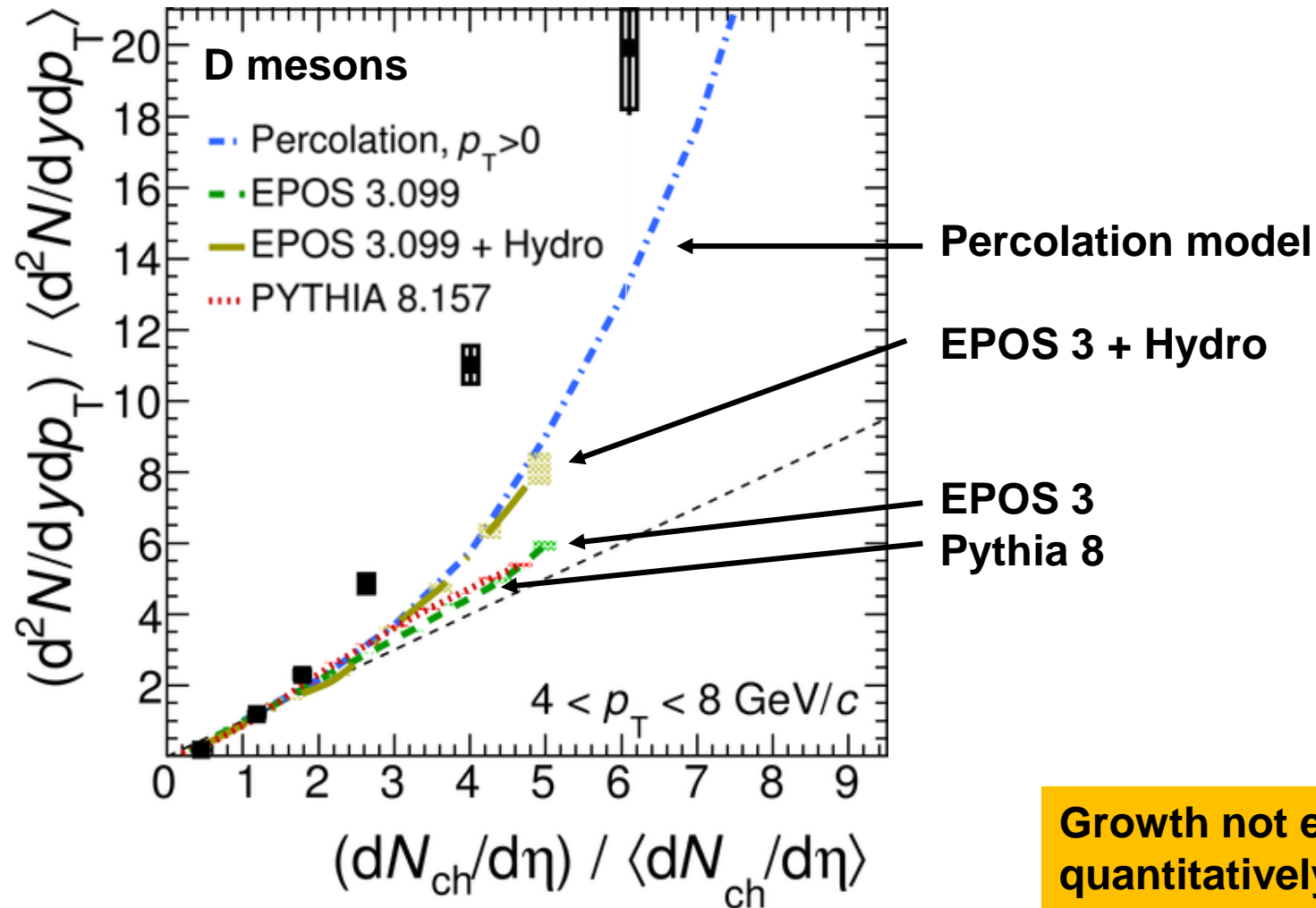
Gluon from Initial or final state radiation splits into c quark

62%

$2 \rightarrow 2$ scattering produces high virtuality gluon which splits into c quark

6%

Further Model Comparisons





Summary

Hard Probes vs. Multiplicity

- D and J/ψ measured as a function of multiplicity
 - Proxy of the correlation of the production of hard and soft probes
- Rapidity dependence reveals auto-correlation bias

- D and J/ψ yields grow faster than multiplicity
- Quantitatively not explained by current models



Hard Double Parton Scattering

Effective Cross-Section

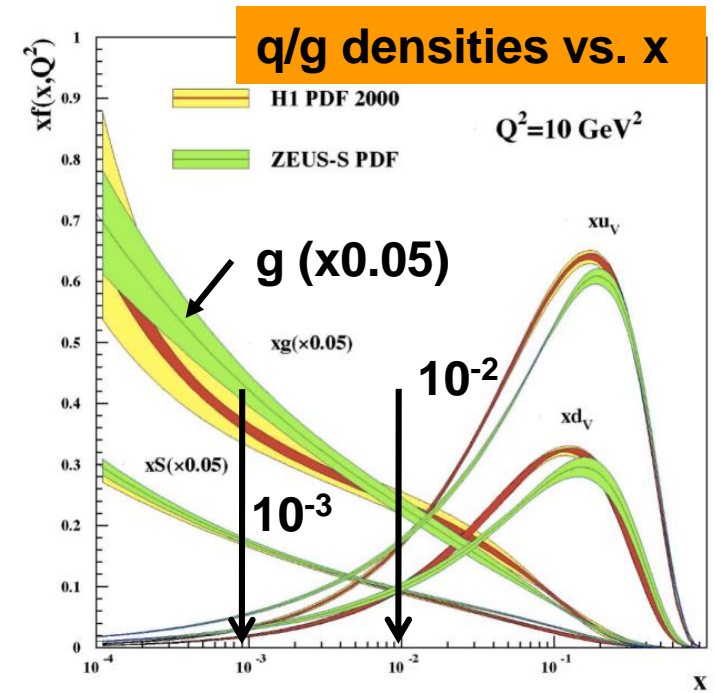
- Ample evidence for MPI at soft scales ($Q^2 \sim \text{few GeV}^2$)
- Semi-hard production also involved in MPI (D, J/ψ)
- What about higher Q^2 ?
 - $2 \rightarrow 2$ scattering probes higher x partons
 - densities are lower at larger x ($x \sim 2 p_T / \sqrt{s}$)
- Quantified by effective cross-section σ_{eff}

$$\sigma_{\text{eff}} = \frac{\sigma_i \sigma_j}{\sigma_{ij}} \quad \sigma_{\text{eff}} = \frac{\sigma_i^2}{2\sigma_{ii}}$$

- Process independent!
- “Encodes” PDF
- In Eikonal picture

↑ prefactor for identical processes

$$\sigma_{\text{eff}} = \frac{1}{\int d^2b A(b)^2} \quad \int d^2b A(b) = 1 \quad \mathbf{A(b)} = \text{“overlap distribution”}$$



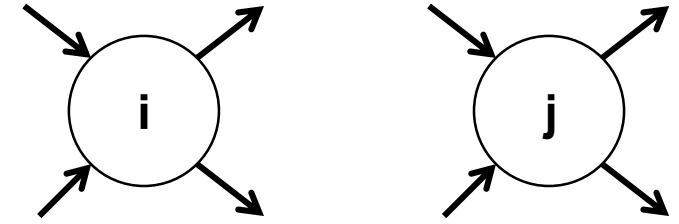
σ_i inclusive \rightarrow if occurs twice in the same event, i needs to be counted twice

σ_{ij} only in double parton scattering (not in two separate parton scatterings)



What is σ_{eff} ?

- Process i with σ_i
- Process j with σ_j
- Probability σ_{ij} to have i and j at the same time?
 - As independent processes



$$\sigma_{\text{eff}} = \frac{\sigma_i^2}{2\sigma_{ii}} \quad \sigma_{\text{eff}} = \frac{\sigma_i \sigma_j}{\sigma_{ij}}$$

Multiplying probabilities is very typical. Imagine 2 dice with 6 sides each.

What is the probability to roll two times 1?

→ $1/6 * 1/6 = 1/36$

However, here we look for the probability that processes occur alone or together.

- For Poisson distribution and identical processes
 - $P(1) = e^{-\lambda} \lambda$ $P(2) = e^{-\lambda} \lambda^2/2$
 - $\sigma_{\text{eff}} = 1$
- For pp collisions at LHC, $\sigma_{\text{eff}} \sim 20 \text{ mb}$
 - Prefactor encoding circumstances in which processes occur

$$\sigma_{ij} = \frac{1}{\underbrace{\sigma_{\text{eff}}}_{\text{“suppression factor”}}} \sigma_i \sigma_j$$

How to measure σ_{eff} ?

Measure single process i

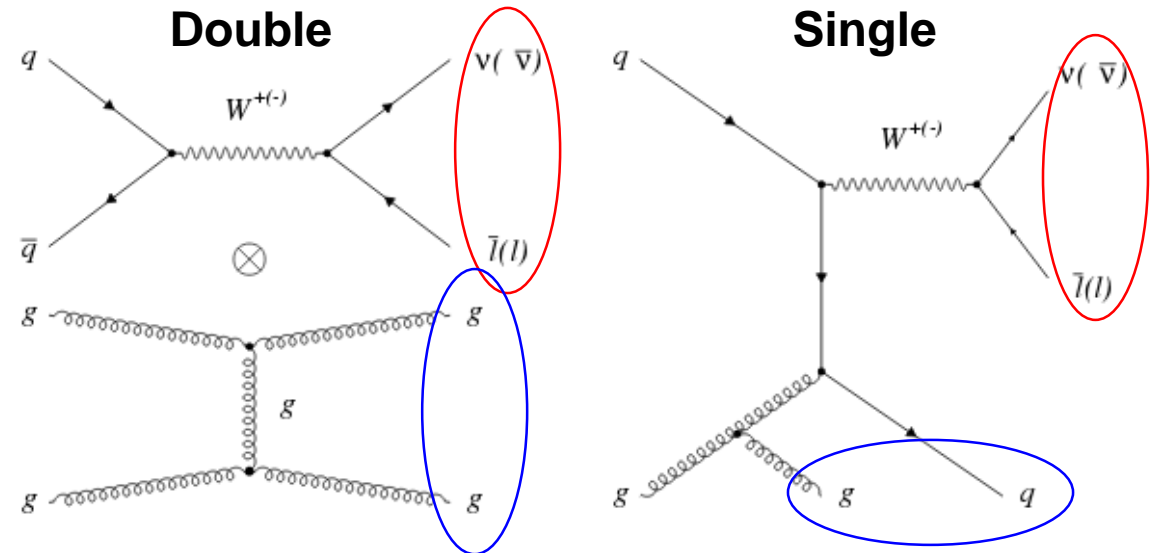
Measure single process j

$$\sigma_{\text{eff}} = \frac{\sigma_i \sigma_j}{\sigma_{ij}}$$

Measure processes i and j
in the same event and

from different parton scatterings

- Trivial if we would know that i and j cannot come from the same parton scattering
 - Not the case in practice
- Example: W+2 jet events



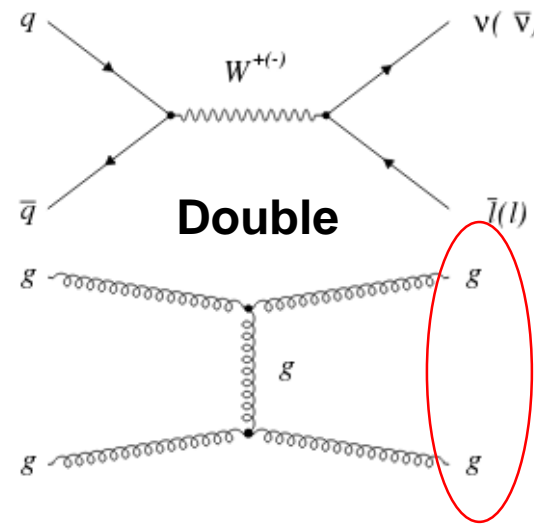
- Need experimental handle to distinguish single and double parton scattering

Distinguish single and double parton scattering in $W+2$ jet events

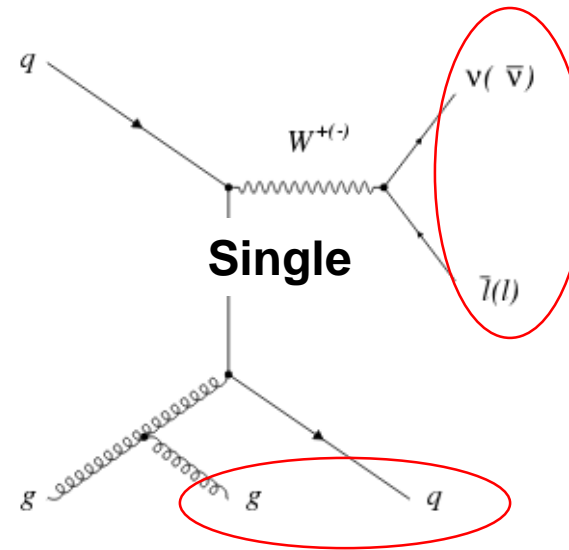
Azimuthal angle between W and dijet

$$\Delta S = \arccos \left(\frac{\vec{p}_T(\mu, E_T) \cdot \vec{p}_T(j_1, j_2)}{|\vec{p}_T(\mu, E_T)| \cdot |\vec{p}_T(j_1, j_2)|} \right)$$

$\Delta S \sim \text{random}$



W boson and dijet system balance each other $\rightarrow \Delta S \sim \pi$



Relative p_T balance

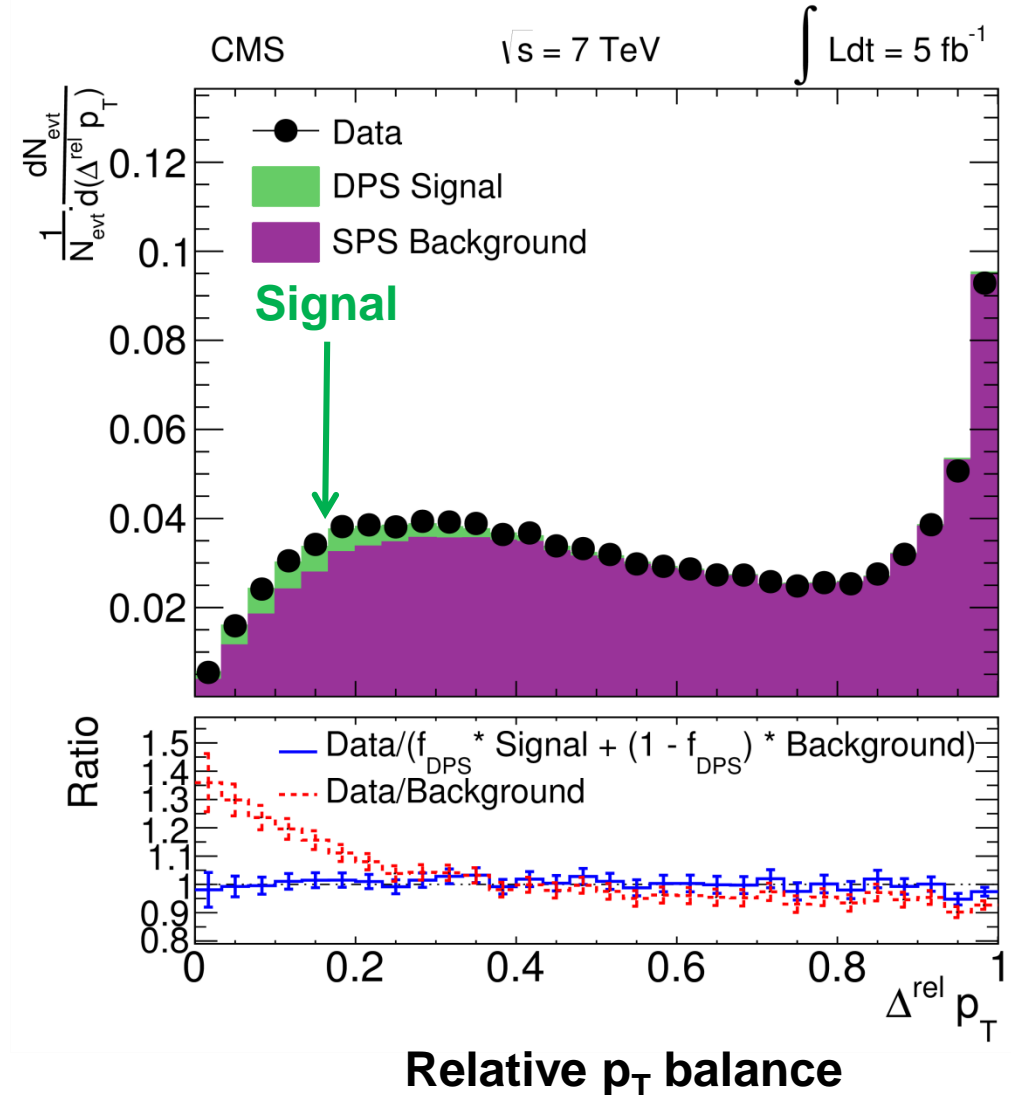
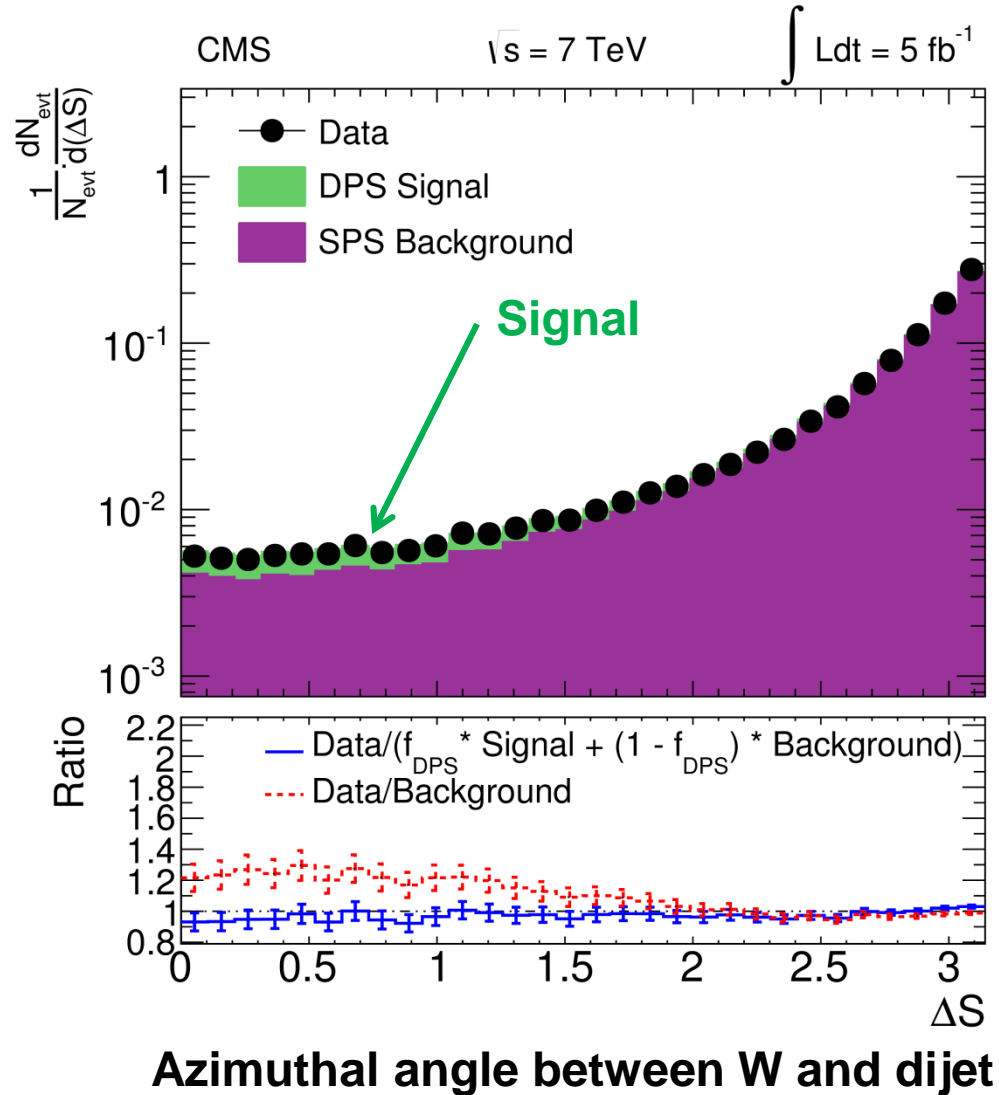
$$\Delta^{\text{rel}} p_T = \frac{|\vec{p}_T(j_1) + \vec{p}_T(j_2)|}{|\vec{p}_T(j_1)| + |\vec{p}_T(j_2)|}$$

Jets balance each other $\rightarrow \Delta^{\text{rel}} p_T$ small

$\Delta^{\text{rel}} p_T$ large



Signal and Background Distributions

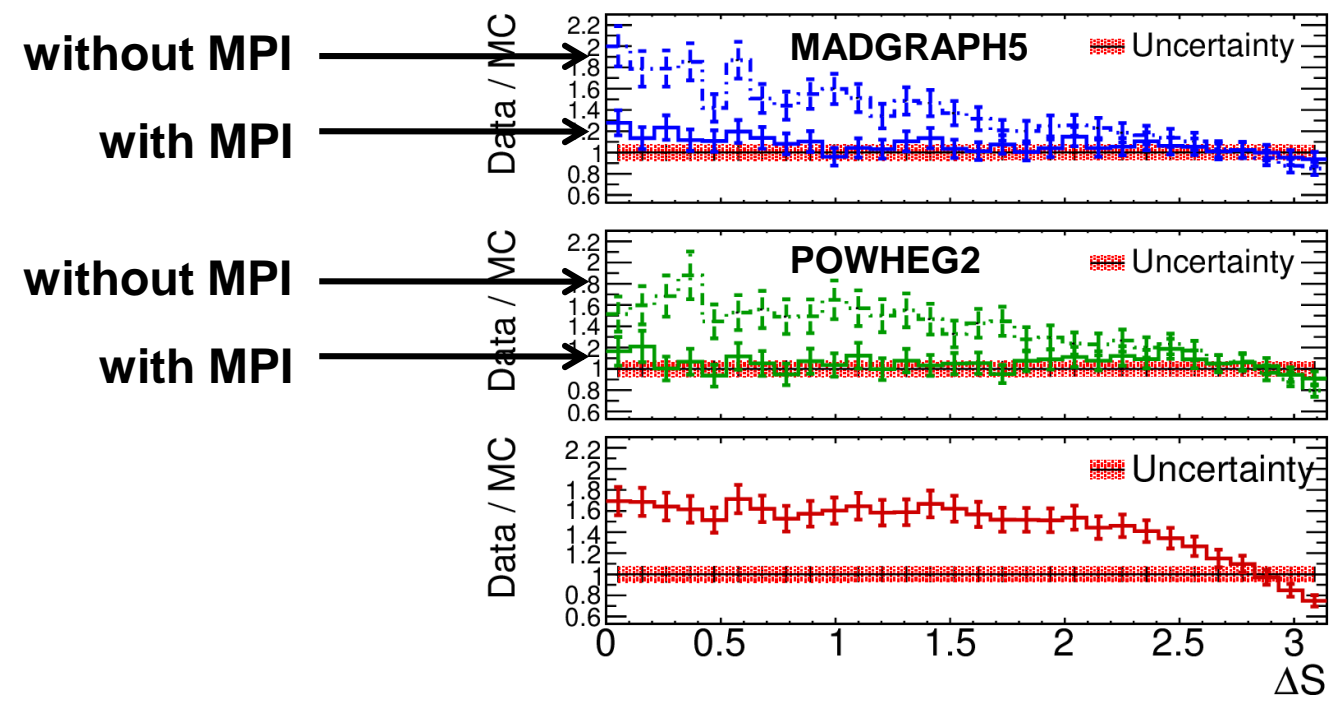
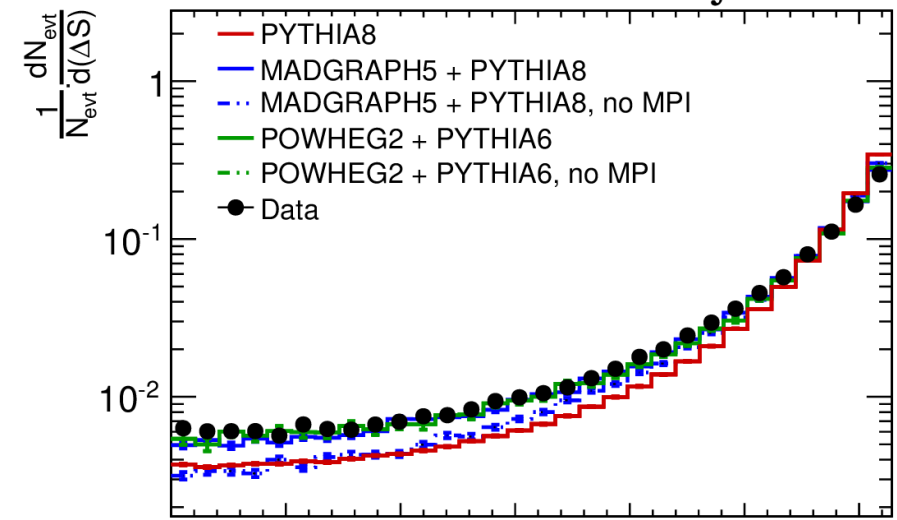




Influence of MPI

- Correct description of ΔS and $\Delta^{\text{rel}} p_T$
 - requires higher-order diagrams
 - inclusion of MPI

CMS $\sqrt{s} = 7 \text{ TeV}$ $\int Ldt = 5 \text{ fb}^{-1}$



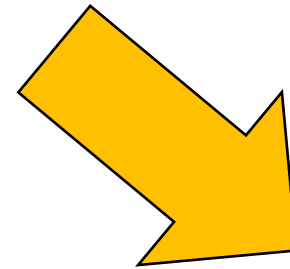
JHEP 03 (2014) 032

Extraction Method

$$\sigma_{eff} = \frac{\sigma_i \sigma_j}{\sigma_{ij}} = \frac{\sigma_{W+0jets} \sigma_{2jets}}{\sigma_{W+2jets}^{DPS}} = \frac{N_{W+0jets} \sigma_{2jets}}{N_{W+2jets}^{DPS}} = \frac{R}{f_{DPS}} \sigma_{2jets} \longrightarrow 0.0409 \text{ mb}$$

$$R = \frac{N_{W+0jets}}{N_{W+2jets}} \longrightarrow 27.8$$

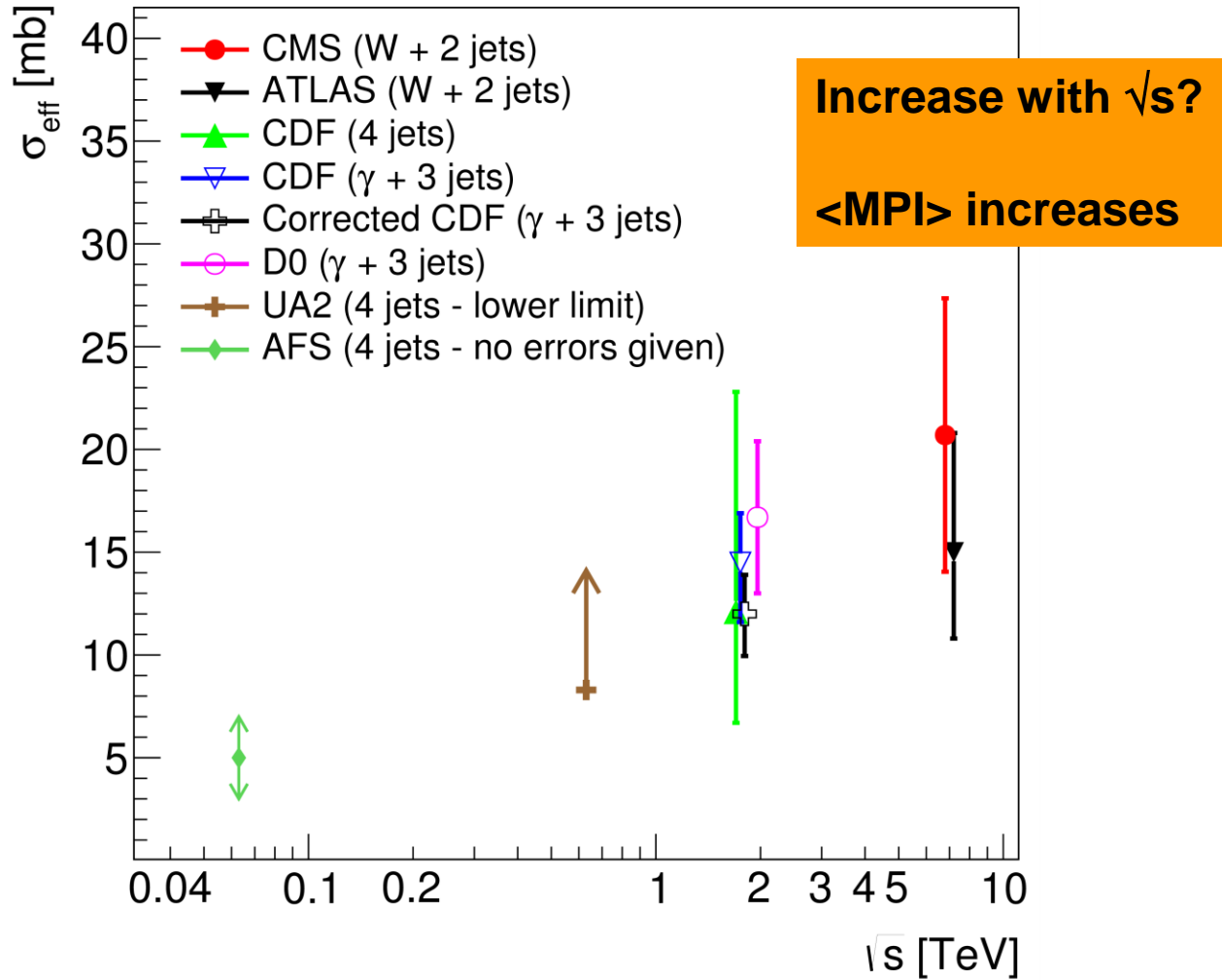
$$f_{DPS} = \frac{N_{W+2jets}^{DPS}}{N_{W+2jets}} \longrightarrow 0.055$$



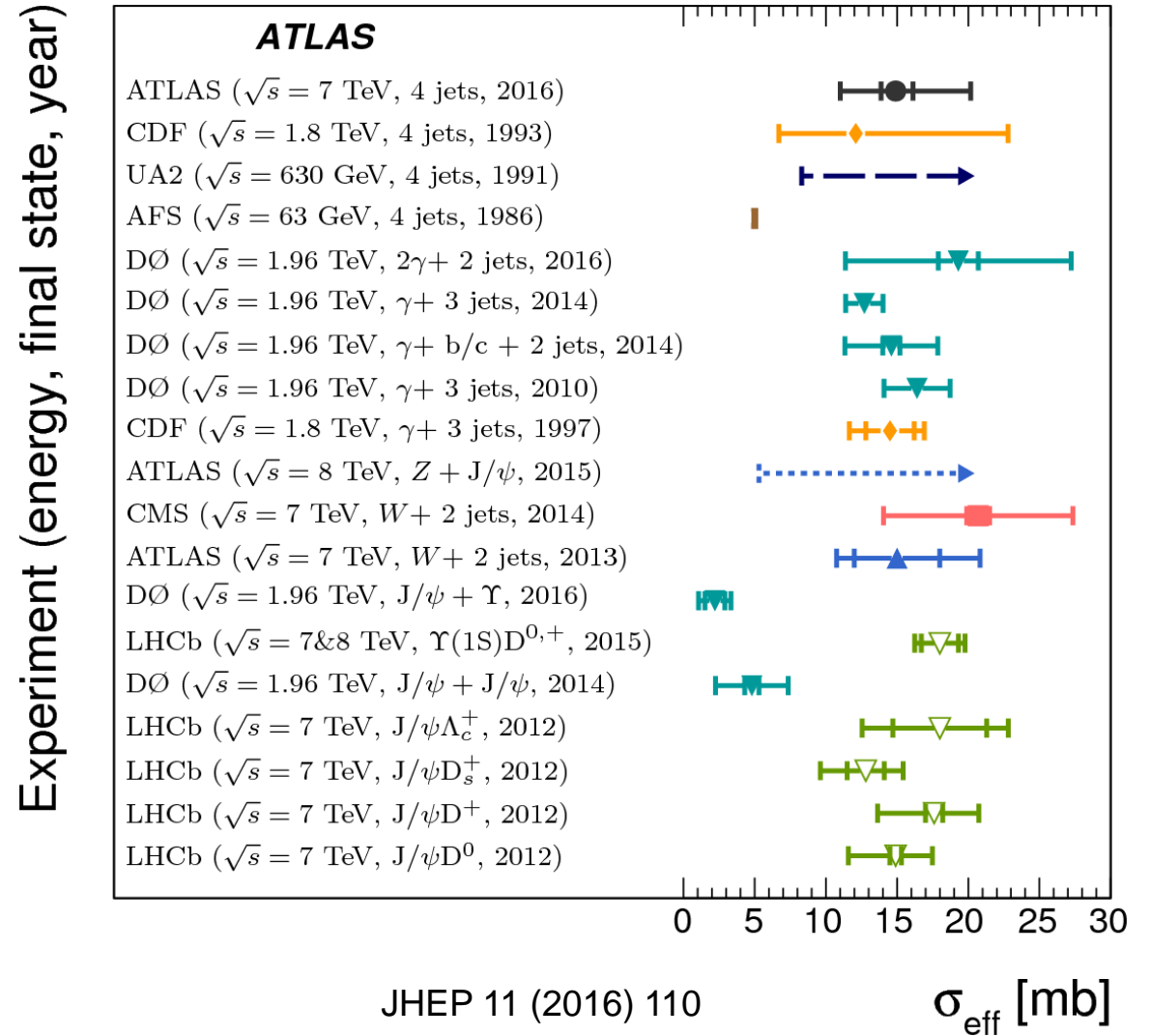
$\sigma_{eff} = 20.7 \pm 0.8 \text{ (stat.)} \pm 6.6 \text{ (syst.) mb}$



\sqrt{s} Dependence



JHEP 03 (2014) 032



JHEP 11 (2016) 110



Summary

Hard Double Parton Scattering

- Double parton scattering measures the probability that two processes occur in the one collision in different parton scatterings
 - Quantified by σ_{eff}
- Irreducible background of higher-order diagrams
 - Diagram contains both processes within one parton scattering



Multiplicity Biases



Bias?

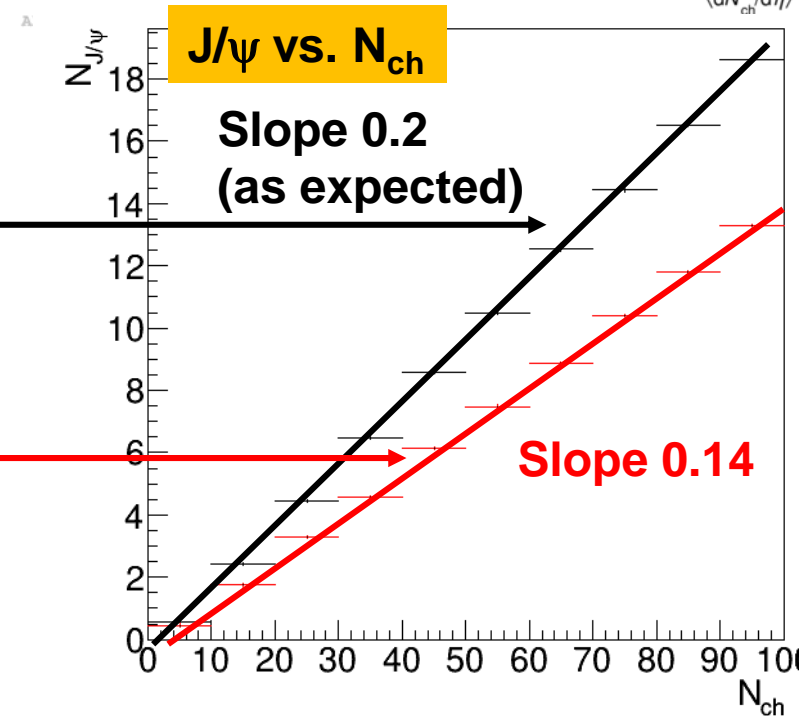
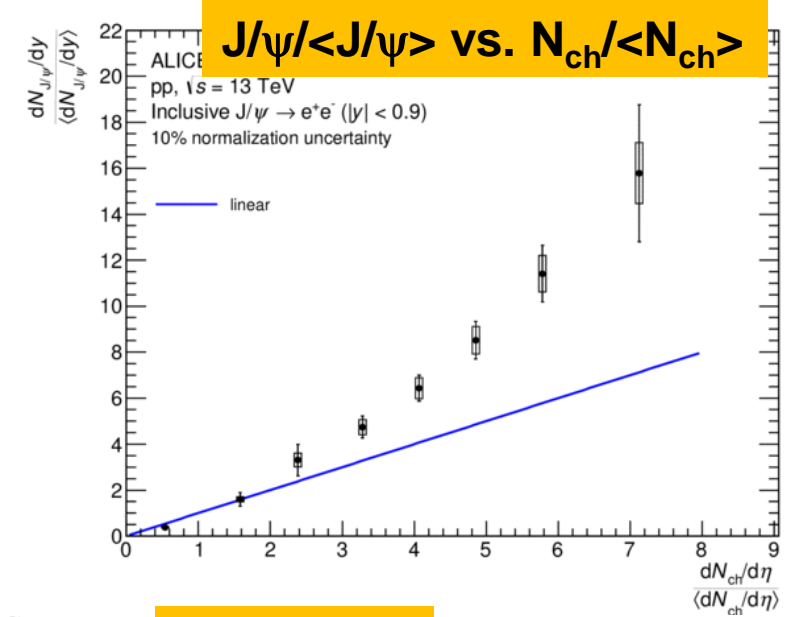


- Many observables measured as a function of multiplicity
- Can we consider the multiplicity independent from the studied process?
 - Independent = only characterization of the event activity
 - Correlation between multiplicity and studied process only indirectly through event activity
- Let's discuss two aspects
 - What biases can occur when multiplicity is used to slice events into classes
 - How are these biases related to MPI



Bias!

- We discussed J/ψ vs. N_{ch} measurement
- Imagine simple (unphysical) picture
 - Random number of particles
 - Per particle probability of producing J/ψ is 20%
 - Variant: Per produced J/ψ add 2 particles
 - Slope drastically changed

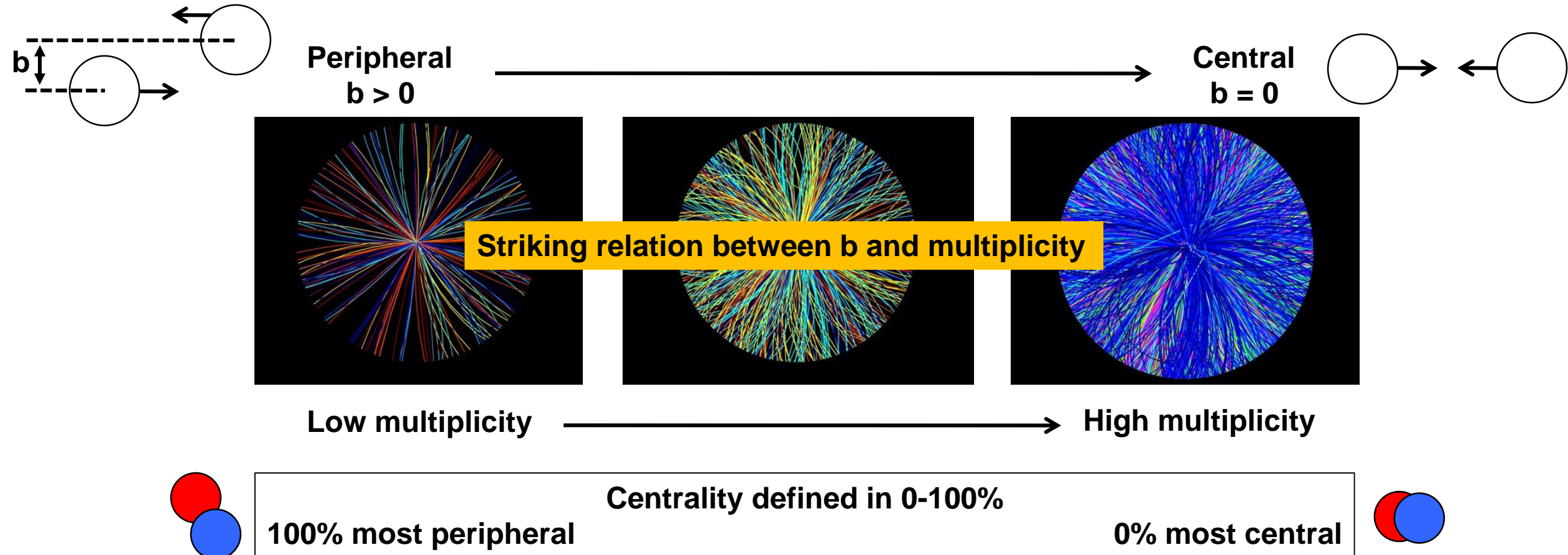




Concept: Centrality

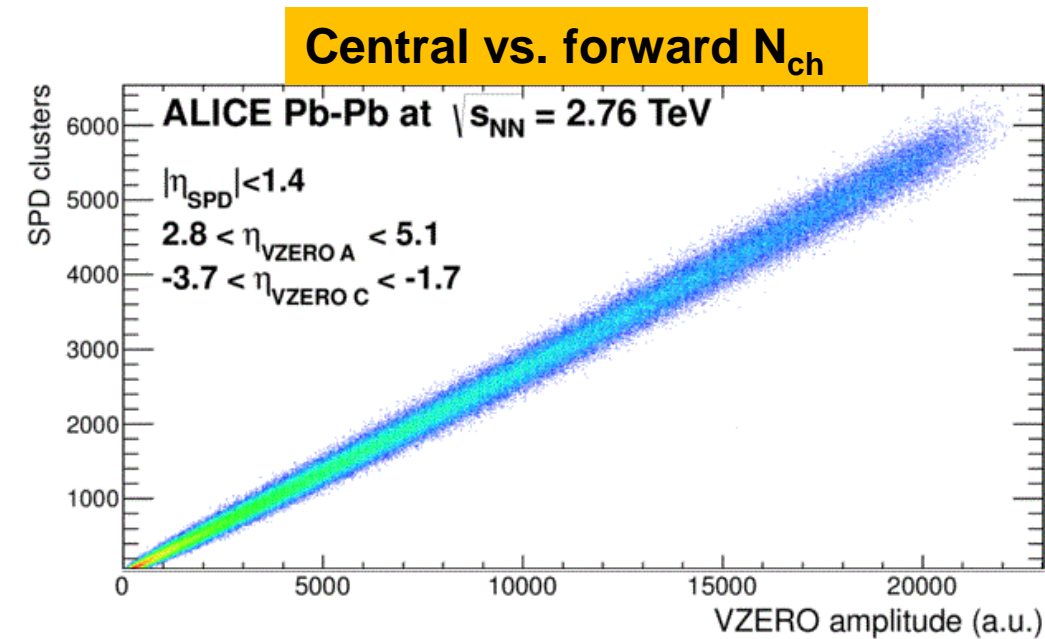
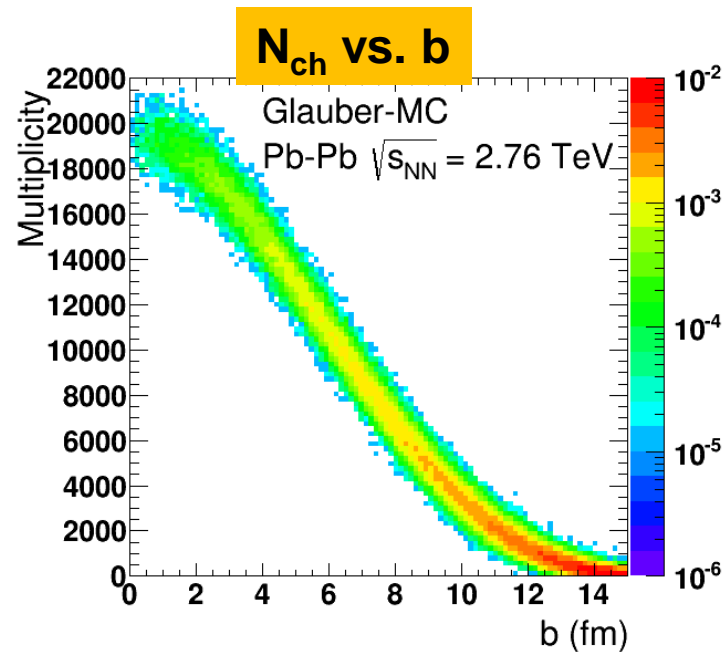
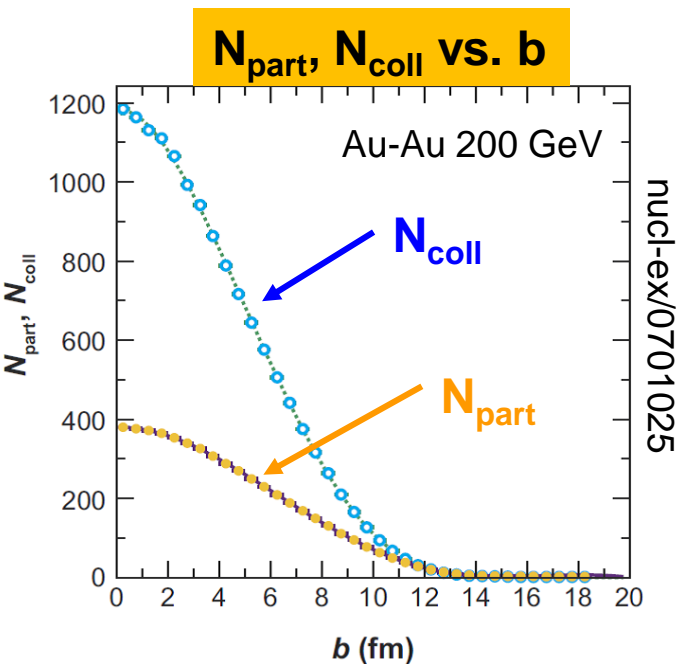
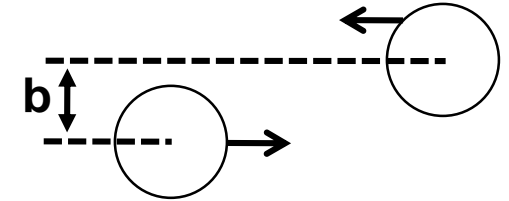
Short excursion to heavy-ion physics

- Overall activity and multiplicity depends on nuclear overlap



Large Systems: Pb-Pb

- Multiplicity depends on participants nucleons N_{part}
 - N_{part} depends on collision impact parameter b
- Clear correlation between multiplicity and b
- Correlation correlated across phase space



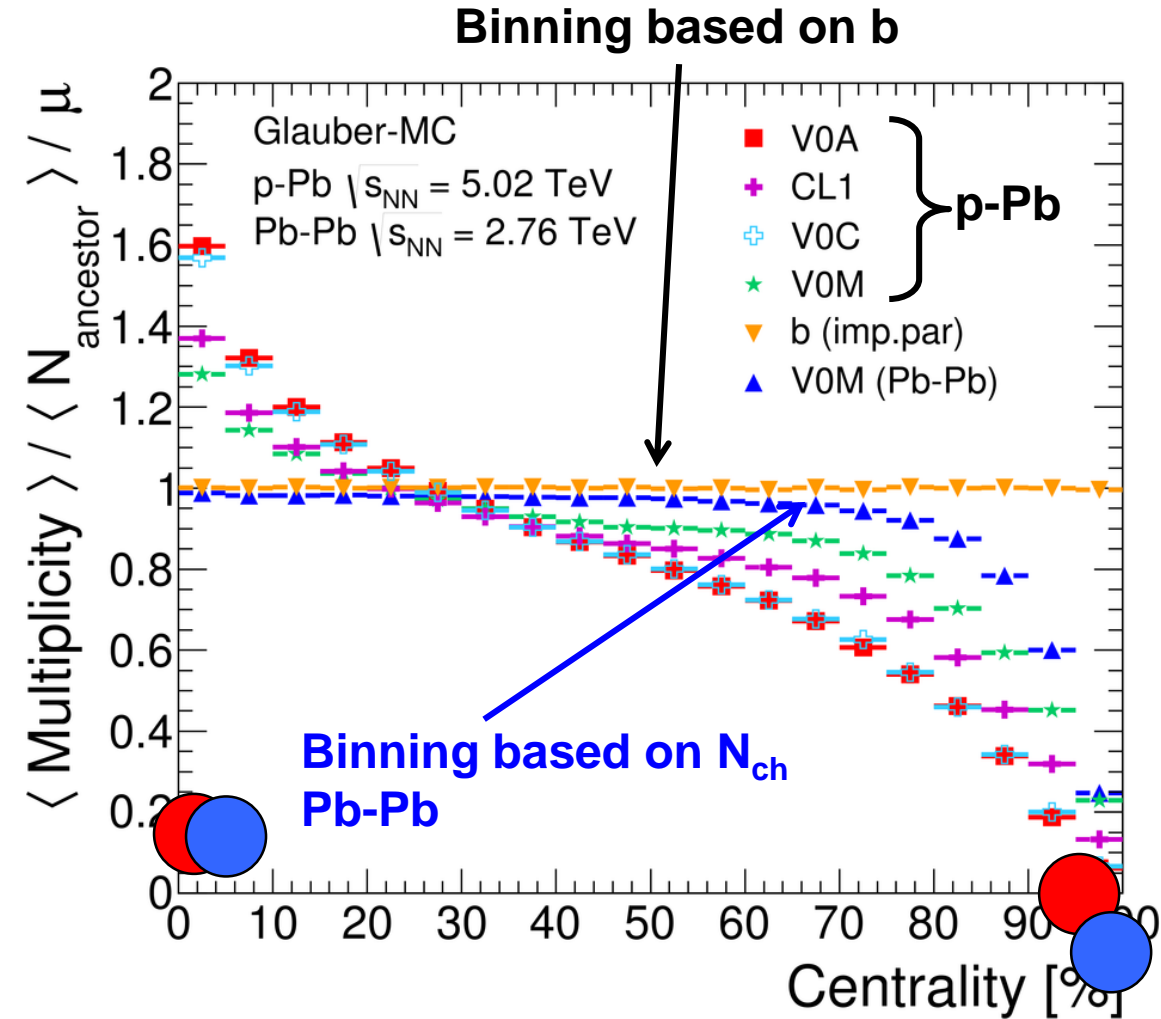
Large Systems: Pb-Pb

- Can the multiplicity stemming from each N_{part} be treated independently?
- Tested within Glauber model

$$\frac{N_{ch} / N_{part}}{\mu}$$

$\mu = \text{average per } N_{part}$
 [in Glauber: $\langle N_{ch} \rangle$ per NBD]

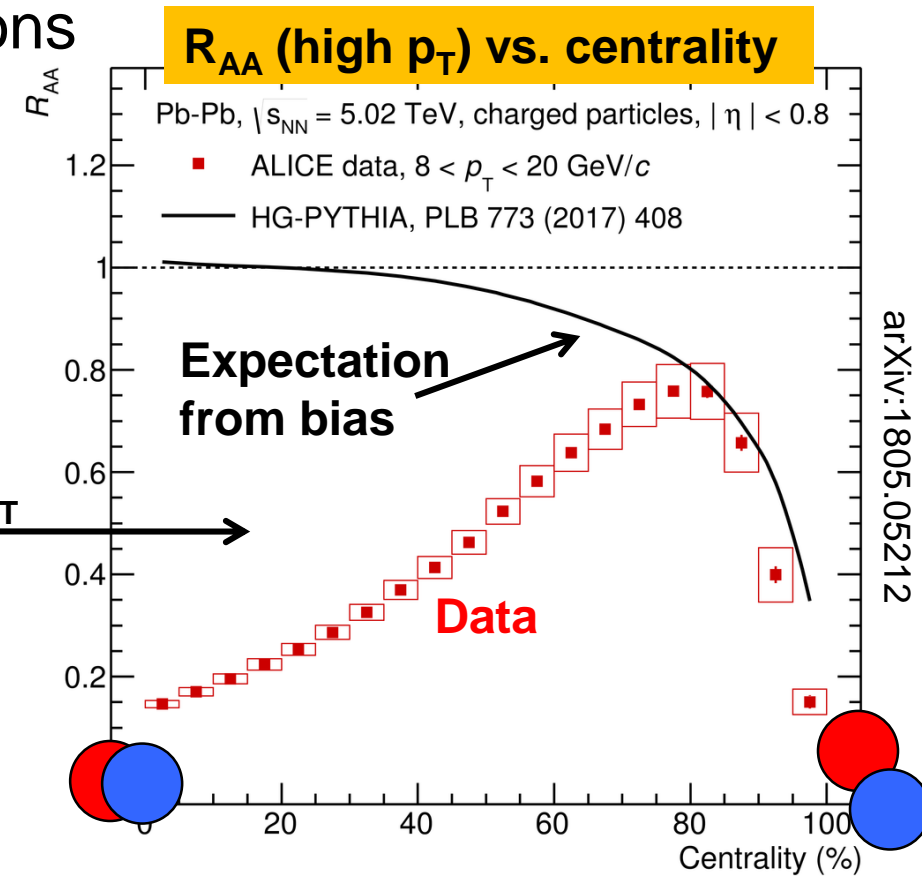
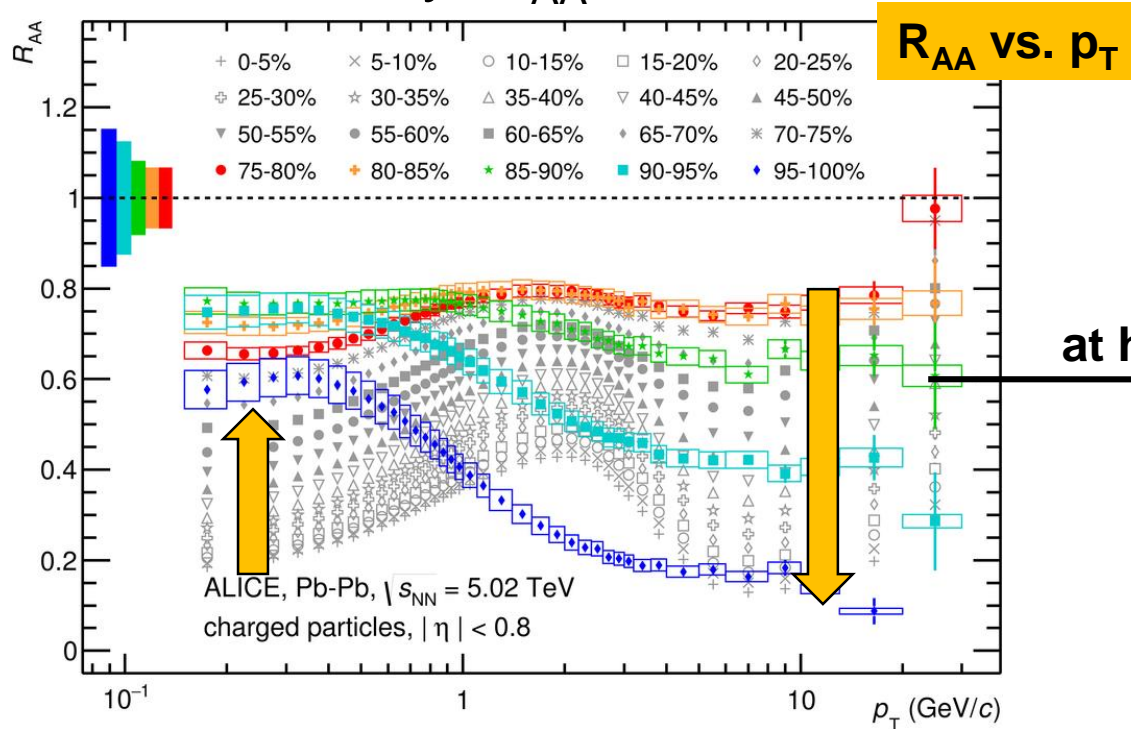
- Binning in $b \rightarrow$ unity
- Binning in N_{ch}
 - Unity for 0-70% centrality
 - Deviations for the 30% lowest multiplicity
- So called *multiplicity bias*



Consequence: R_{AA} in peripheral Pb-Pb

- Nuclear modification factor R_{AA} commonly used to quantify energy loss in the Quark-Gluon Plasma
- Multiplicity bias distorts signal in peripheral collisions
- Above 80% centrality, R_{AA} decreases due to bias

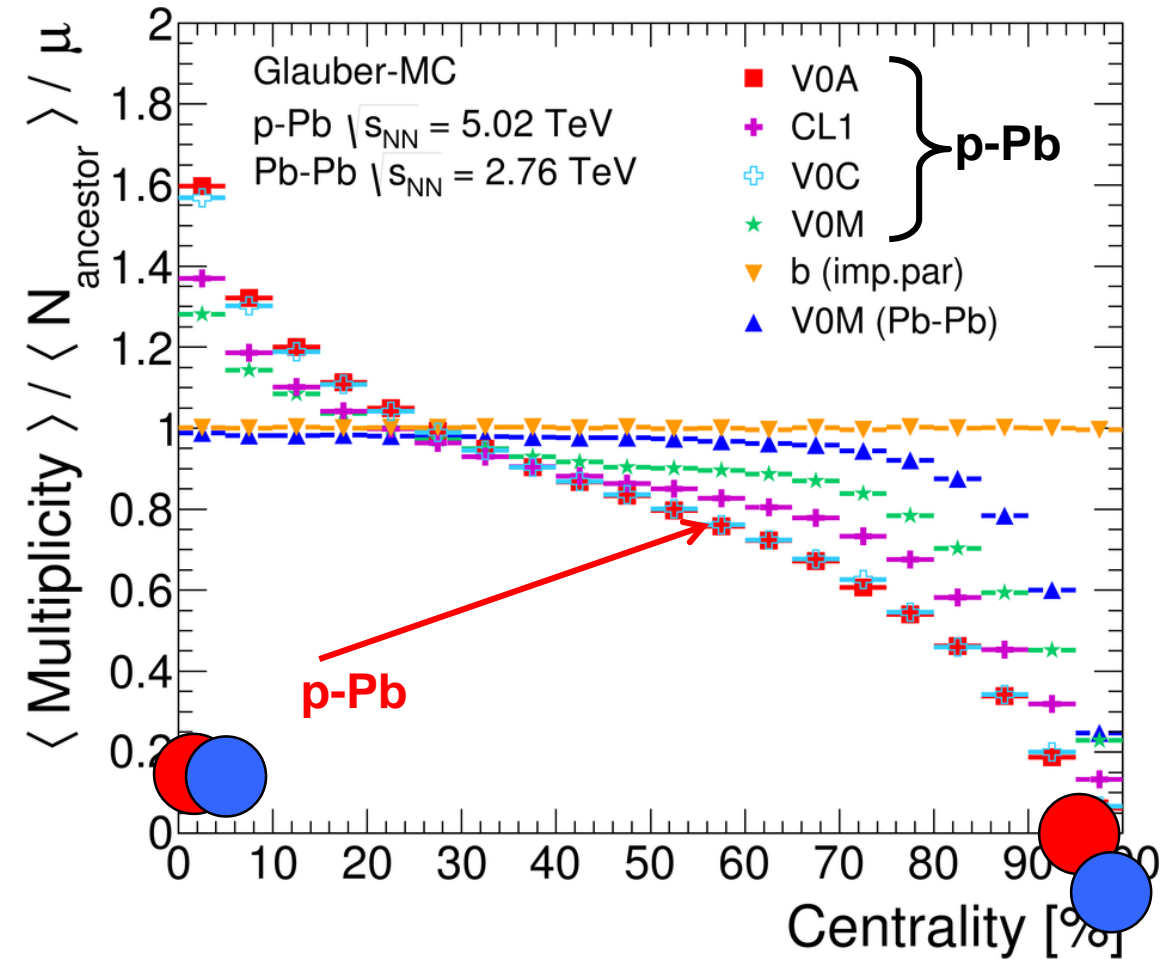
$$R_{AA} = \frac{dN_{AA} / dp_T}{\langle N_{coll} \rangle dN_{pp} / dp_T}$$





Intermediate Systems: p-Pb

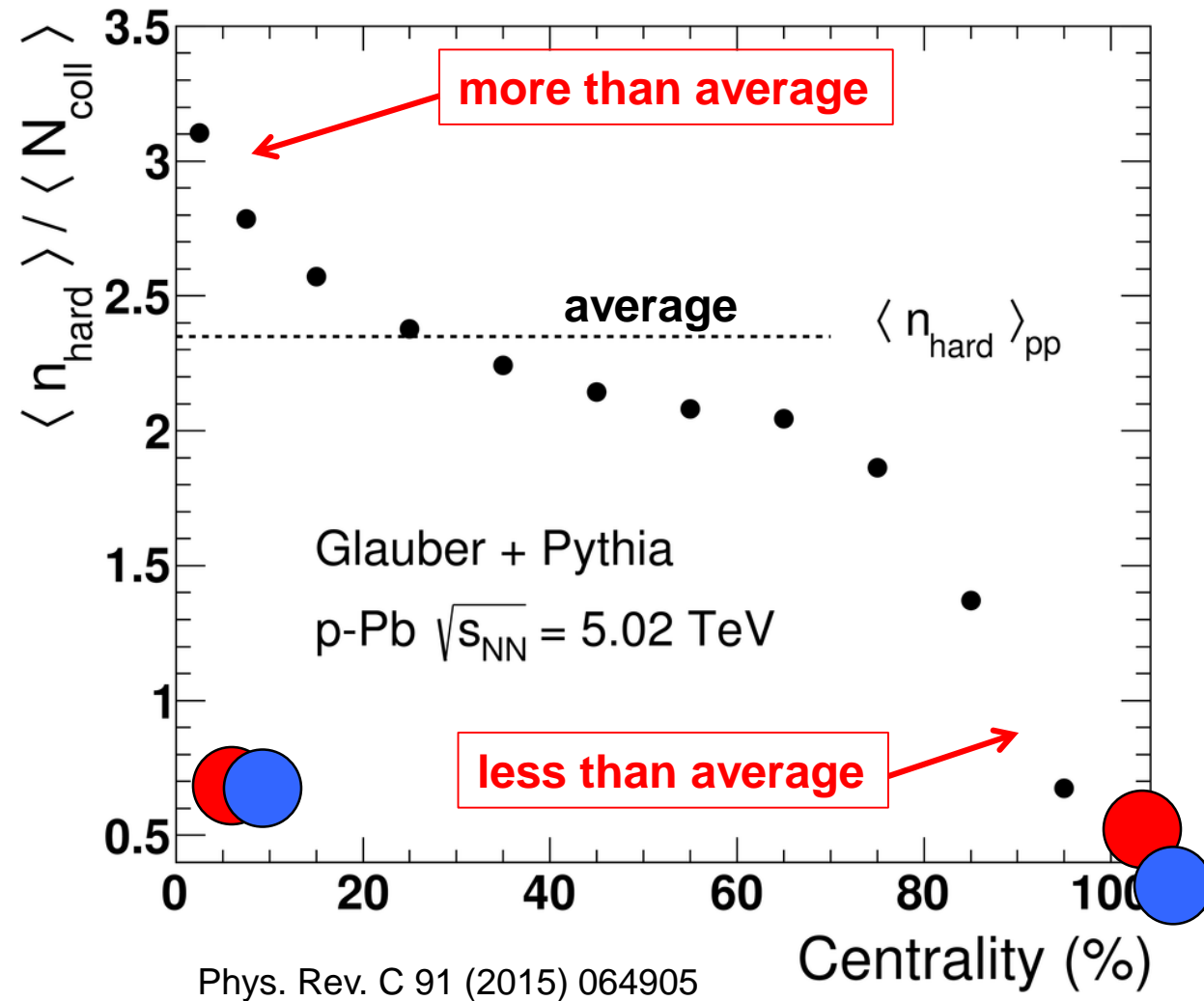
- Less participating nucleons
→ larger biases
(8 in p-Pb vs. 110 in Pb-Pb)
- Multiplicity bias at all centralities



Phys. Rev. C 91 (2015) 064905

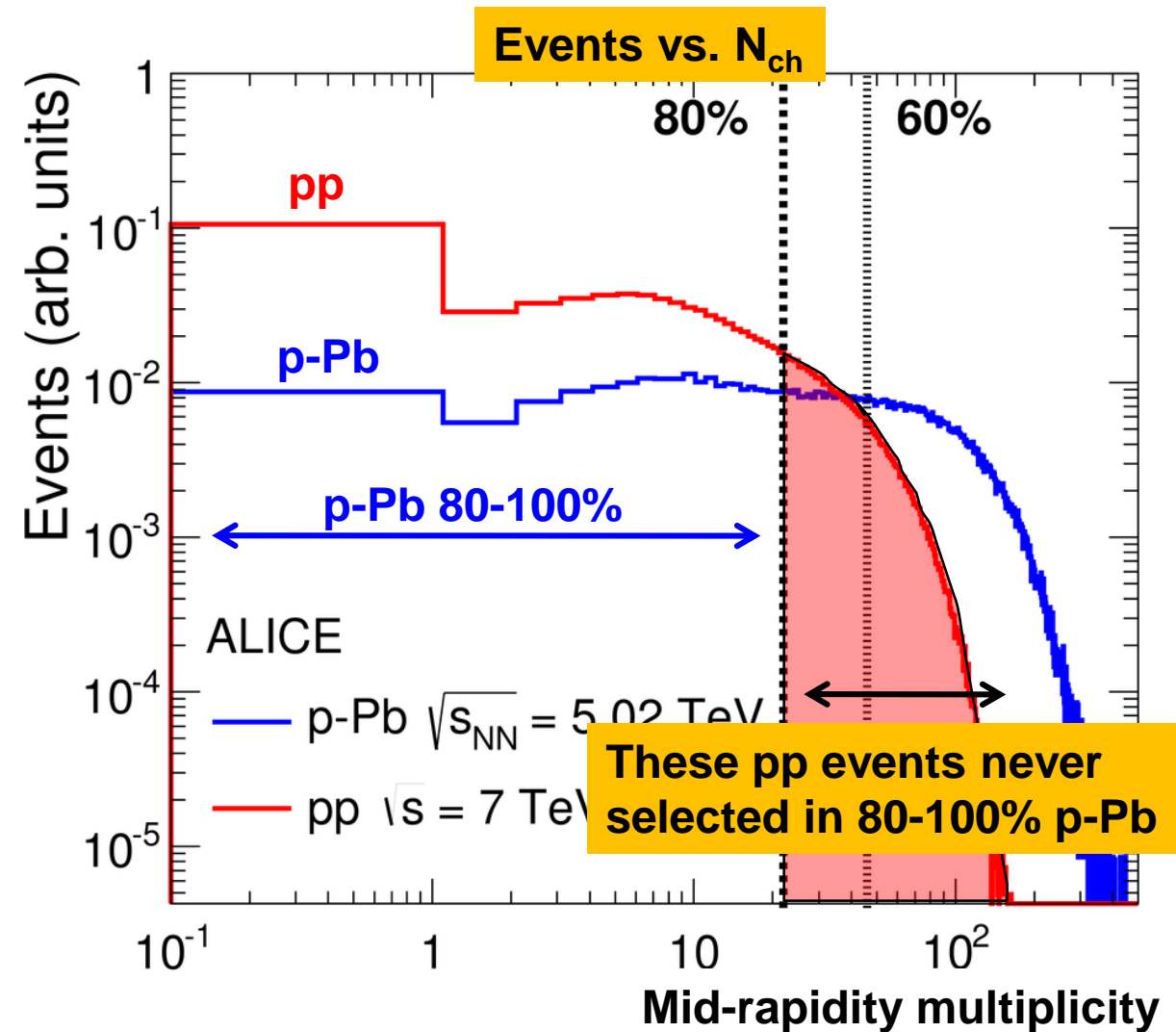
Intermediate Systems: p-Pb

- Couple Glauber and PYTHIA
- Calculate #MPI per NN collision
- Significant deviations from average
- Clear bias
→ bias on N_{ch} , hard yields, ...



Intermediate Systems: p-Pb

- High p_T particles are produced only in high Q^2 processes
 - High $Q^2 \rightarrow$ high N_{ch} (on average)
 - Introduces trivial correlation
- Low multiplicity selections are depleted of such processes
 - High p_T yields reduced at low N_{ch}
- *Jet-veto bias*



Phys. Rev. C 91 (2015) 064905

Intermediate Systems: p-Pb

- Nucleon-nucleon impact parameter b_{NN}
 - Increases in peripheral collisions \rightarrow less MPI
 - Decreases in central collisions \rightarrow more MPI

Geometrical bias

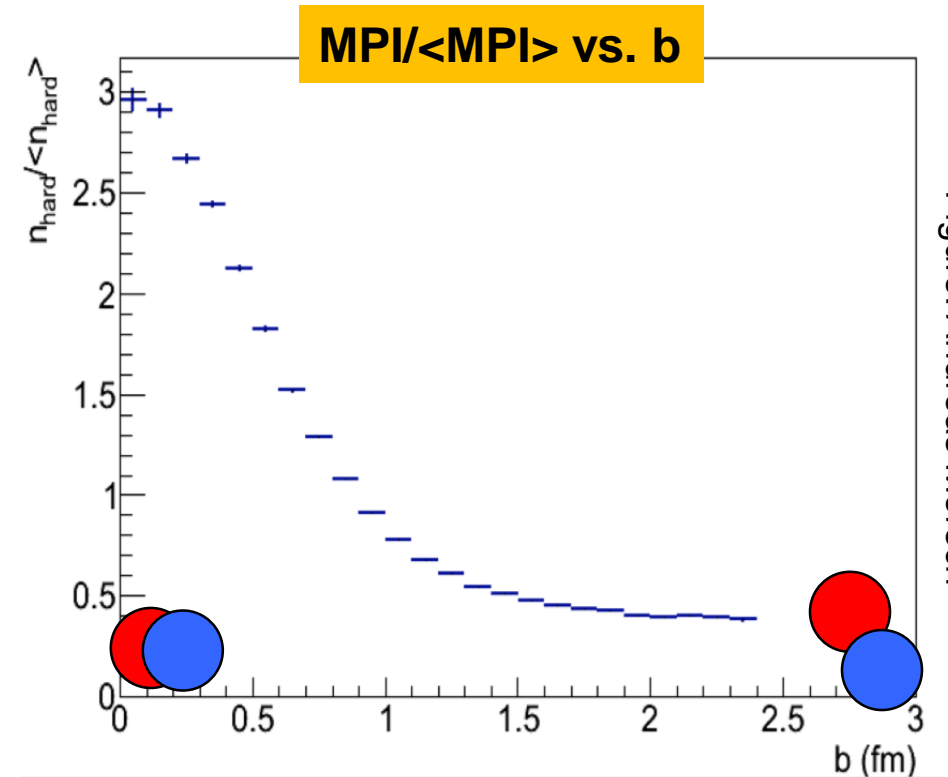
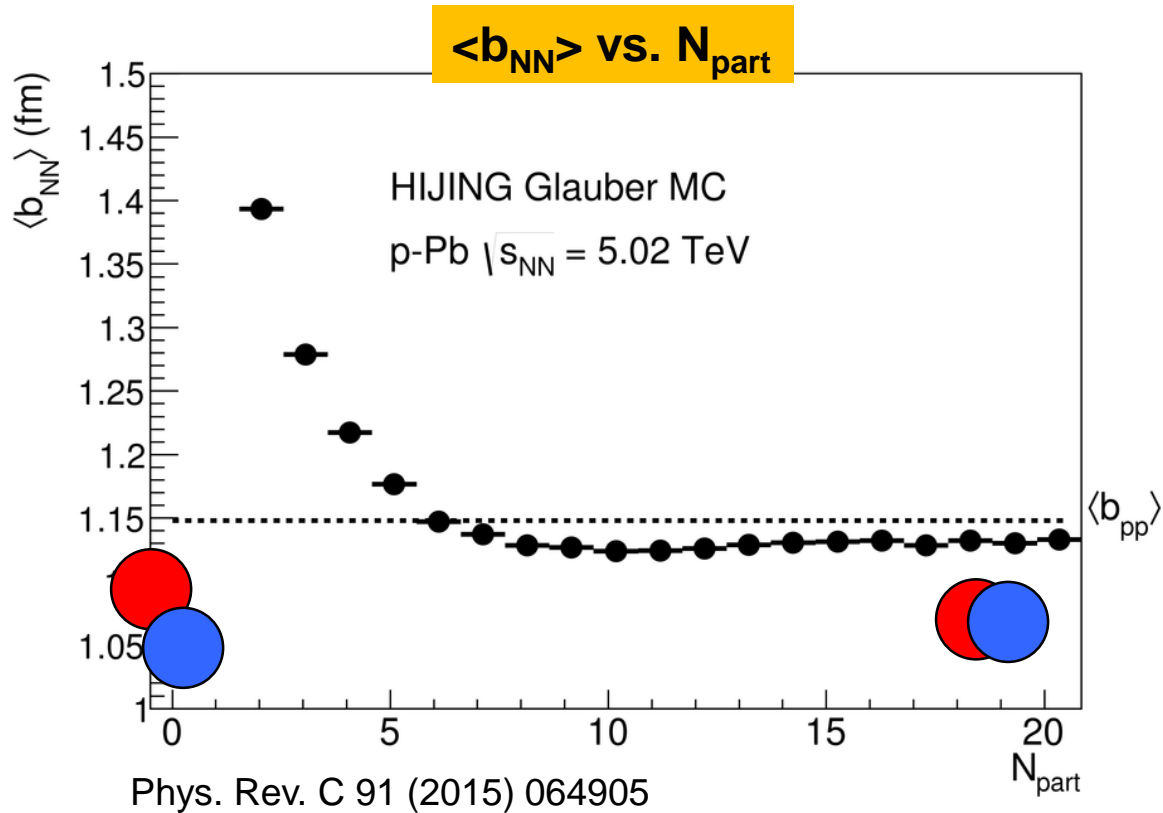


Figure: Andreas Morsch

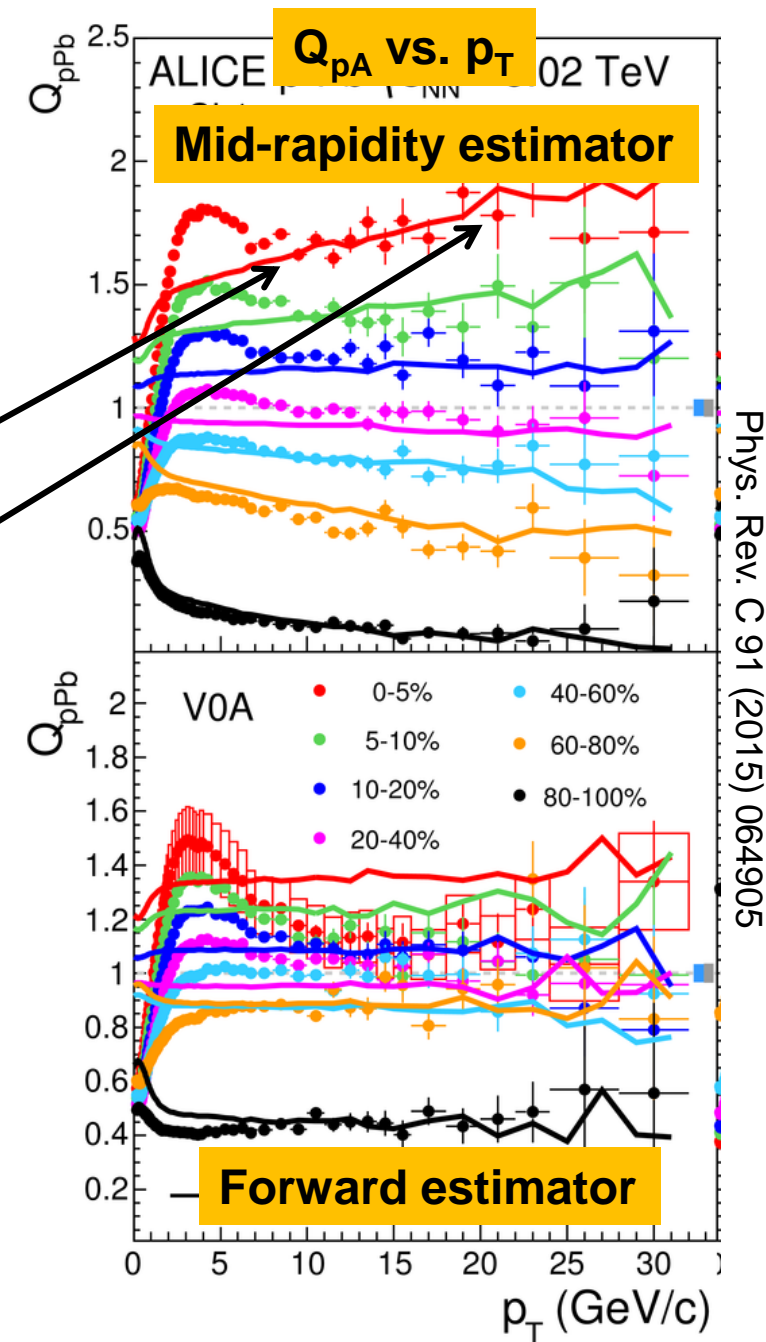


Consequence: R_{pA} in p-Pb

- R_{pA} usually sensitive to energy loss
 - Distorted by these biases
- Effect depends on centrality estimator used
 - The larger the separation between estimator and measurement, the smaller the biases
- No measurement without considering these biases
 - Due to estimator dependence R_{pA} renamed to Q_{pA}

Model estimating bias

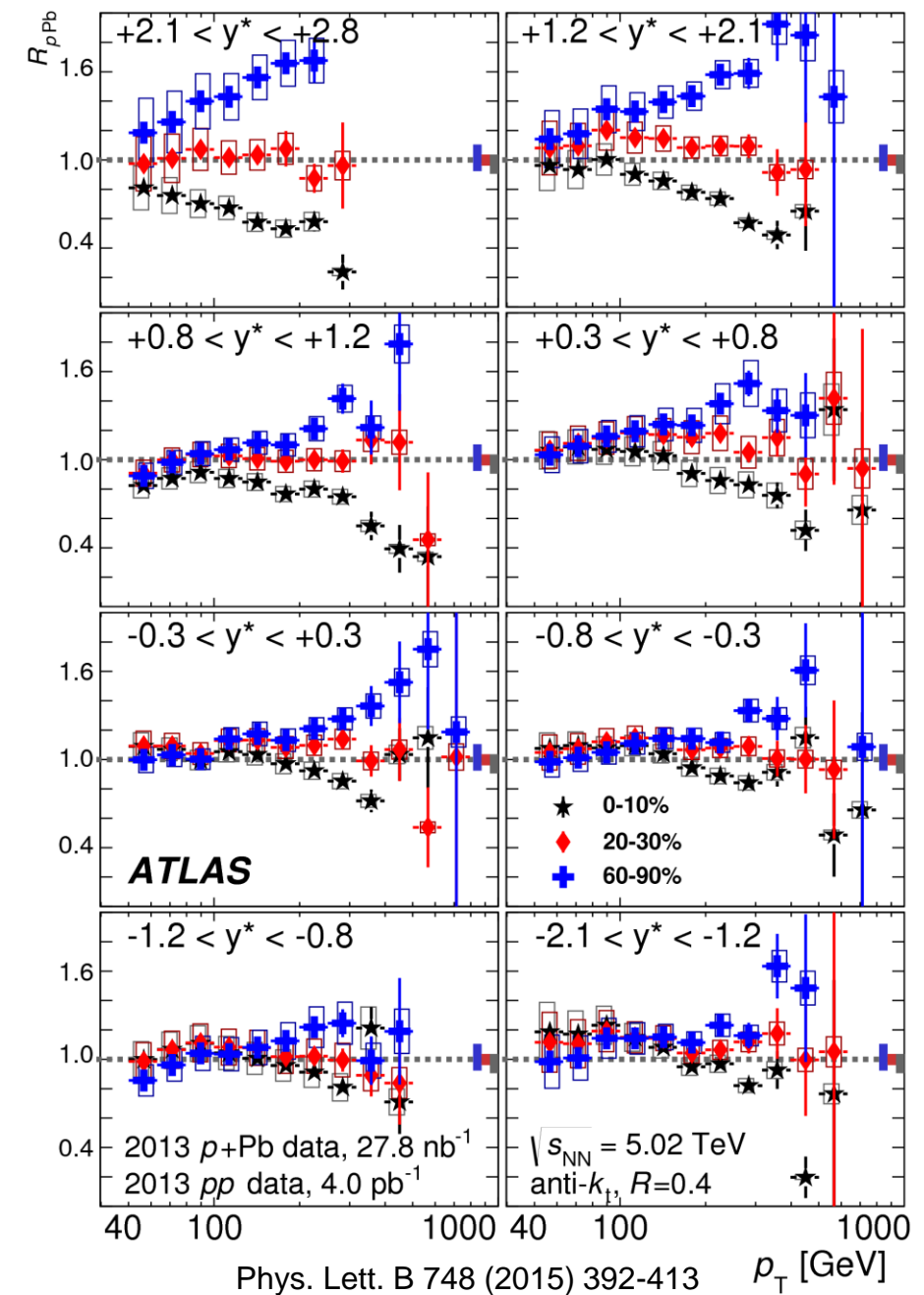
Data





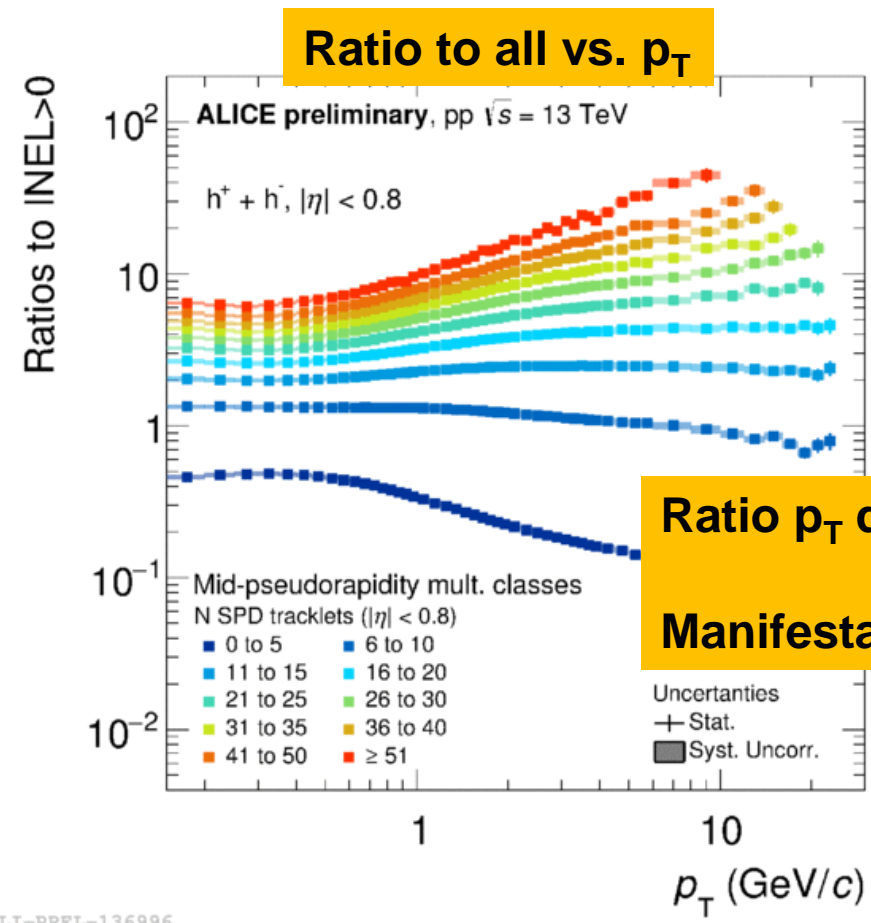
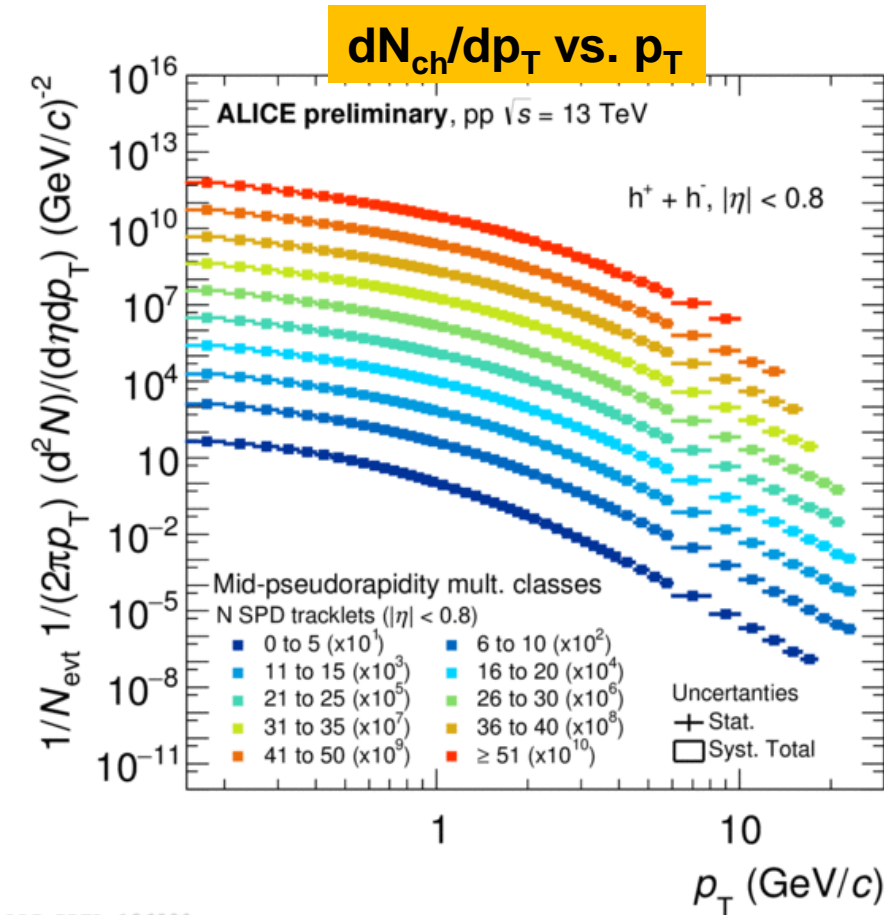
Consequence: R_{pA} in p-Pb

- Similar bias for R_{pA} of reconstructed jets
- Rapidity dependence clearly visible



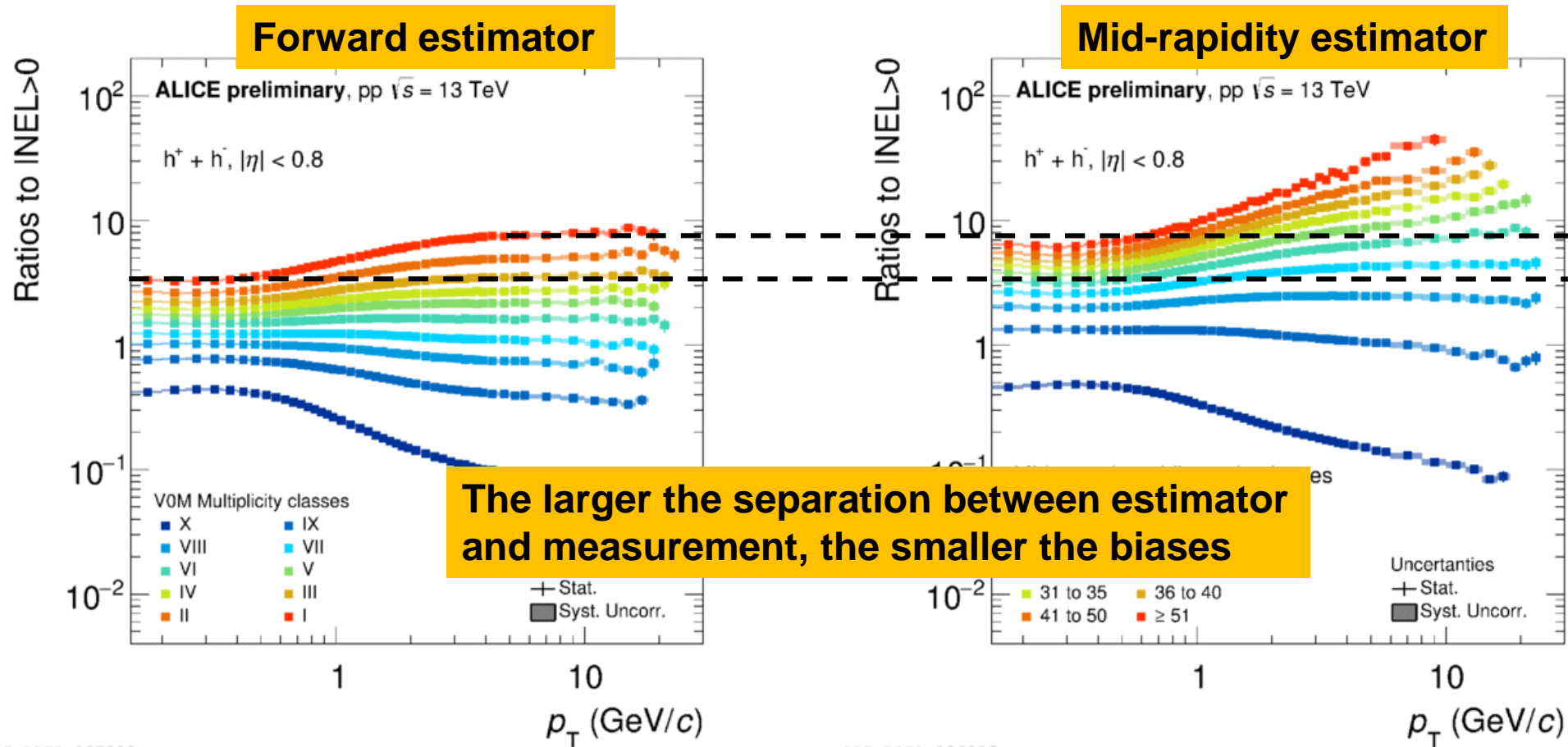
Small Systems: pp

- Charged-particle spectra in multiplicity bins



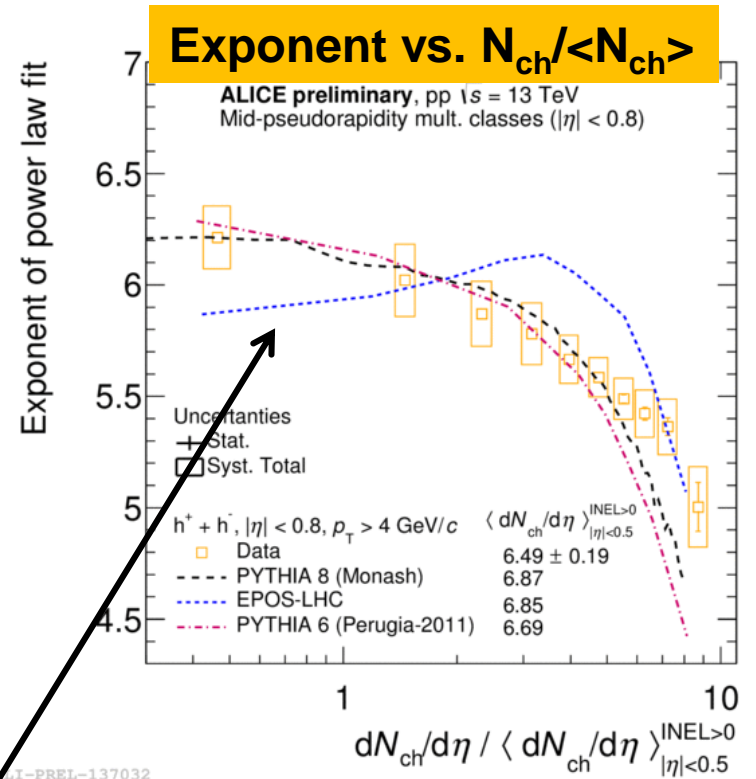
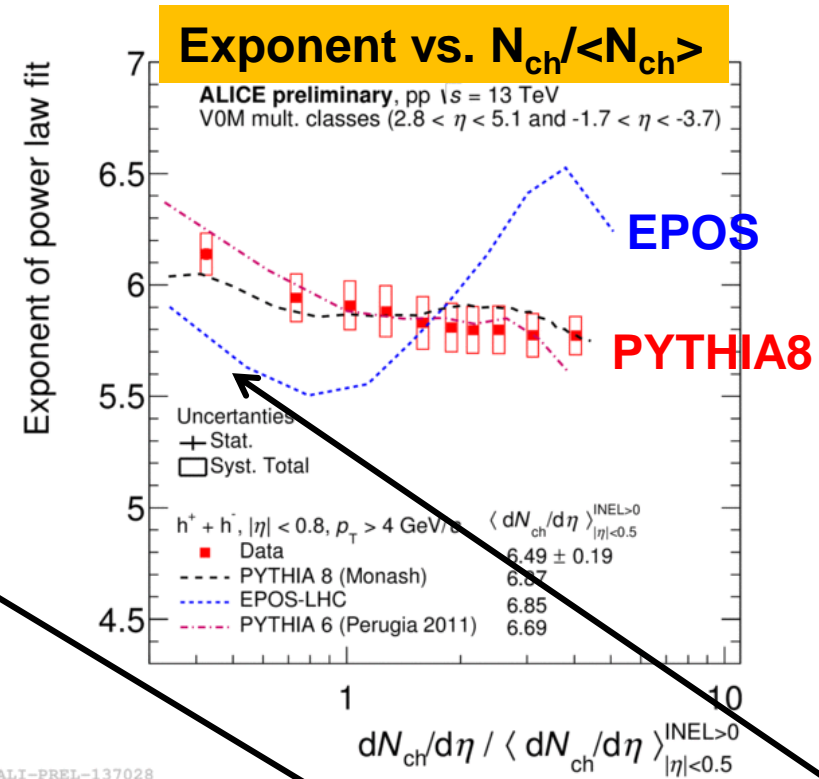
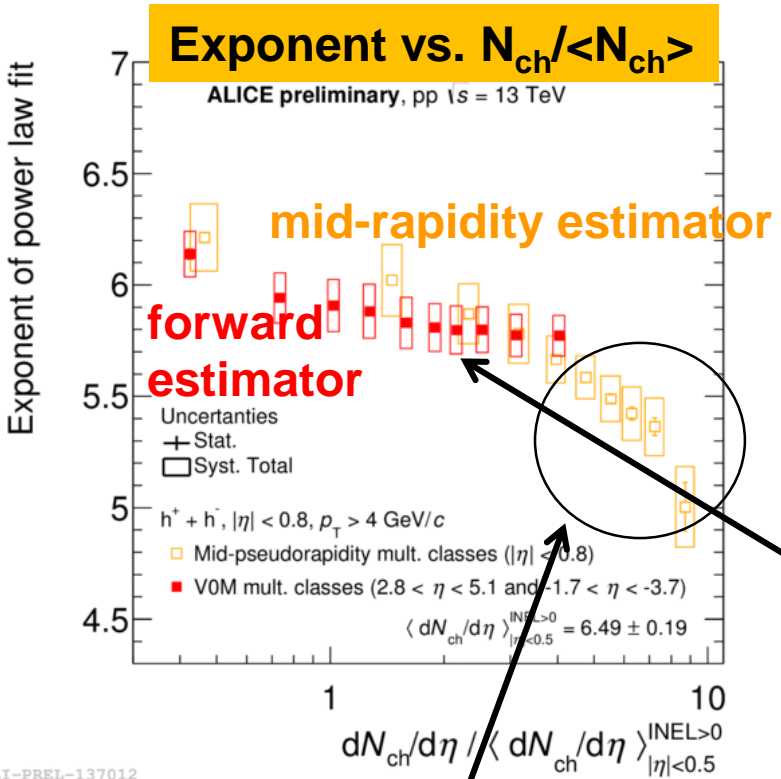
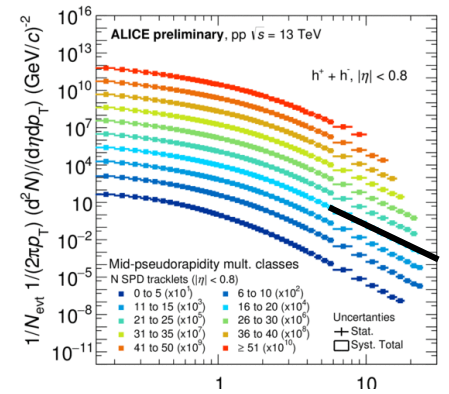
Small Systems: pp

- Charged-particle spectra in multiplicity bins



Small Systems: pp

- What is the high p_T shape evolution?
 - Quantified by power-law fit above 6 GeV/c



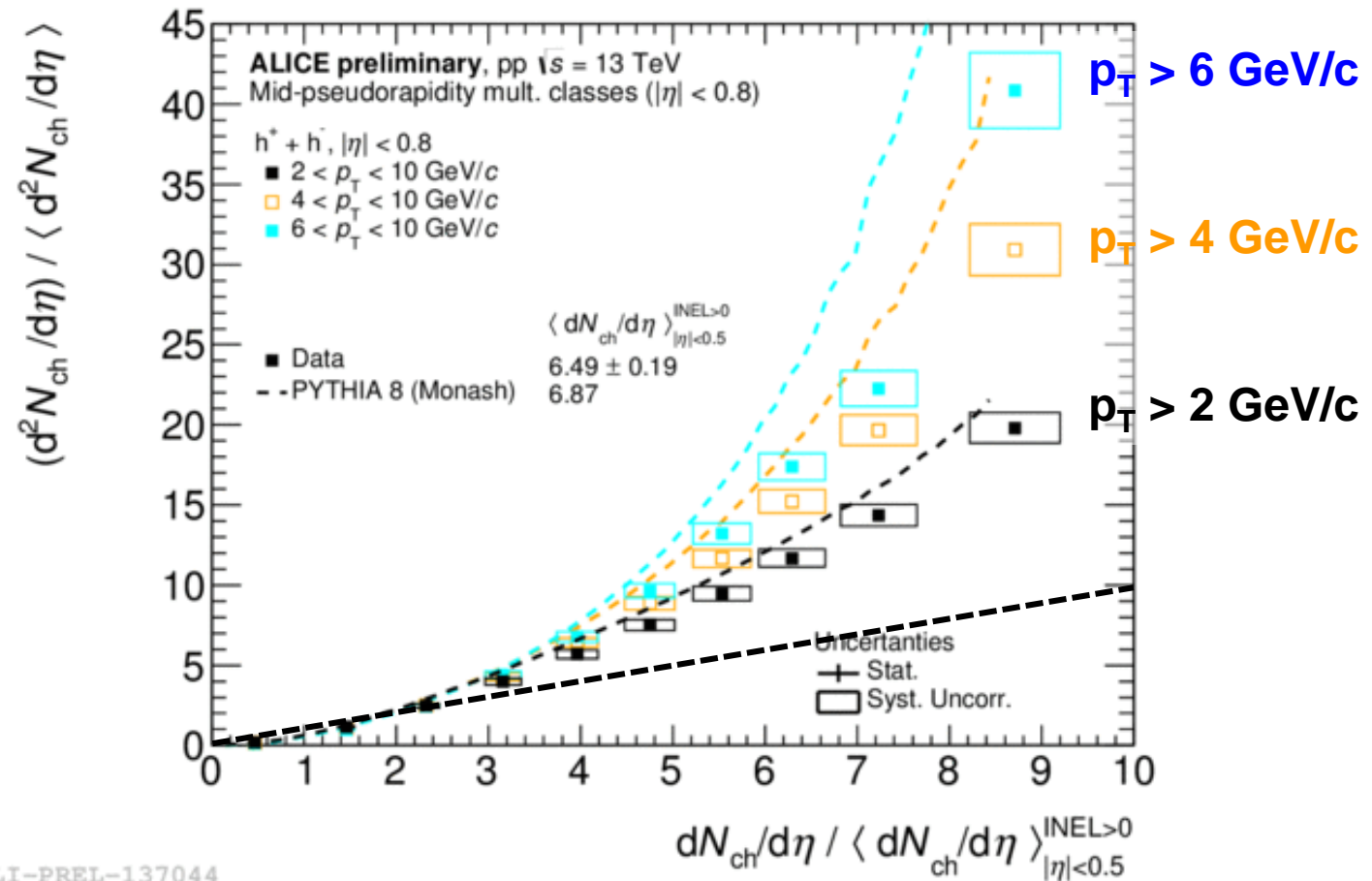
Dynamic range

Similar exponent in data ... not necessarily in MC

Small Systems: pp

- How do the high p_T yield scale with multiplicity?

- Significant growth
 - The larger the larger the p_T



ALI-PREL-137044



Summary

Multiplicity Biases

- Characterization of event activity with multiplicity is biased
 - Multiplicity bias, e.g. when desiring a selection in impact parameter but using multiplicity
 - Geometric bias, e.g. when high-multiplicity collisions select smaller-than-average nucleon-nucleon impact parameter
 - Jet-veto bias, e.g. low multiplicity disfavours large Q^2 processes
- In large systems like Pb-Pb present in peripheral collisions
- In medium systems like p-Pb present in all event classes
- In pp collisions omnipresent and crucial for interpretation



Collective Phenomena

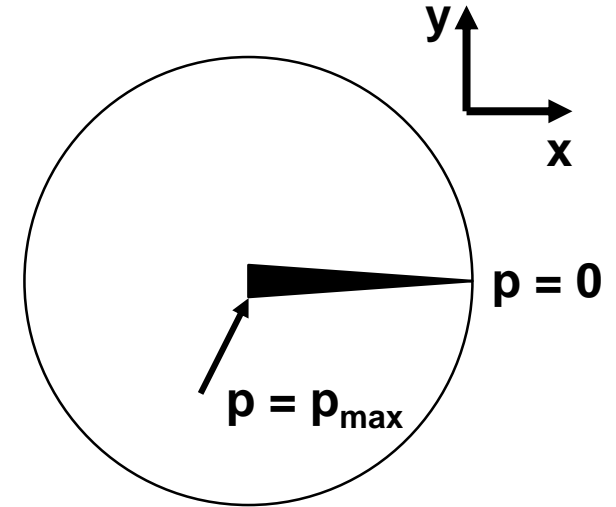
Expansion

Short excursion to heavy-ion physics

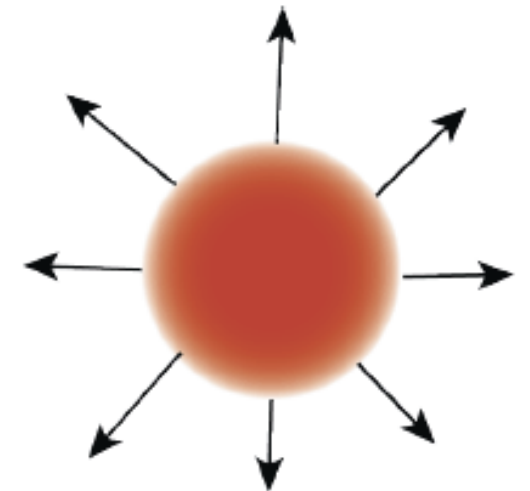
- After collision, QGP droplet in vacuum
- Energy density very high
- Strong pressure gradient from center to boundary

- Consequence: rapid expansion (“little bang”)
- Partons get pushed by expansion
 - Momentum increase

- Measurable in the transverse plane (p_T)
 - Called *radial flow*



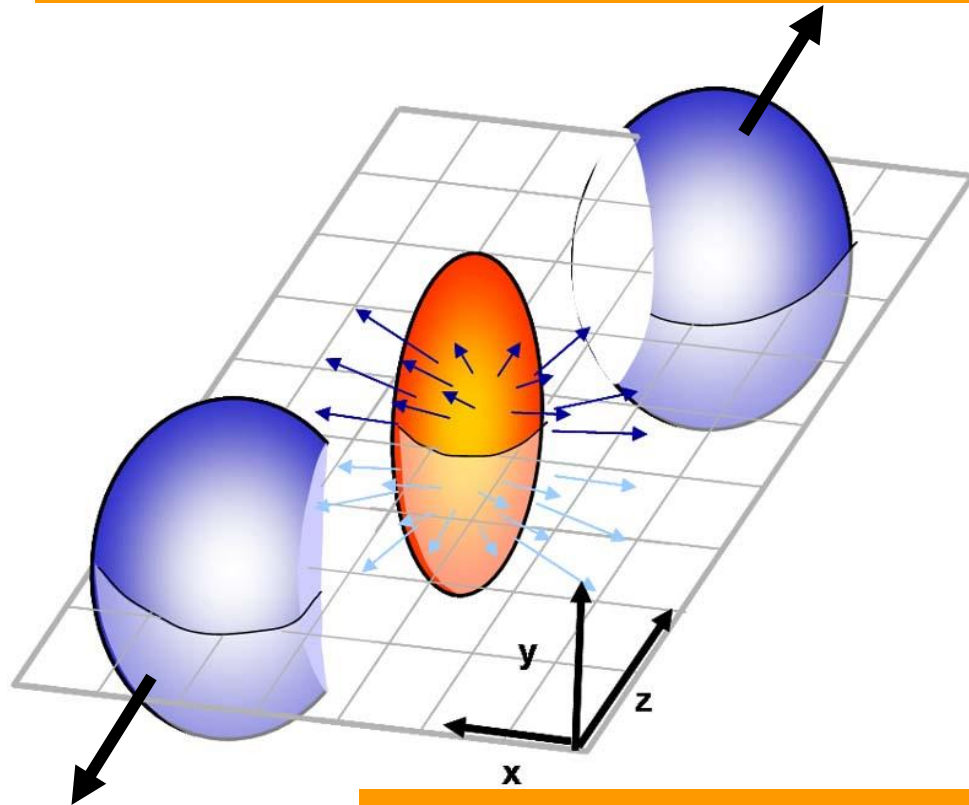
view in beam direction



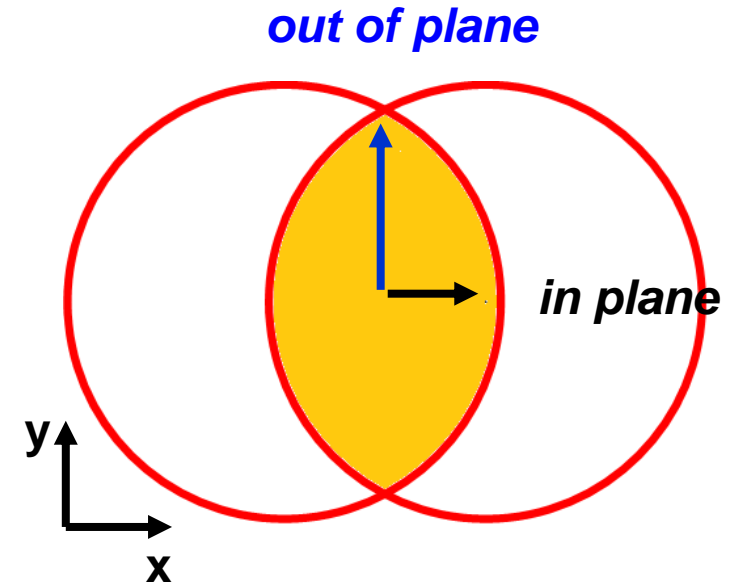
Elliptic Flow

Short excursion to heavy-ion physics

Overlap of colliding nuclei not isotropic in non-central collisions



Defines reaction plane Ψ_{RP}
(spanned by beam axis and impact parameter vector)



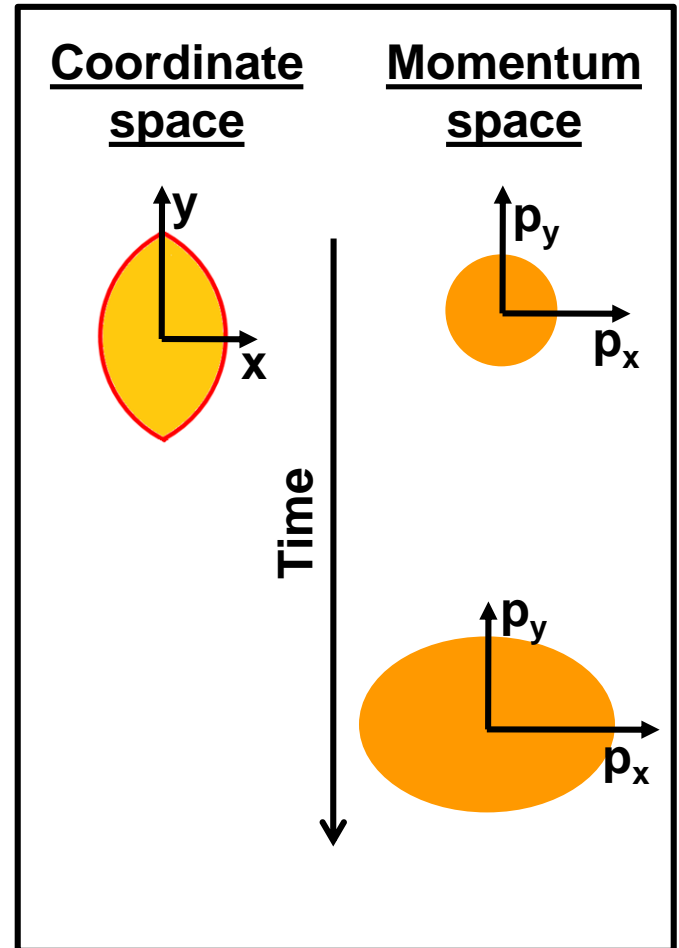
→ Pressure gradients dependent on direction

here: $\frac{dp_x}{dL} > \frac{dp_y}{dL}$

Anisotropy

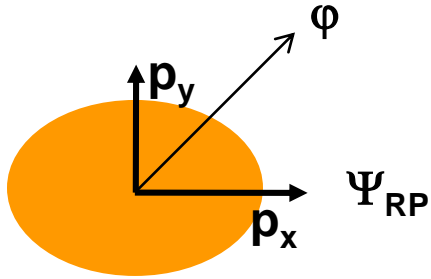
Short excursion to heavy-ion physics

- Spatial anisotropy (almond shape)
 - Quantified by eccentricity $\varepsilon = \frac{y^2 - x^2}{y^2 + x^2}$
- Pressure gradient larger in-plane
- Pressure pushes partons
 - More in in-plane than out-of-plane
- Spatial anisotropy converts into momentum-space anisotropy
 - “Faster” particles in-plane
 - Measurable in the final state!



Experimental Signal

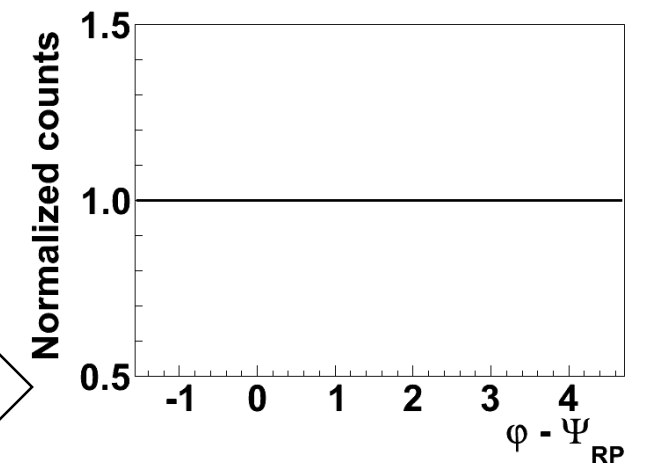
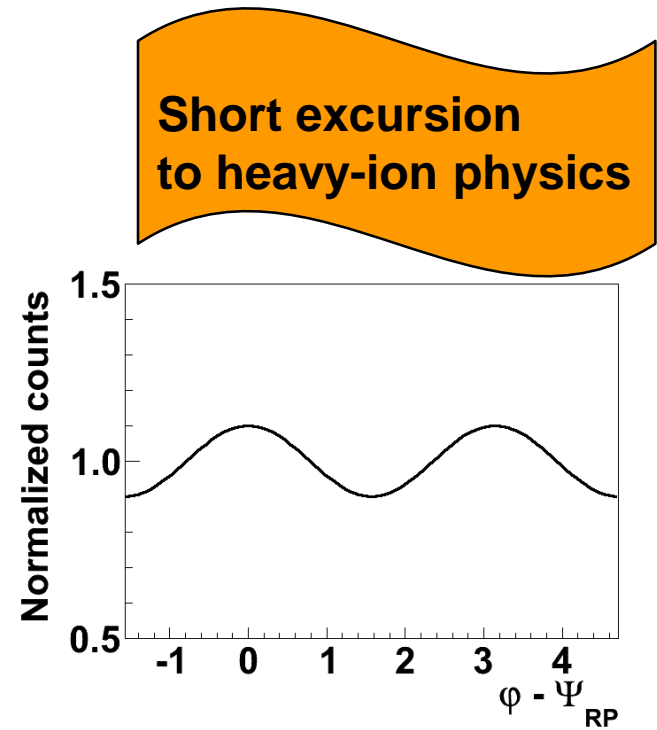
- Particles as a function of $\varphi - \Psi_{RP}$



$$\frac{dN}{d\varphi} = A(1 + 2v_2 \cos 2(\varphi - \Psi_{RP}))$$

- Define $v_2 = \langle \cos 2(\varphi - \Psi_{RP}) \rangle$
 - Second coefficient of Fourier expansion

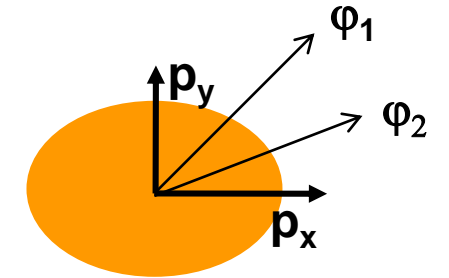
- Ψ_{RP} common *symmetry plane* (for all particles)
- What if there were no correlations with Ψ_{RP} ?



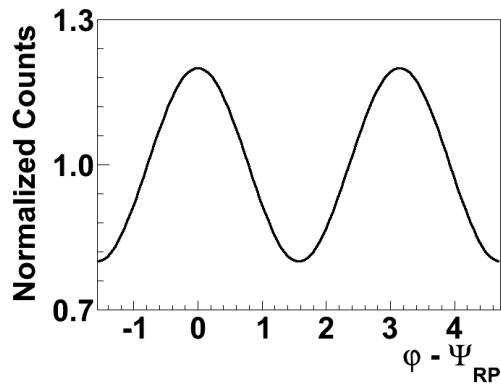
Two-Particle Correlations

Short excursion to heavy-ion physics

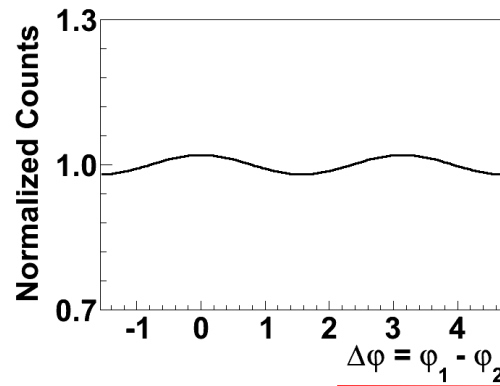
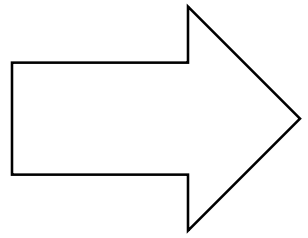
- Rewrite $v_2 = \langle \cos 2(\varphi - \Psi_{RP}) \rangle$ as $v_2 = \langle e^{i2(\varphi - \Psi_{RP})} \rangle$
- Reaction-plane estimation can be experimentally tricky
- v_2 can also be measured from 2-particle correlations



$$\langle e^{i2(\varphi_1 - \varphi_2)} \rangle = \langle e^{i2(\varphi_1 - \Psi_{RP} - (\varphi_2 - \Psi_{RP}))} \rangle = \langle e^{i2(\varphi_1 - \Psi_{RP})} \rangle \langle e^{i2(\varphi_2 - \Psi_{RP})} \rangle = v_2^2$$



$$v_2 = \langle e^{i2(\varphi - \Psi_{RP})} \rangle$$

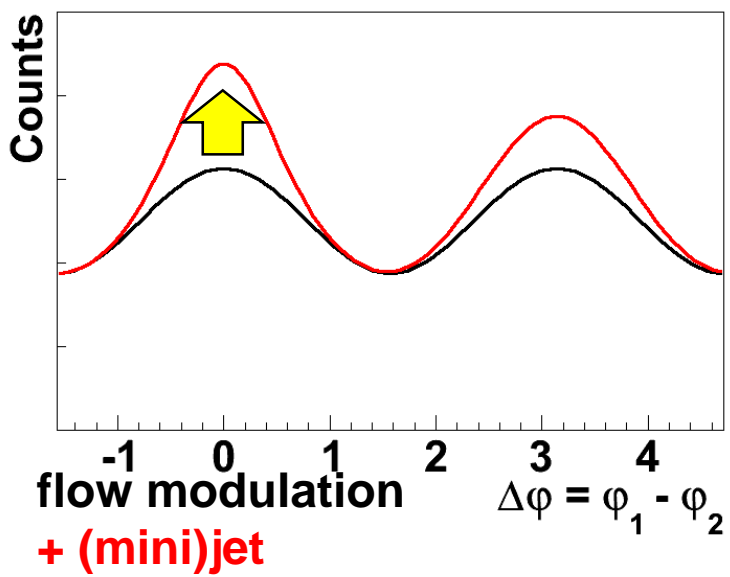


$$v_2^2 = \langle e^{i2(\varphi_1 - \varphi_2)} \rangle$$

Modulation smaller due to $v_2 \rightarrow (v_2)^2$ but statistical power similar

2D Two-Particle Correlations

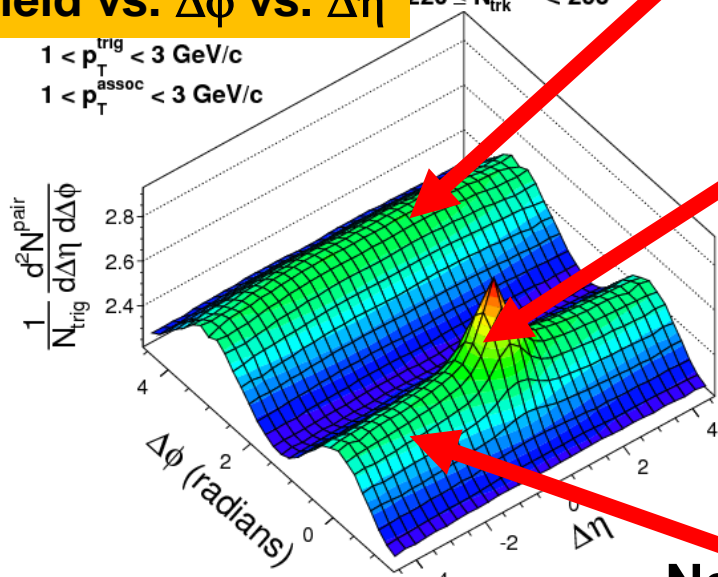
- Flow component overlaid by (mini)jet contribution
- This can also be looked at in two dimensions
 - Azimuth $\Delta\phi$ and pseudorapidity $\Delta\eta$



include $\Delta\eta$ axis

Yield vs. $\Delta\phi$ vs. $\Delta\eta$ $220 \leq N_{\text{trk}}^{\text{offline}} < 260$

$1 < p_T^{\text{trig}} < 3 \text{ GeV}/c$
 $1 < p_T^{\text{assoc}} < 3 \text{ GeV}/c$

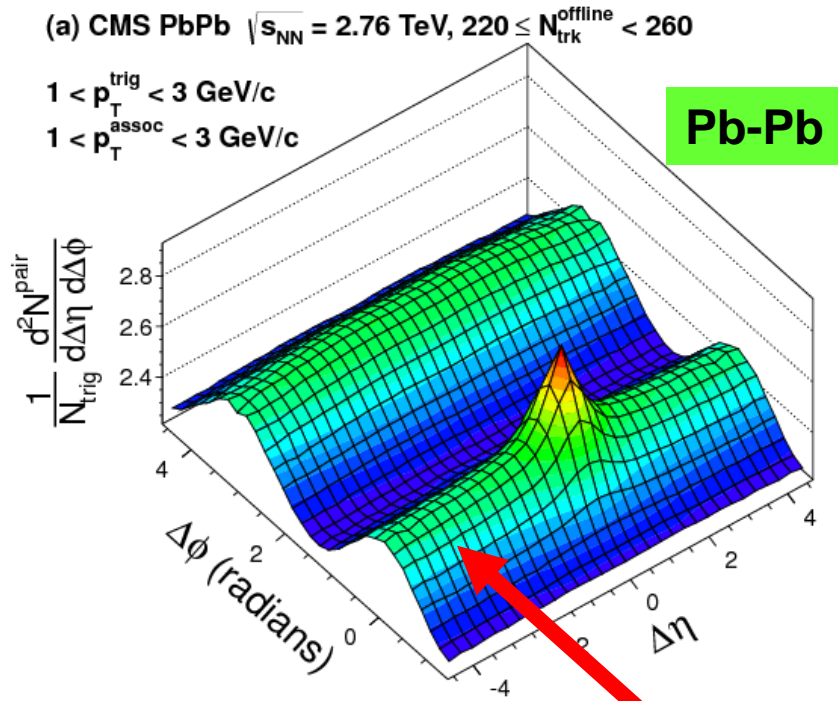


Away-side jet + flow
 $(\Delta\phi \sim \pi, \text{ elongated in } \Delta\eta)$

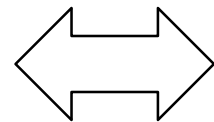
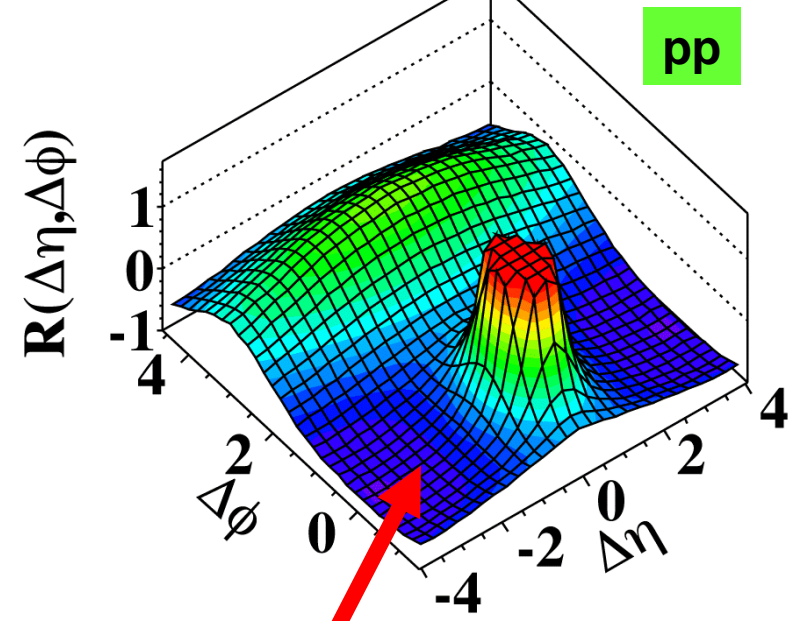
Near-side jet + resonances, ...
 $(\Delta\phi \sim 0, \Delta\eta \sim 0)$

Near-side flow ridge
 $(\Delta\phi \sim 0, \text{ elongated in } \Delta\eta)$

And in pp?



CMS 2010, $\sqrt{s}=7\text{TeV}$
 MinBias, $1.0\text{GeV}/c < p_{\text{T}} < 3.0\text{GeV}/c$



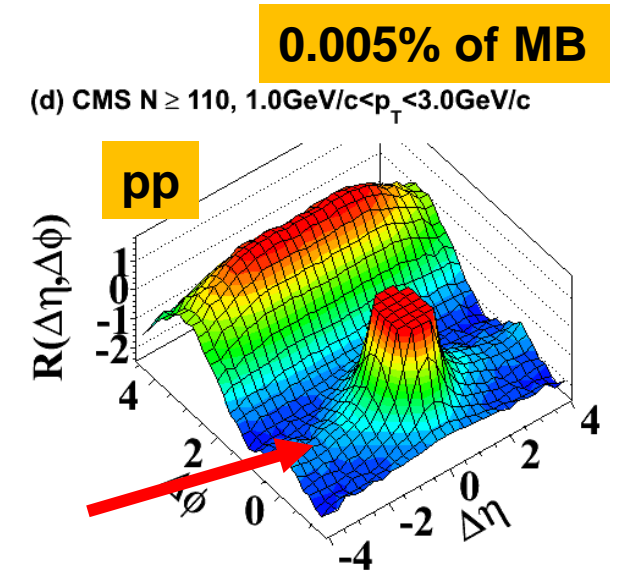
Near-side ridge
 (flow) only in Pb-Pb

at least everyone thought so for a long time...

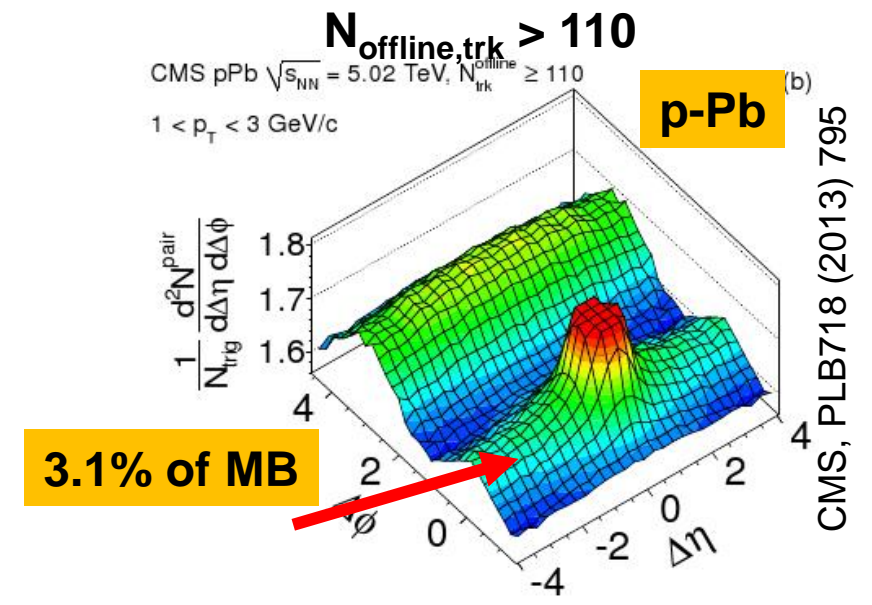


Near-Side Ridge

- ...Observed in very high-multiplicity pp collisions
 - 0.005% events with highest multiplicity
- ...observed in high multiplicity p-Pb collisions
 - ~40% events with highest multiplicity
 - Surprisingly large magnitude



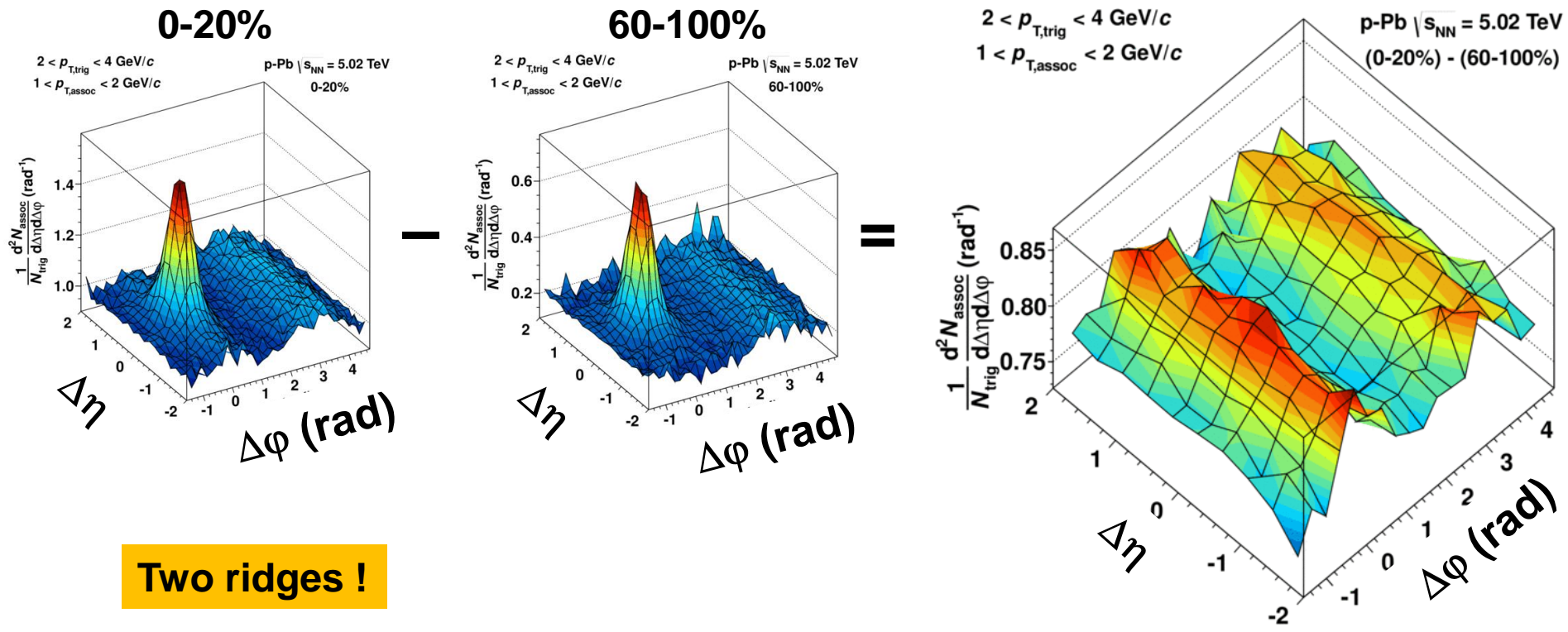
CMS, JHEP09(2010)091



CMS, PLB718 (2013) 795

Double Ridge in p-Pb

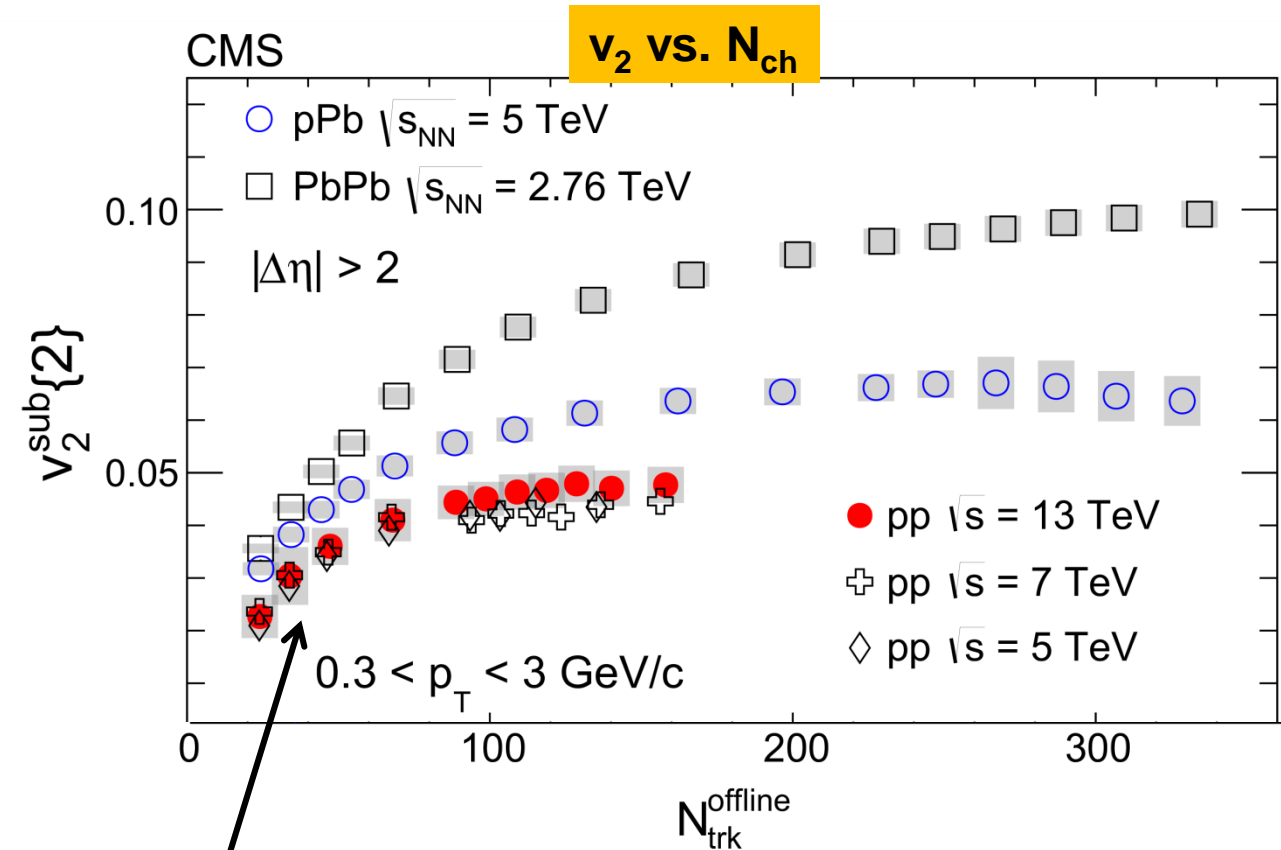
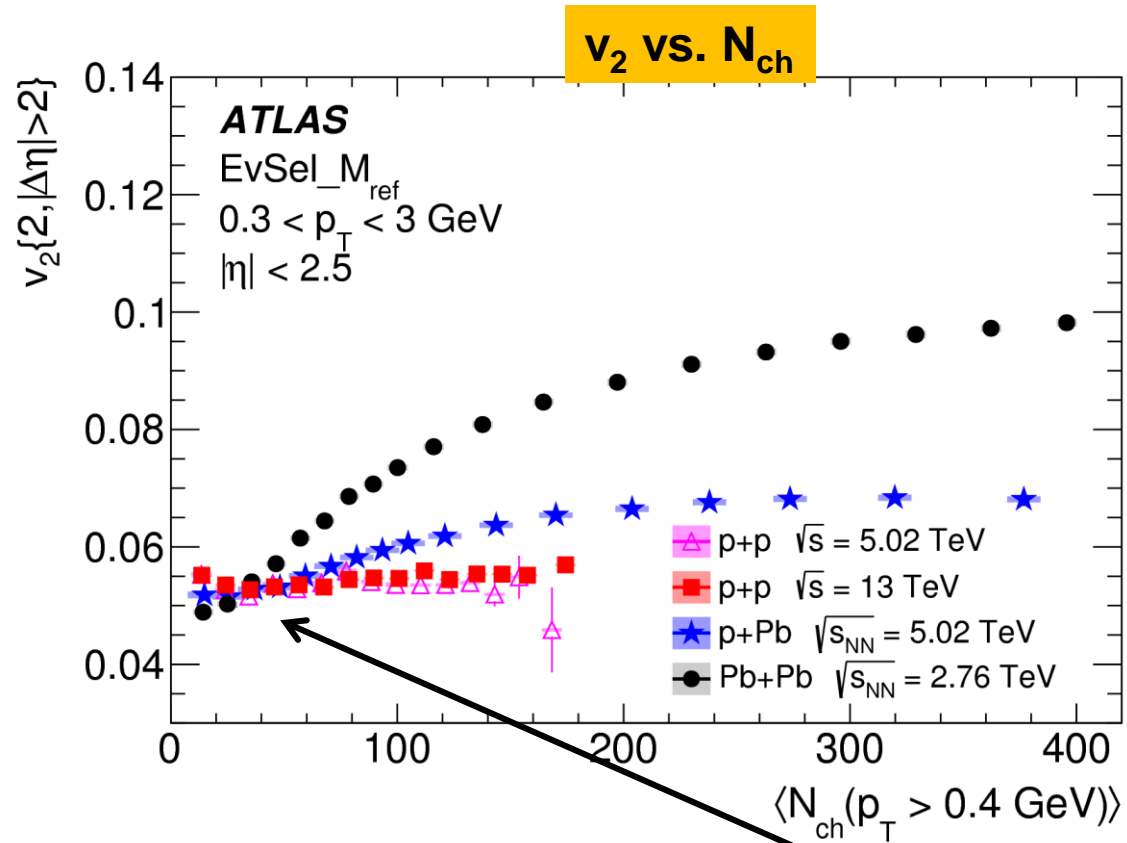
- Subtraction procedure to “isolate” ridge contribution from jet correlations
 - No ridge seen in 60-100% and similar to pp



ALICE, PLB719 (2013) 29

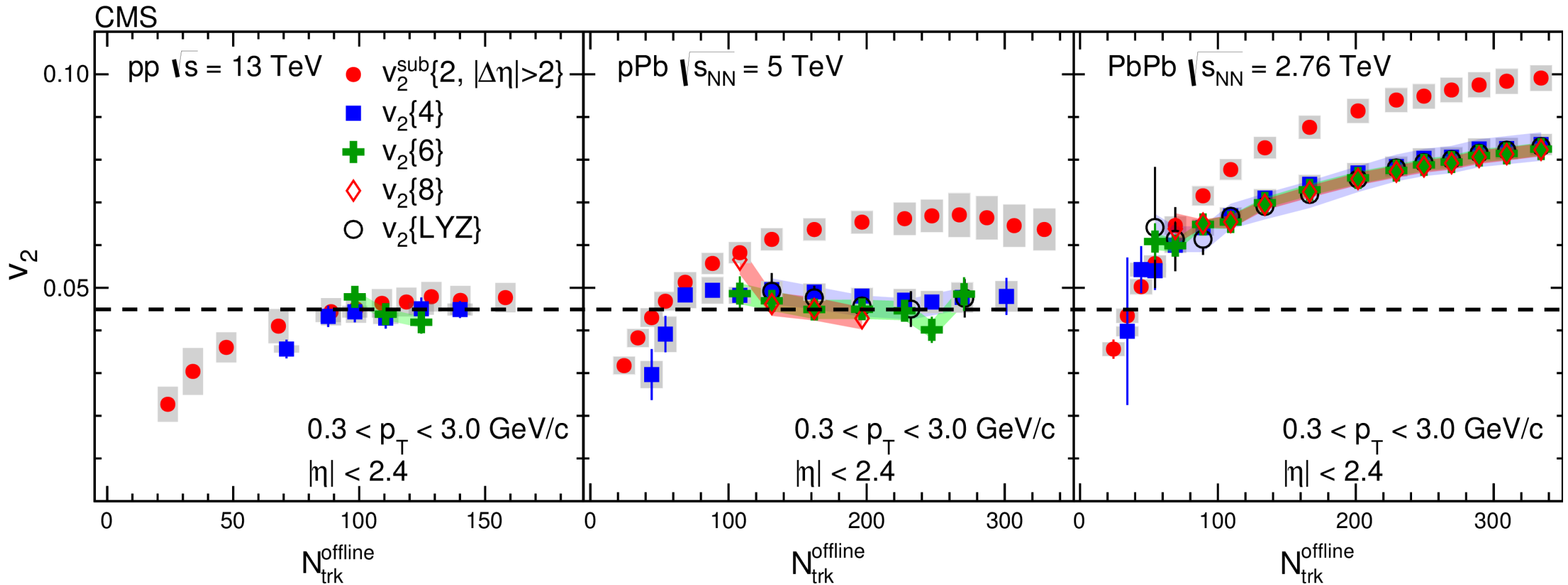
here: $\eta = \eta_{\text{lab}}$

v_2 Coefficients in pp



Low N_{ch} behaviour depends on procedure

System Comparison



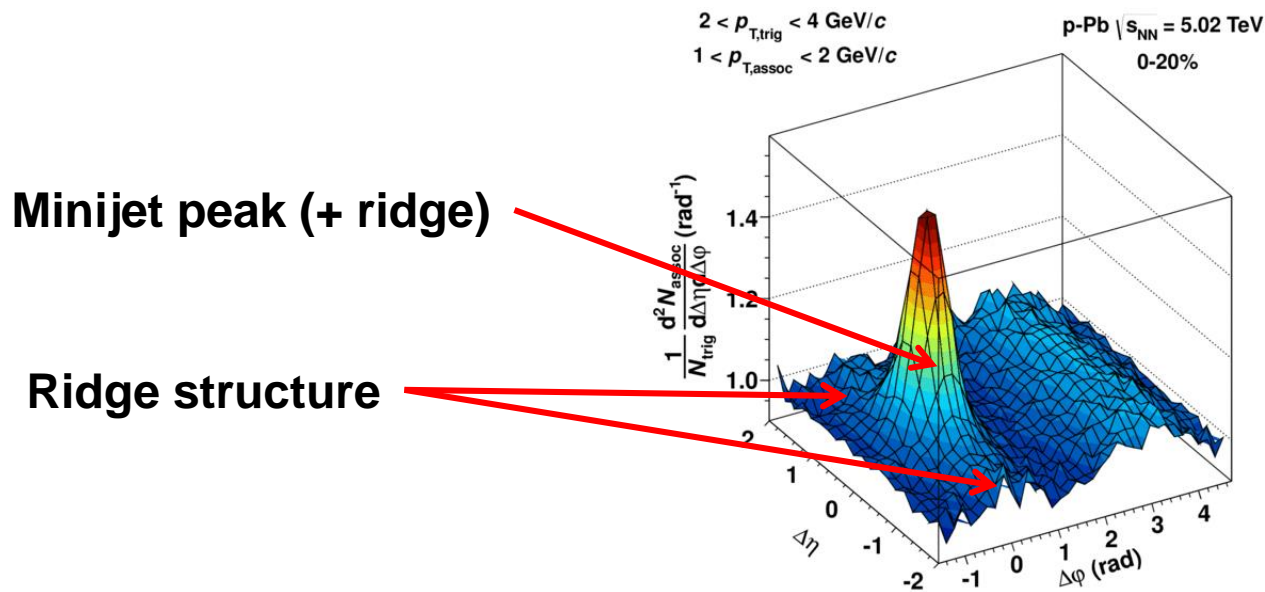
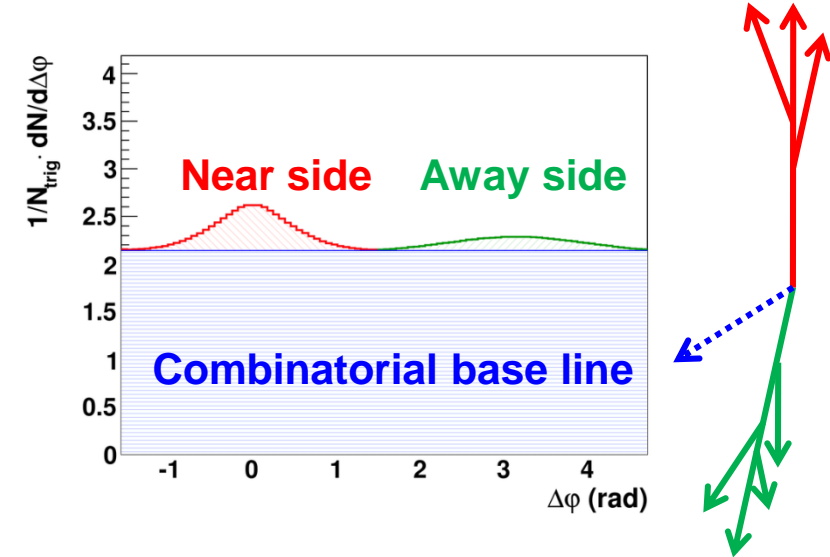


Recap

- In Pb-Pb collisions, correlations between all particles through a common symmetry planes are observed
- Small systems, p-Pb and (high-multiplicity) pp, show similar features
 - Paradigm shift in the understanding of heavy-ion collisions
- Can part of these effects be related to MPI and the correlations between them?
 - For this it is useful to answer the question if the observed ridge is related to the (mini)jet production

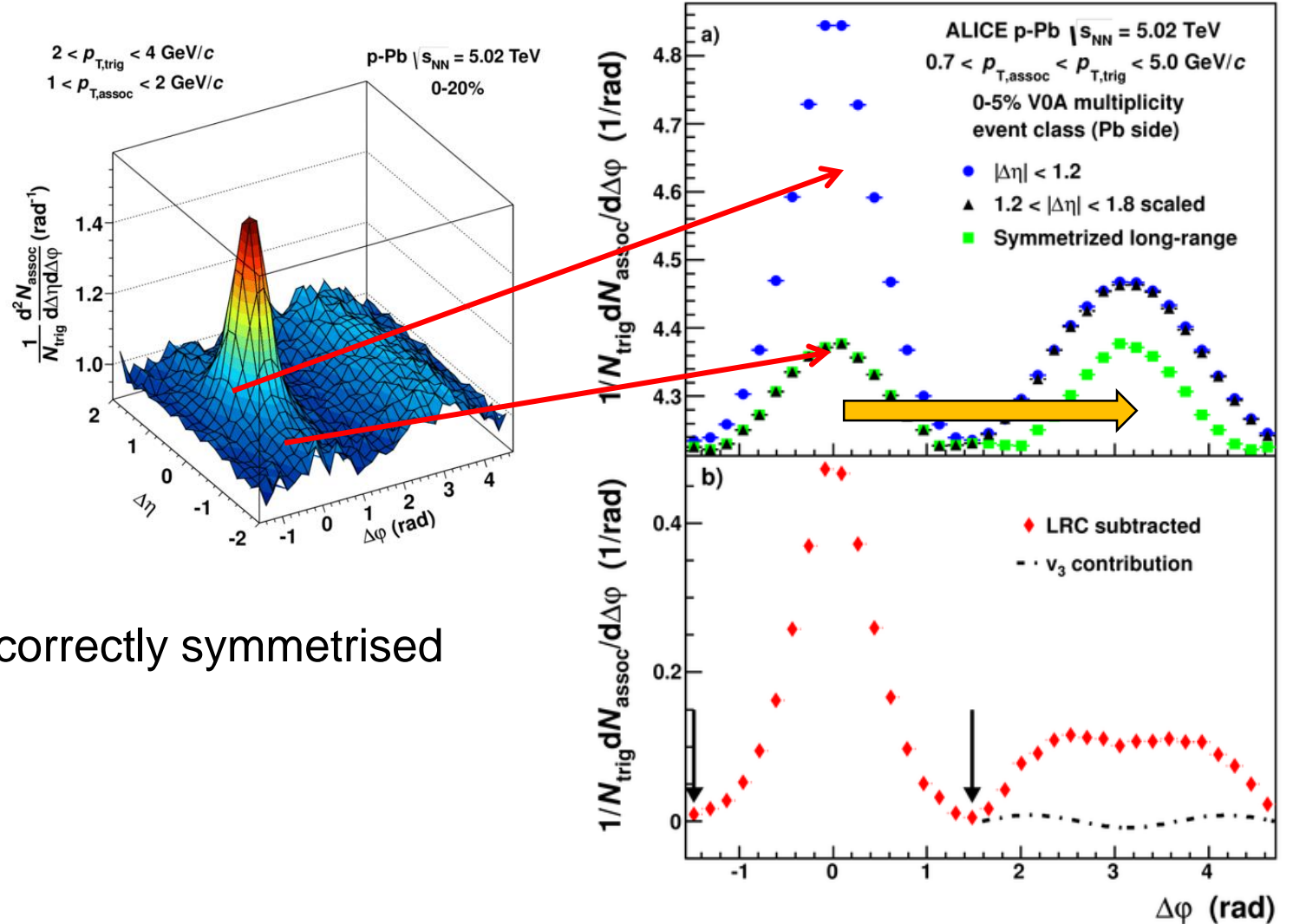
Uncorrelated Seeds in p-Pb

- Already discussed uncorrelated seeds measurement can be applied to p-Pb
 - Challenge: how to count particles in ridge?
 - Exploit two-dimensional ($\Delta\phi$ and $\Delta\eta$) near-side structure

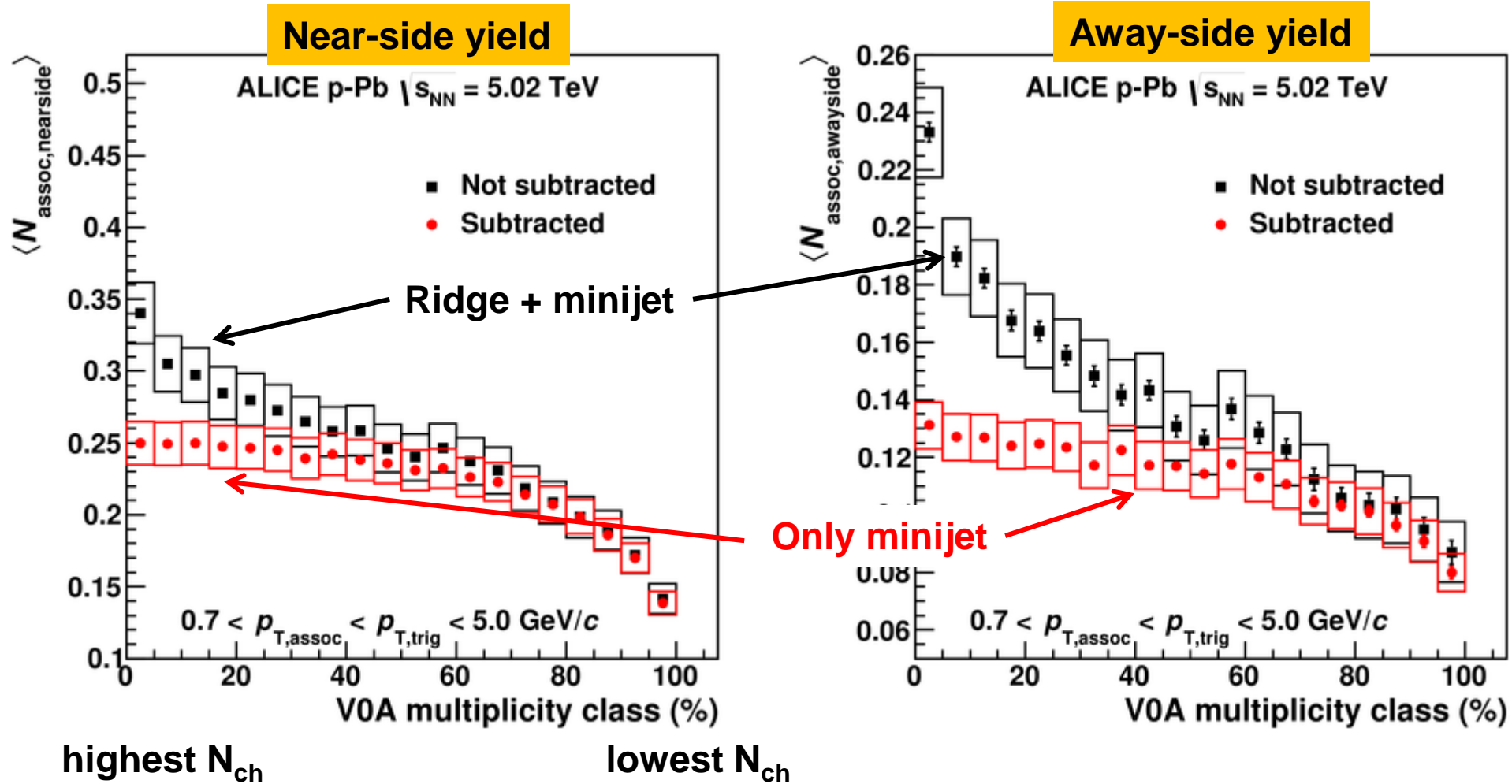


Ridge Subtraction

- Short range ($|\Delta\eta| < 1.2$)
- Long range ($|\Delta\eta| > 1.2$)
 - Symmetrise to away side
 - Subtract
- Caveats?
 - Odd harmonics (like v_3) not correctly symmetrised
→ systematic uncertainties

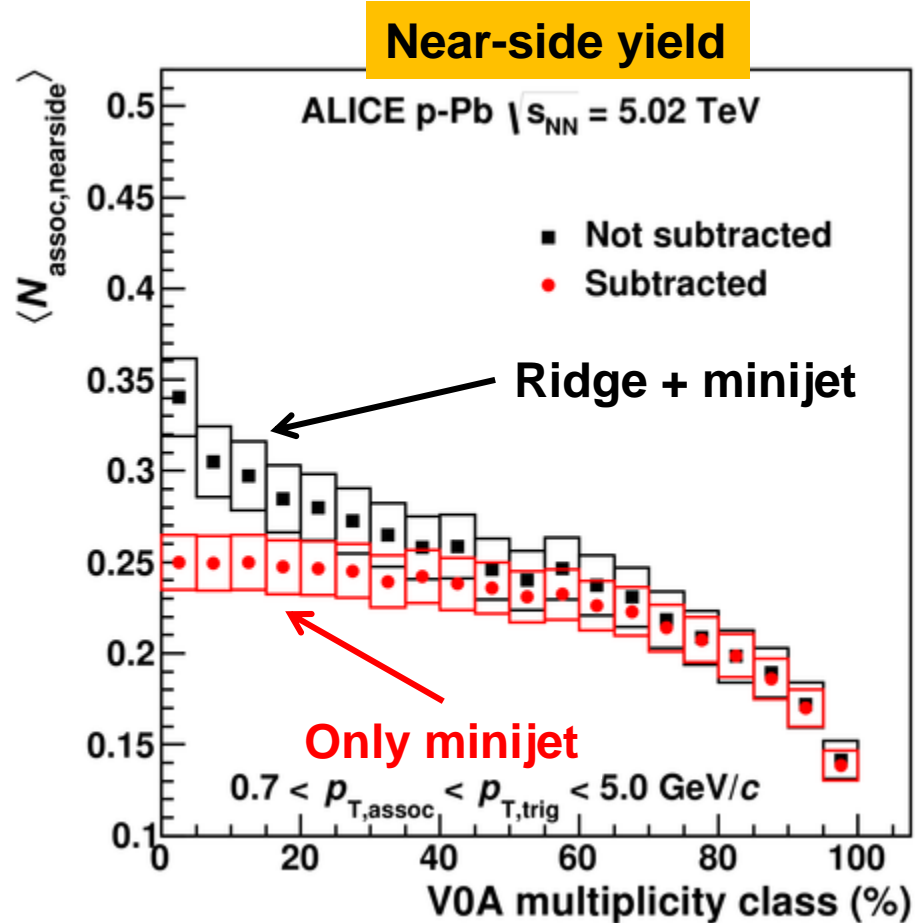


Near-Side and Away-Side Yields



Minijet contribution flattens for highest 60% multiplicity

Correlation of Hard and Soft



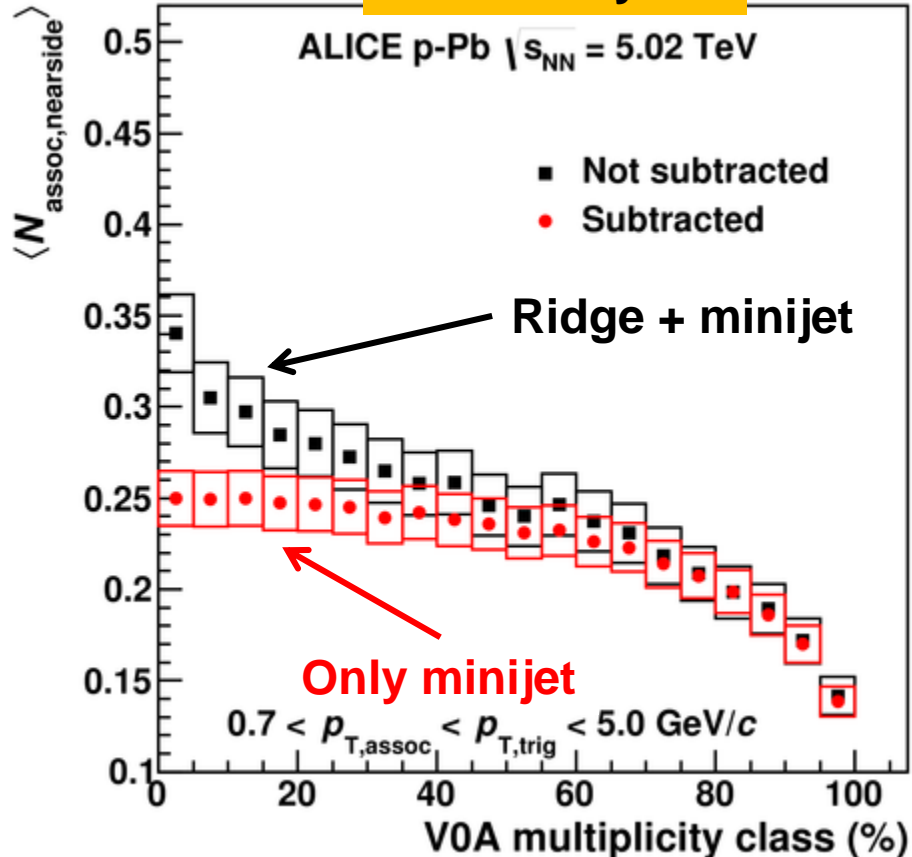
- Observable = associated yield/trigger
- Associated yield = particles from minijet
- Trigger = particles from minijet + uncorrelated bg
- Simple scenario
 - N_{minijets} with $N_{\text{associated}}$ particles each
 - Some soft background N_{soft}

$$\frac{\text{associated yield}}{\text{trigger particle}} = \frac{N_{\text{minijets}} \cdot N_{\text{assoc}}(N_{\text{assoc}} - 1)/2}{N_{\text{minijets}} \cdot N_{\text{assoc}} + N_{\text{soft}}} = \text{overall mult. } N_{\text{ch}}$$

- Quantity stays constant with N_{ch} only if N_{minijets} and N_{soft} change by same factor
 \rightarrow hard and soft particle production exhibit same evolution with multiplicity

Correlation of Hard and Soft

Near-side yield

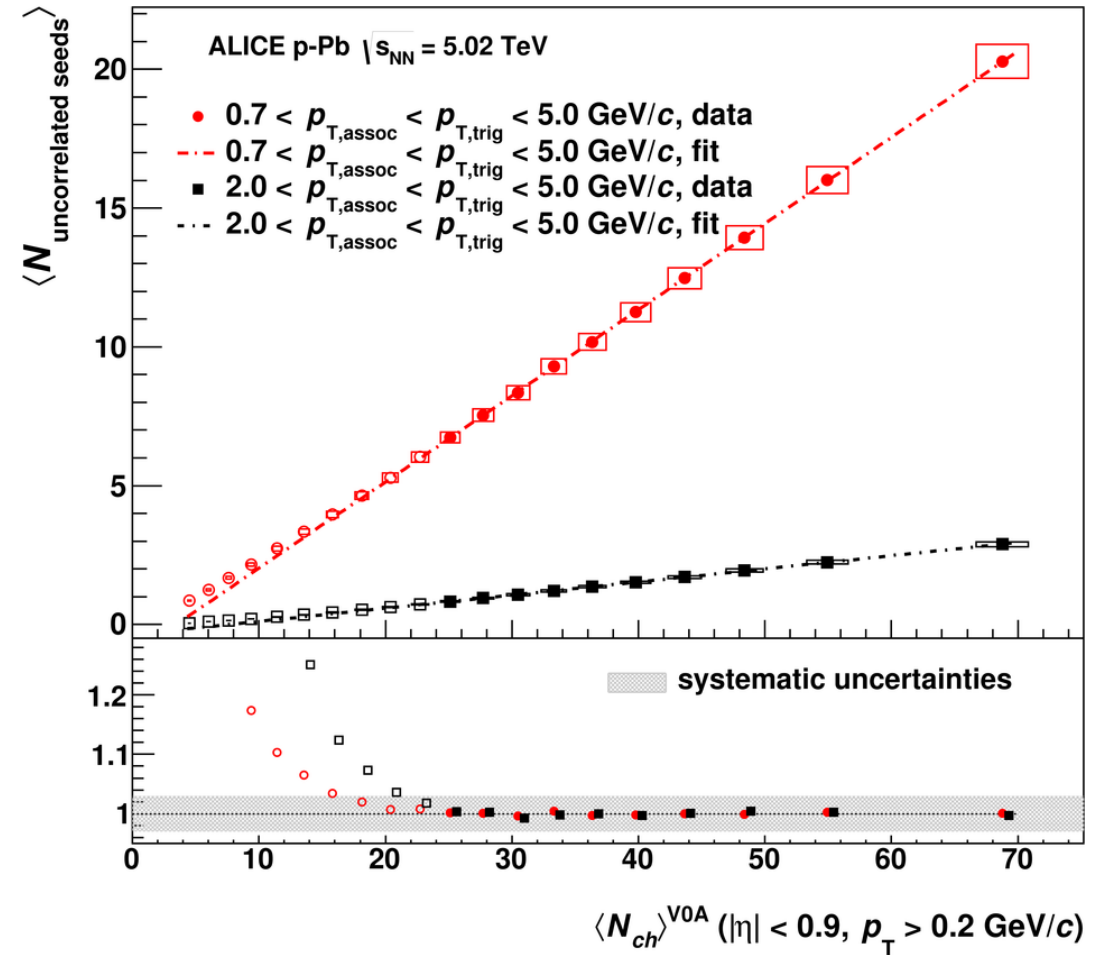
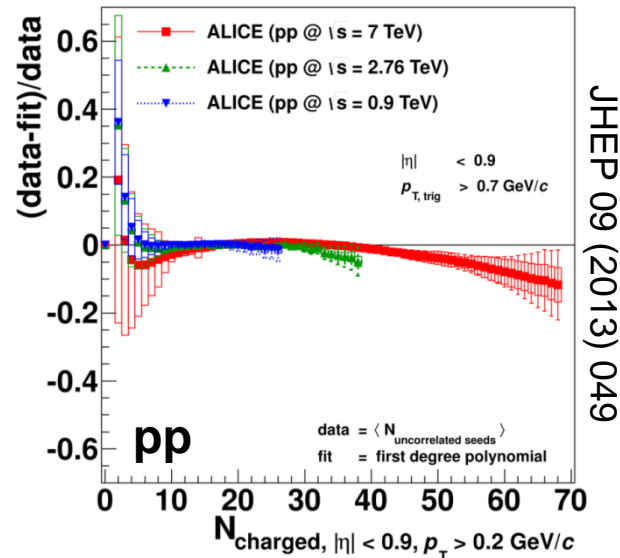


$$\frac{\text{associated yield}}{\text{trigger particle}} = \frac{N_{\text{minijets}} \cdot N_{\text{assoc}}(N_{\text{assoc}} - 1)/2}{N_{\text{minijets}} \cdot N_{\text{assoc}} + N_{\text{soft}}} = \text{overall mult. } N_{\text{ch}}$$

- Quantity stays constant with N_{ch} only if N_{minijets} and N_{soft} change by same factor \rightarrow hard and soft particle production exhibit same evolution with multiplicity
- Statement doesn't hold when ridge included
- Conclusion
 - Independent parton-parton scatterings + incoherent fragmentation produce minijets
 - Ridge is result of other source(s)

Saturation of MPI in p-Pb?

- Uncorrelated seeds after subtraction of ridge component
- Linear growths with multiplicity
- No sign of saturation of number of MPI as hinted at in pp collisions





Summary

Collective Phenomena

- Expanding hot and dense matter leads to collective phenomena
 - All particles correlated with each other through common symmetry planes
 - Text-book observable in heavy-ion collisions
- Similar effects observed in small collision systems
 - Involving ions on one side: (p-A, d-A)
 - In pp collisions well established at high N_{ch} ; under investigation at low N_{ch}
- Ridge structure in p-Pb collisions seems to be additive to minijets produced by independent parton-parton scatterings + incoherent fragmentation



Take-Home Messages

- **Multiplicity distribution** of events with different number of PI very different, but experimentally inaccessible
- **Underlying event** transverse region measures activity from additional PI in the same collision
- **Uncorrelated seeds** extracted from two-particle correlations are proportional to the number of PI (in MCs)
- Hard probes like D and J/ψ measured as a function of multiplicity are a proxy of the correlation of the **production of hard and soft probes**
- **Double parton scattering** quantifies with σ_{eff} the probability that two hard processes occur in the one collision in different parton scatterings
- Multiplicity as event characterization suffers from **various biases** which have to be considering before drawing physics conclusions
- The **collective ridge** structure observed in small systems is additive to minijets produced by MPI

Thank you for your attention!



Backup



Toy for Selection Bias

```
#include "TF1.h"
#include "TMath.h"
#include "TProfile.h"
#include "TCanvas.h"
#include "TH2F.h"

void selection_bias() {
    TF1* ptDist = new TF1("ptDist",
        "x** -4.4", 0.5, 10);
    TProfile* prof = new TProfile("prof",
        ";p_{T,lead};N_{ch}", 100, 0, 10);

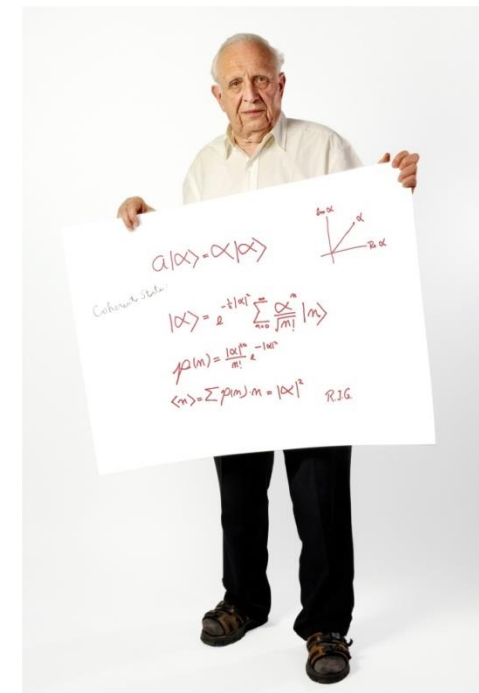
    for (int trial=0; trial<10000; trial++) {
        for (int n=1; n<50; n++) {
            double maxpt = 0;
            for (int i=0; i<n; i++)
                maxpt = TMath::Max(maxpt,
                    ptDist->GetRandom());
            prof->Fill(maxpt, n);
        }
    }

    new TCanvas;
    prof->SetStats(kFALSE);
    prof->Draw("COLZ");
}
```

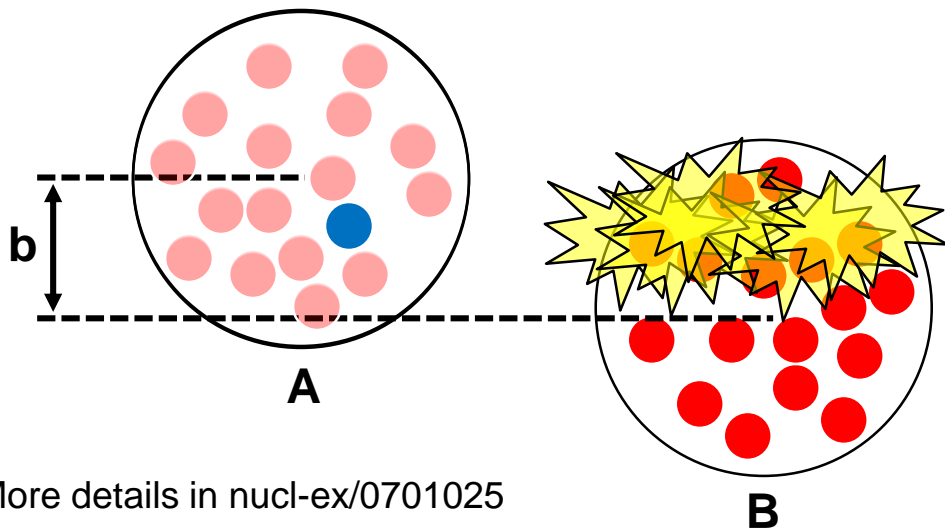


Glauber Monte Carlo

- Nucleons travel on straight lines
- Collisions do not alter their trajectory (energy of nucleons large enough)
- No quantum-mechanical interference
- Interaction probability for two nucleons is nucleon-nucleon cross-section



Roy Glauber



“Blue” nucleon has suffered 5 NN collisions

Need to repeat for all other nucleons in A

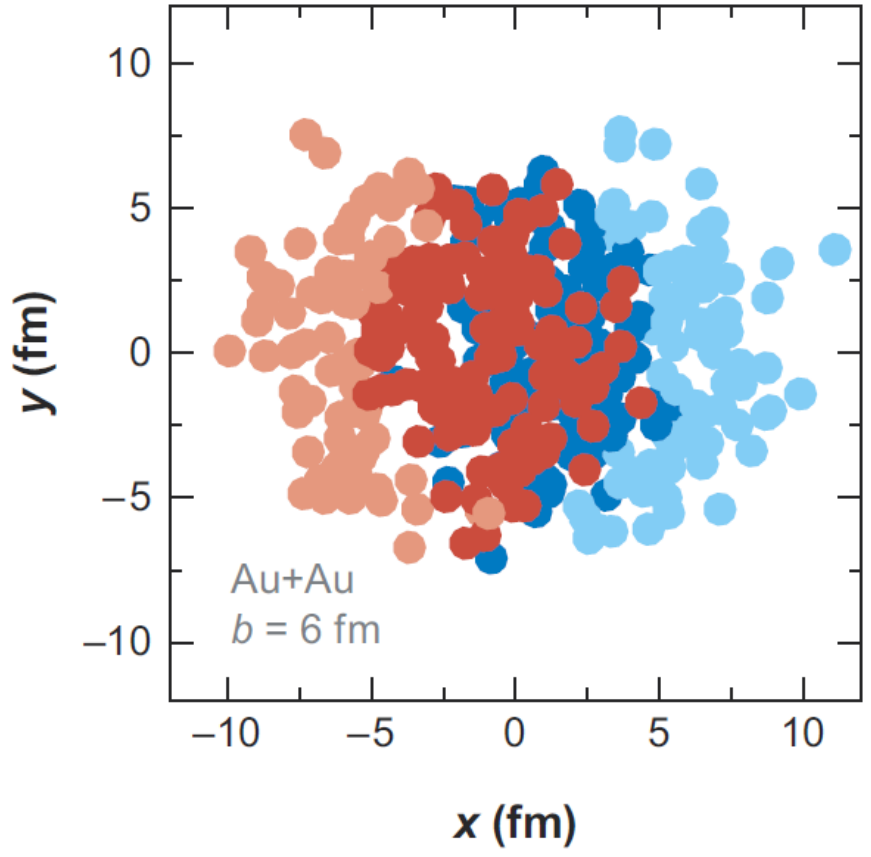
Strongly dependent on *impact parameter b*

More details in nucl-ex/0701025



Realistic Example

Transverse view



Along the beam axis

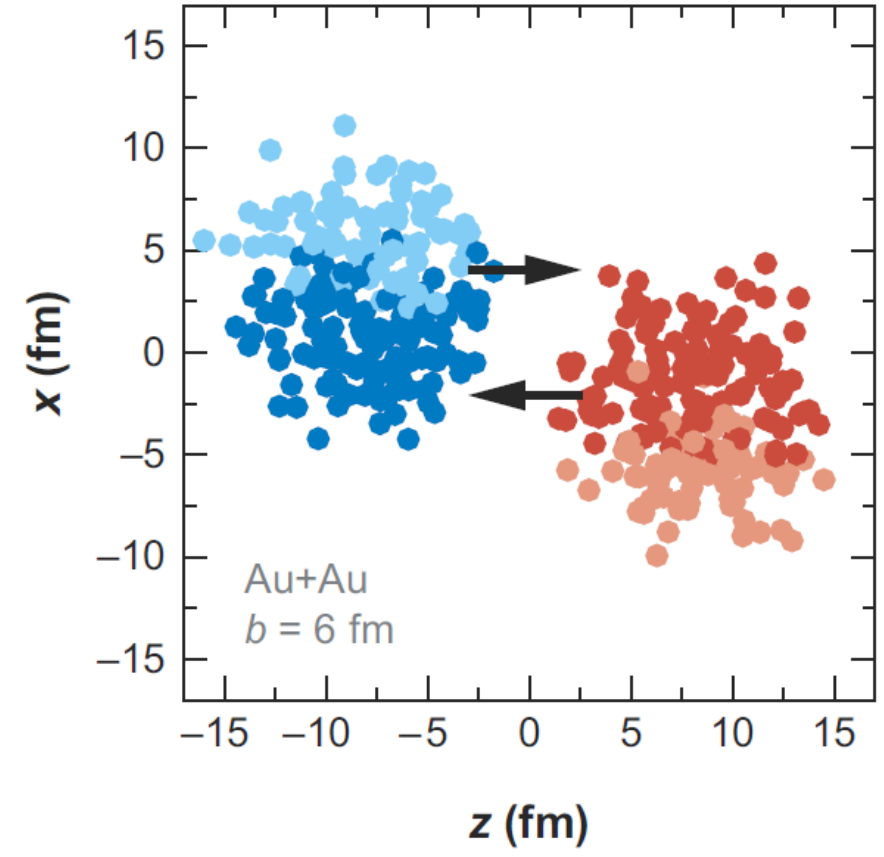


Figure: nucl-ex/0701025

Input to Glauber MC

- Distribution of nucleons in nuclei
 - Based on nuclear density
 - Typically Woods-Saxon distribution

$$\rho(r) = \rho_0 \frac{1}{1 + \exp\left(\frac{r-R}{a}\right)}$$

ρ_0 : Density in the center
 R : Nuclear radius
 a : Skin depth

- Nucleon-nucleon cross-section
 - From pp measurements / extrapolations

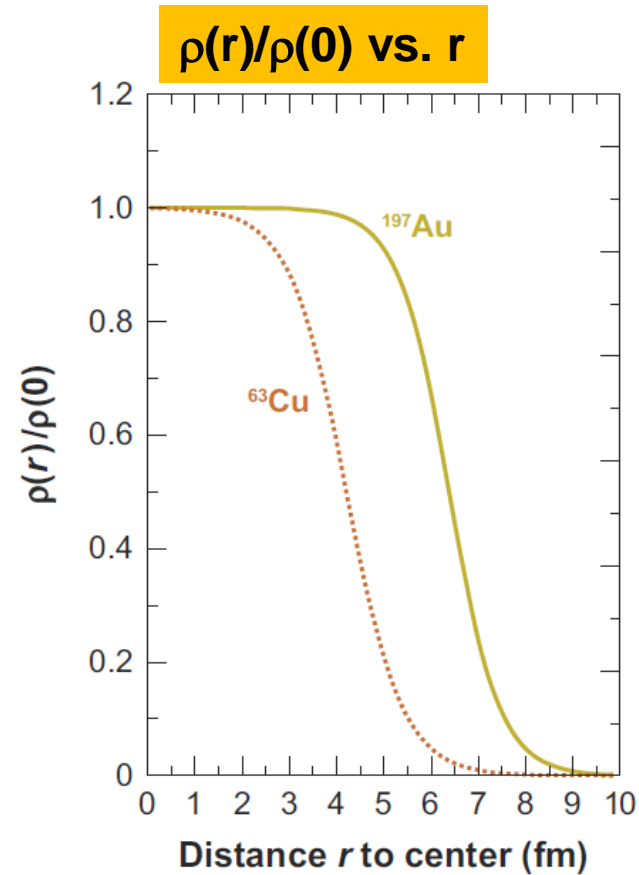
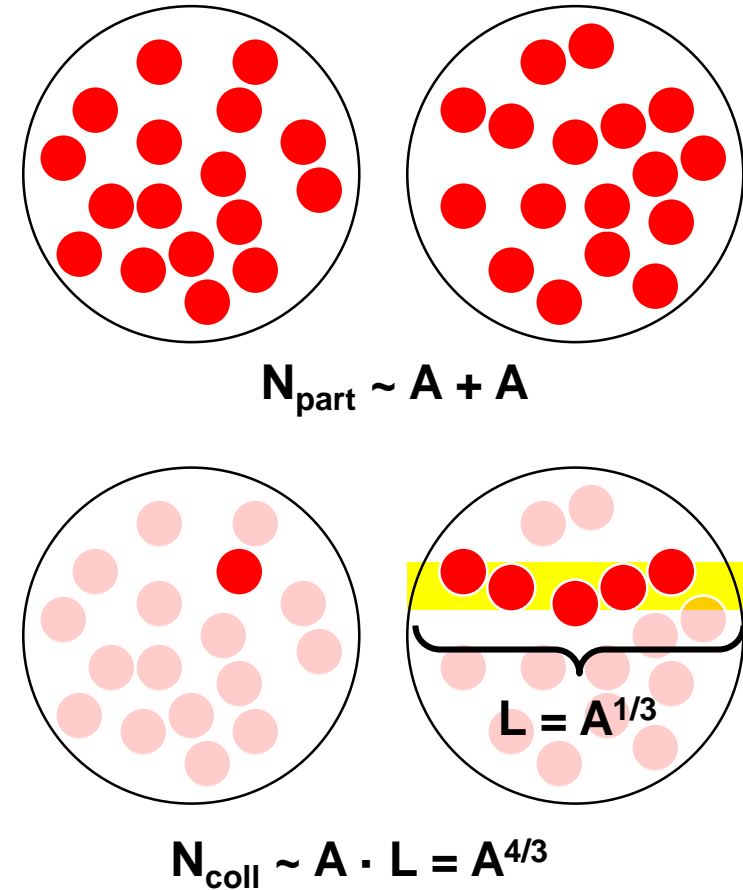


Figure: nucl-ex/0701025

Glauber MC Output

- Number of spectators
 - Nucleons which did not collide
- Participant/wounded nucleons
 - Collided at least once
 - Called N_{part}
 - Scale with $2A$ (A = number of nucleons)
- Number of binary collisions
 - Called N_{coll}
 - Scales with $A^{4/3}$
- Rule of thumb
 - Soft (low p_T) observables scale with N_{part}
 - Hard (high p_T) observables scale with N_{coll}





Glauber MC Output (2)

- 10% most central at RHIC (Au-Au, 200 GeV)
 - $N_{\text{coll}} \sim 1200$
 - $N_{\text{part}} \sim 380$
- 5% most central collisions at LHC (Pb-Pb, 5 TeV)
 - $N_{\text{coll}} \sim 1770$
 - $N_{\text{part}} \sim 384$
- Difference mainly due to cross-section increase

